

Image formation

Subhransu Maji

CMPSCI 670: Computer Vision

September 13, 2016

Administrivia and survey results

◆ Topics:

- deep learning, CNNs, machine learning, AI
- **Applications:** self driving cars, face detection/recognition, etc
- robotics, calibration, structure from motion
- graphics, text/natural language processing, speech,

◆ Goals:

- Learn fundamentals of CV/ML/image processing
- Do a supercool project
- Get an awesome industry job (e.g., space exploration @ NASA)

◆ Programming: 7.5 - 8.5, Math: 6.5 - 7.5

◆ Spire: waitlisted students? there are a few more open slots

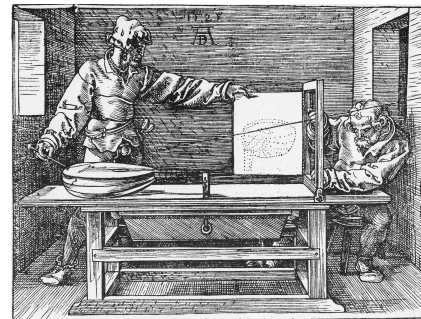
◆ Resources for vector algebra and probability added to the webpage

Overview of the next two lectures

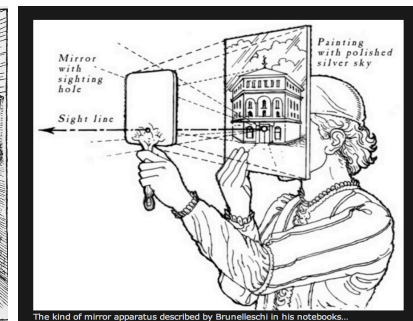
◆ The pinhole projection model

- qualitative properties
- ◆ **Cameras with lenses**
 - Depth of focus
 - Field of view
 - Lens aberrations
- ◆ **Digital cameras**
 - Sensors
 - Colors
 - Artifacts
- ◆ **Computational photography**
 - Novel sensors and cameras

Cameras

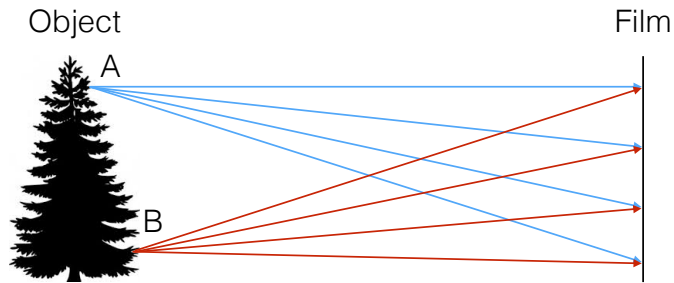


Albrecht Dürer early 1500s



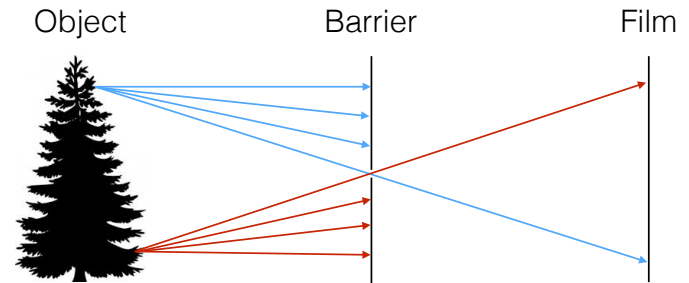
Brunelleschi, early 1400s

Lets design a camera



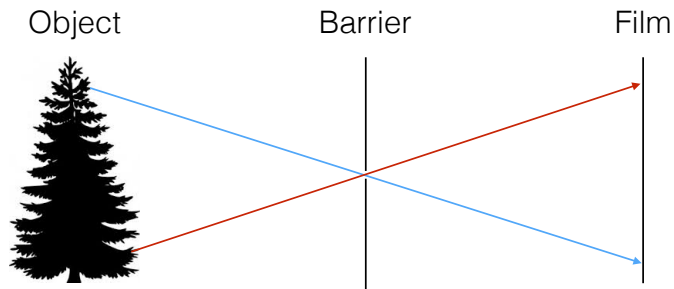
Idea 1: Lets put a film in front of an object
Do we get a reasonable image?

Pinhole camera



Add a barrier to block of most rays

Pinhole camera



- Captures pencil of rays - all rays through a single point: **aperture**, **center of projection**, **focal point**, **camera center**
- The image is formed on the **image plane**

Camera obscura



Gemma Frisius, 1558

“Camera obscura” Latin for “darkened room”

- ◆ Basic principle known to Mozi (470-390 BCE), Aristotle (384-322 BCE)
- ◆ Drawing aids for artists: described by Leonardo Da Vinci (1452-1519 AD)

Pinhole cameras are everywhere



Tree shadow during a solar eclipse
photo credit: Nils van der Burg
<http://www.physicstogo.org/index.cfm>

Accidental pinhole cameras

My hotel room,
contrast enhanced.



The view from my window



Accidental pinholes produce images that are
unnoticed or misinterpreted as shadows

A. Torralba and W. Freeman, [Accidental Pinhole and Pinspeck Cameras](#), CVPR 2012

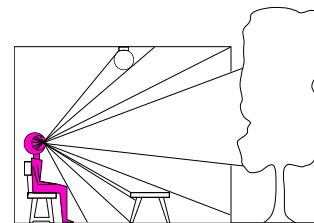
Home-made pinhole camera



<http://www.pauldebevec.com/Pinhole>

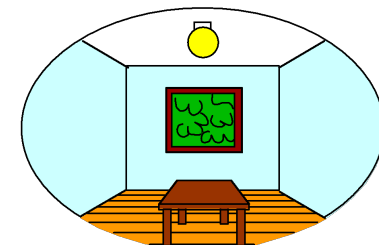
Dimensionality reduction: 3D to 2D

3D world



Point of observation

2D image



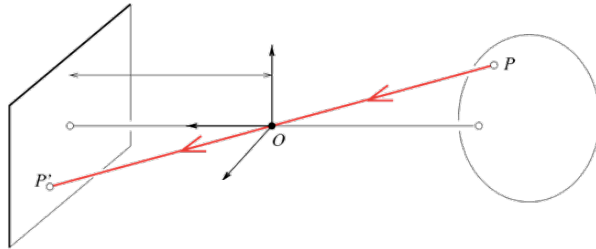
• What is preserved?

- Straight lines, incidence

• What is not preserved?

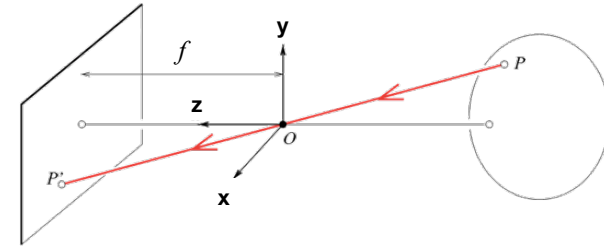
- Angles, lengths

Modeling projection



- ◆ To compute the projection P' of a scene point P , form a **visual ray** connection P to the camera center O and find where it intersects the image plane
 - ▶ All scene points that lie on this visual ray have the same projection on the image
 - ▶ Are there points for which this projection is not defined?

Modeling projection



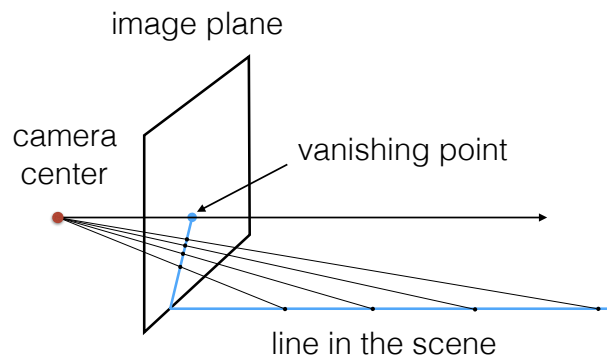
◆ The coordinate system

- ▶ The optical center (O) is at the origin
- ▶ The image plane is parallel to the xy -plane (perpendicular to the z axis)

◆ Projection equations

- ▶ Derive using similar triangles $(x, y, z) \rightarrow (f \frac{x}{z}, f \frac{y}{z})$

Projection of a line



- What if we add another line parallel to the first one?

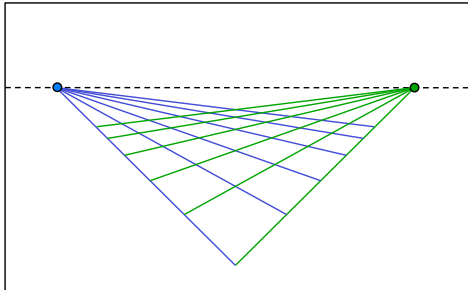
Vanishing points

- ◆ Each direction in space has its own vanishing point
 - ▶ All lines going in the that direction converge at that point
- **Exception:** directions that are parallel to the image plane

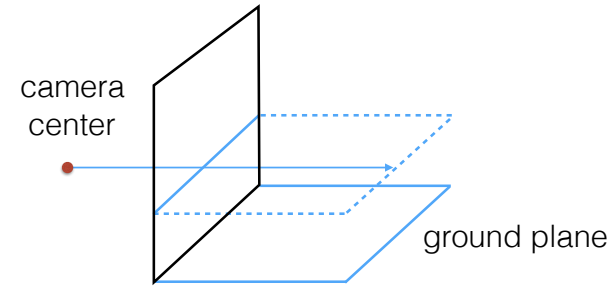


Vanishing points

- ◆ Each direction in space has its own vanishing point
 - All lines going in the that direction converge at that point
- **Exception:** directions that are parallel to the image plane
- What about the vanishing point of a plane?



The horizon



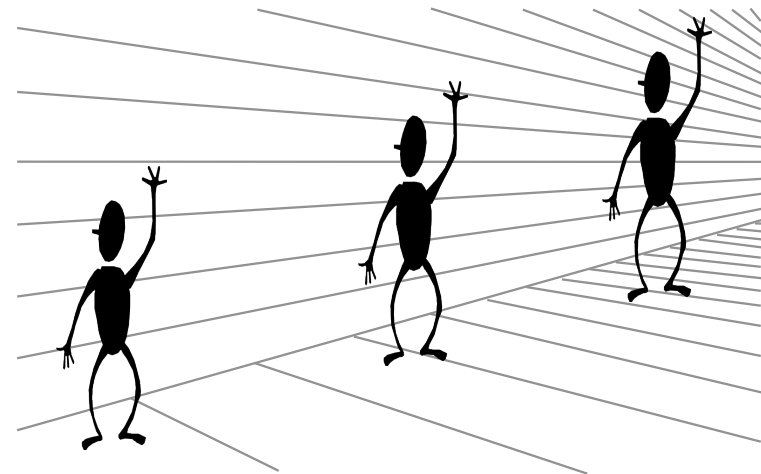
- ◆ Vanishing line of the ground plane
 - All points at the same height of the camera project to the horizon
 - Points above the camera project above the horizon
 - Provides a way of comparing heights of objects

The horizon

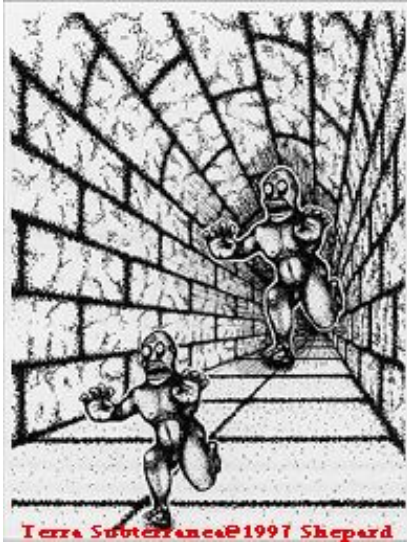


Is the person above or below the viewer?

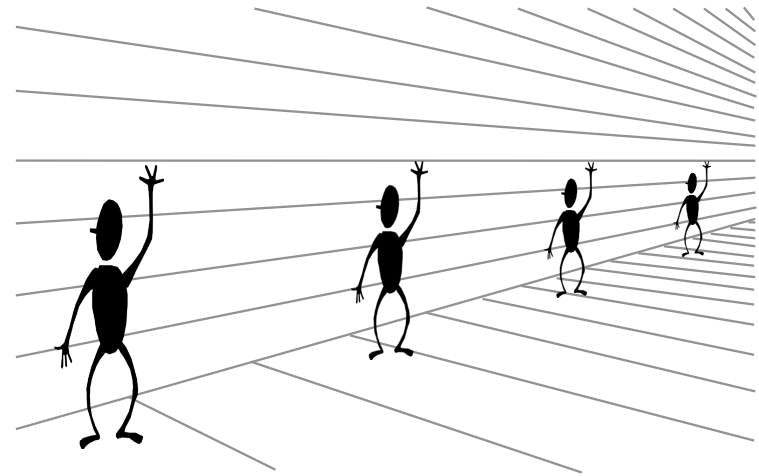
Perspective cues



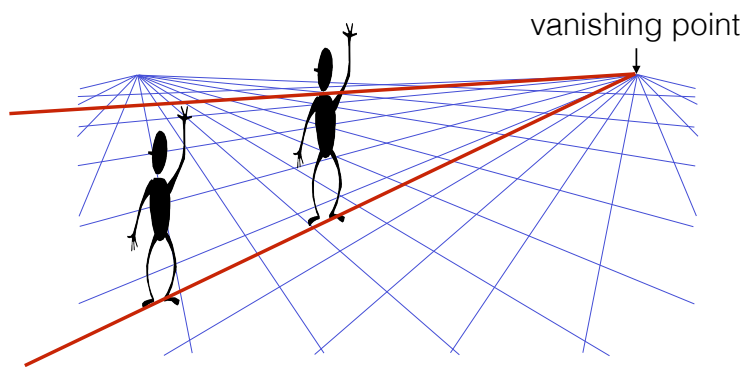
Perspective cues



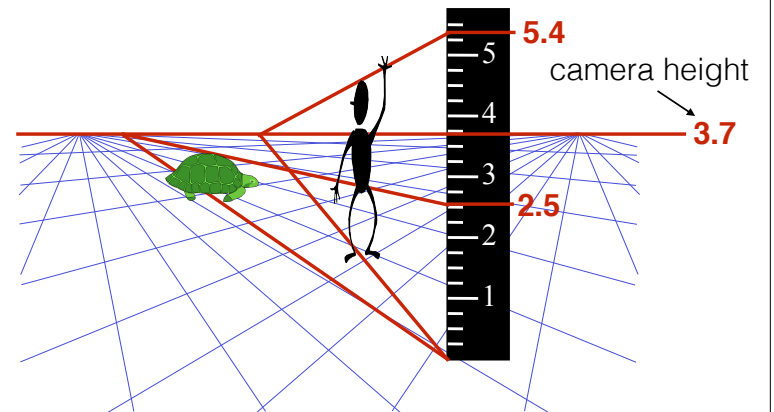
Perspective cues



Comparing heights

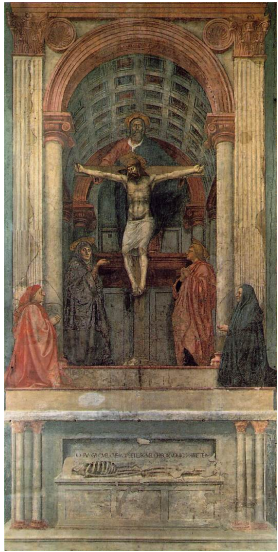


Measuring heights



What is the height of the camera?

Perspective in art



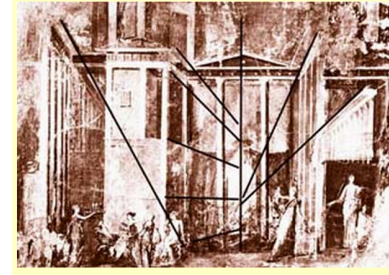
Masaccio,
Trinity, Santa
Maria Novella,
Florence,
1425-28

One of the first
consistent
uses of
perspective in
Western art

Perspective in art

(At least partial) Perspective projections in art well before the Renaissance

Several Pompeii wallpaintings show the fragmentary use of linear perspective:

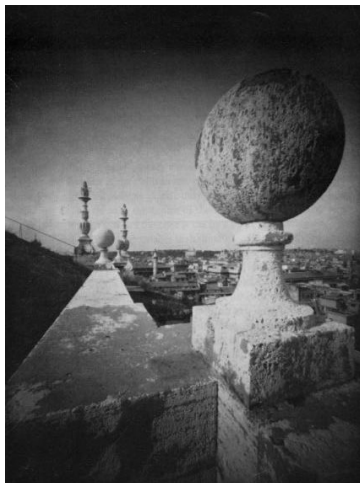


From ottobwiersma.nl

Also some Greek examples,
So apparently pre-renaissance...

Perspective distortion

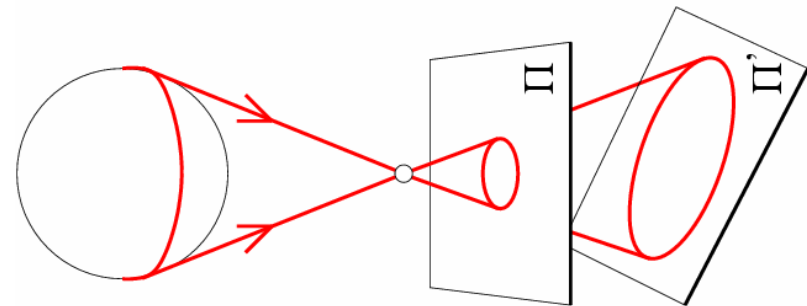
- ◆ What does a sphere project to?



M. H. Pirenne

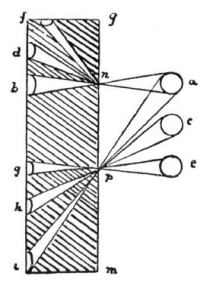
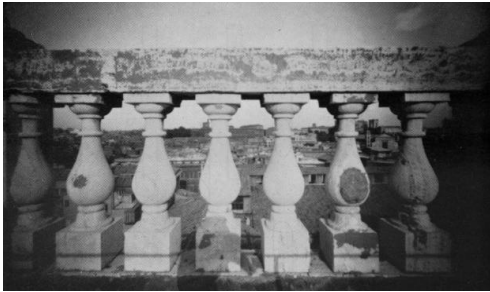
Perspective distortion

- ◆ What does a sphere project to?



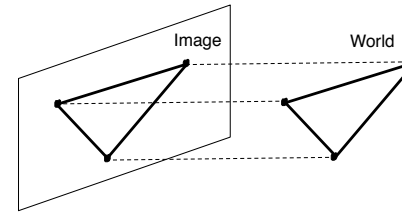
Perspective distortion

- ◆ The exterior looks bigger
- ◆ The distortion is not due to lens flaws
- ◆ Problem pointed out by Da Vinci



Orthographic projection

- ◆ Special case of perspective projection
 - Distance of the object from the image plane is infinite
 - Also called the “parallel projection”



Orthographic projection

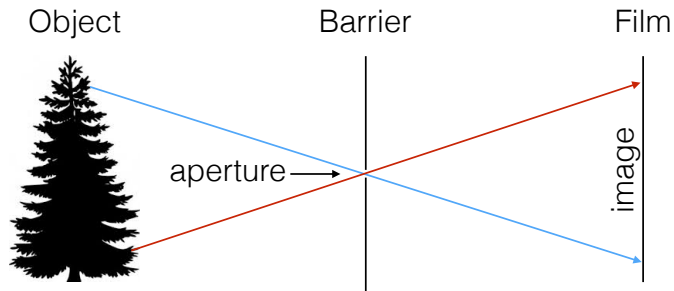
- ◆ Special case of perspective projection
 - Distance of the object from the image plane is infinite
 - Also called the “parallel projection”



Overview of the next two lectures

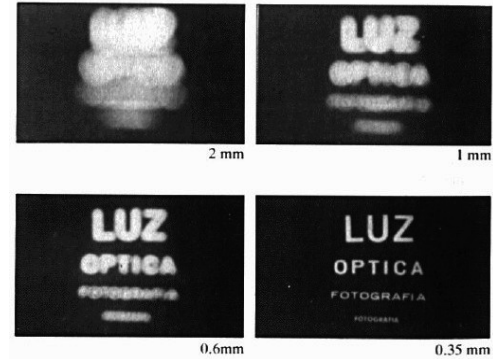
- ◆ The pinhole projection model
 - Qualitative properties
- ◆ Cameras with lenses
 - Depth of focus
 - Field of view
 - Lens aberrations
- ◆ Digital cameras
 - Sensors
 - Colors
 - Artifacts
- ◆ Novel cameras
 - Computational photography

Pinhole camera



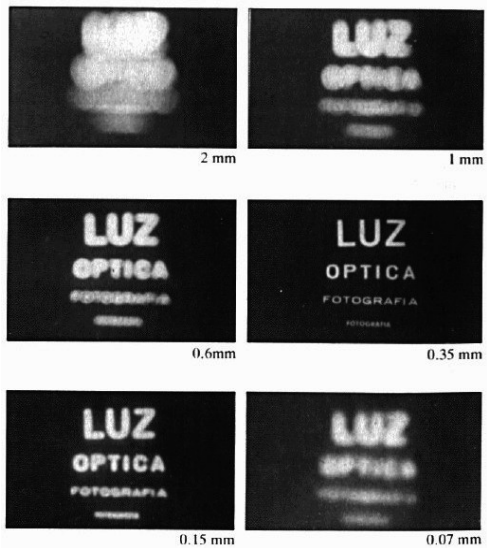
- Captures **pencil of rays** - all rays through a single point: **aperture, center of projection, focal point, camera center**
- The image is formed on the **image plane**

Shrinking the aperture

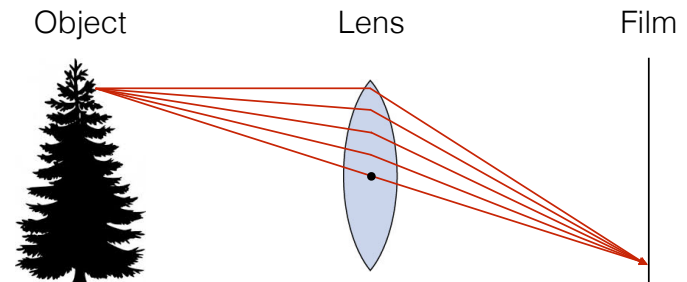


- ◆ Why not make the aperture as small as possible?
 - Less light gets through
 - Diffraction effects

Shrinking the aperture

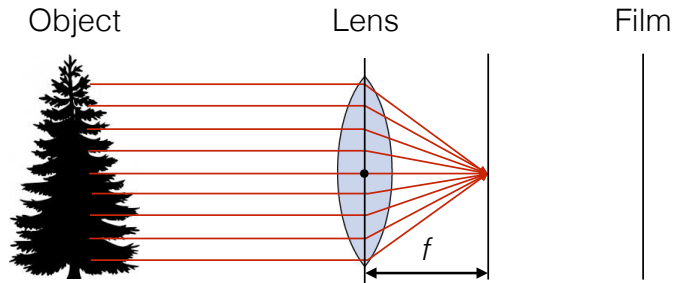


Adding a lens



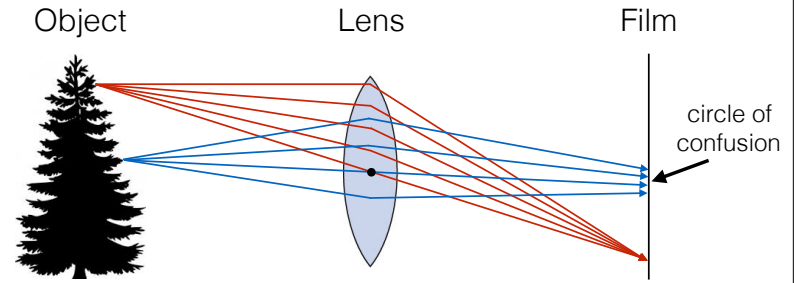
- ◆ A lens focuses light on to the film
 - **Thin lens model:**
 - Rays passing through the center are not deviated (pinhole projection model still holds)

Adding a lens



- ◆ A lens focuses light on to the film
- **Thin lens model:**
 - Rays passing through the center are not deviated (pinhole projection model still holds)
 - All parallel rays converge to one point on a plane located at the *focal length* f

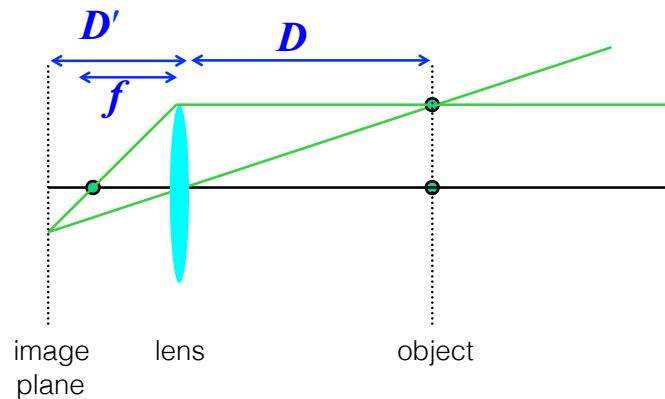
Adding a lens



- ◆ A lens focuses light on to the film
- There is a specific distance at which objects are “in focus”
- other points project on to a “circle of confusion” in the image

Thin lens formula

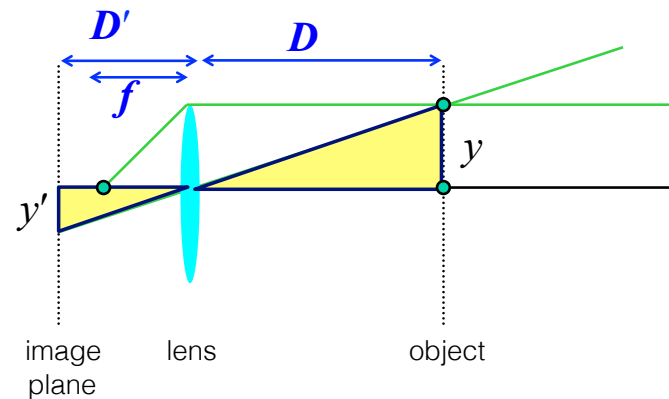
- ◆ What is the relation between the focal length (f), the distance of the object from the optical center (D) and the distance at which the object will be in focus (D')?



Thin lens formula

- ◆ Similar triangles everywhere!

$$y'/y = D'/D$$

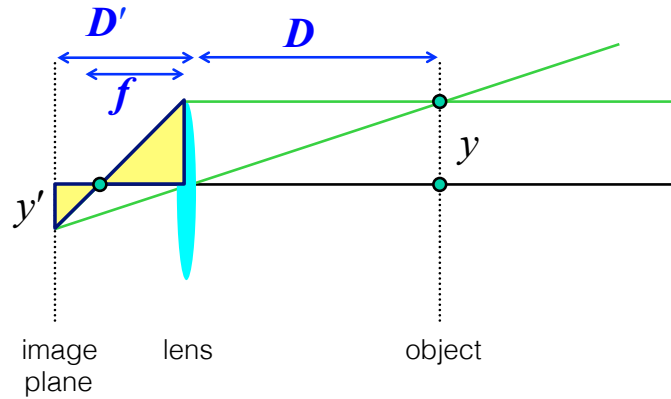


Thin lens formula

- Similar triangles everywhere!

$$y'/y = D'/D$$

$$y'/y = (D'-f)/f$$



CMPSCI 670

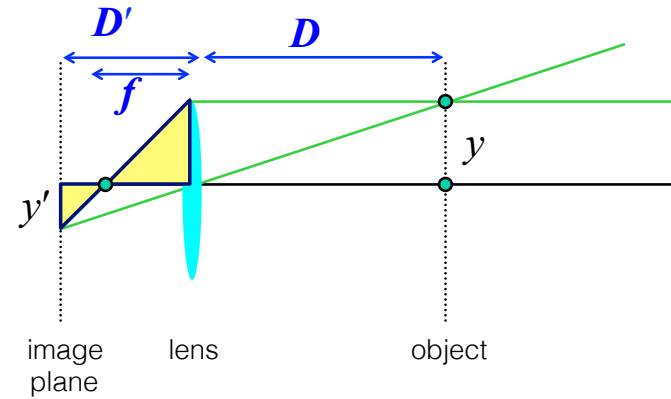
Subhransu Maji (UMass, Fall 16)

Slide by F. Durand 41

Thin lens formula

$$\frac{1}{D'} + \frac{1}{D} = \frac{1}{f}$$

Any point satisfying the thin lens equation is in focus

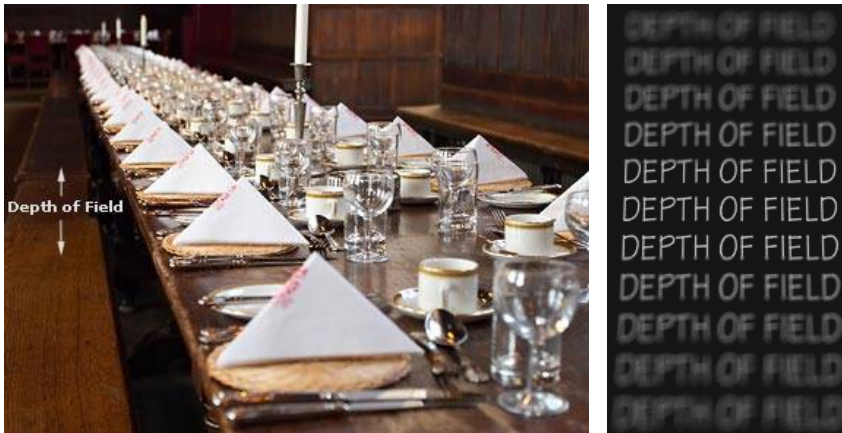


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Slide by F. Durand 42

Depth of field



<http://www.cambridgeincolour.com/tutorials/depth-of-field.htm>

DOF is the distance between the nearest and farthest objects in a scene that appear acceptably sharp in an image

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Slide by A.Efros 43

Varying the aperture



Large aperture = small DOF

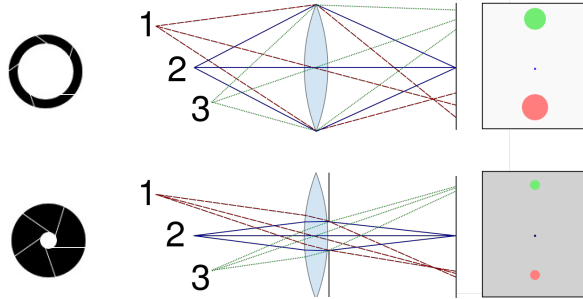
Small aperture = large DOF

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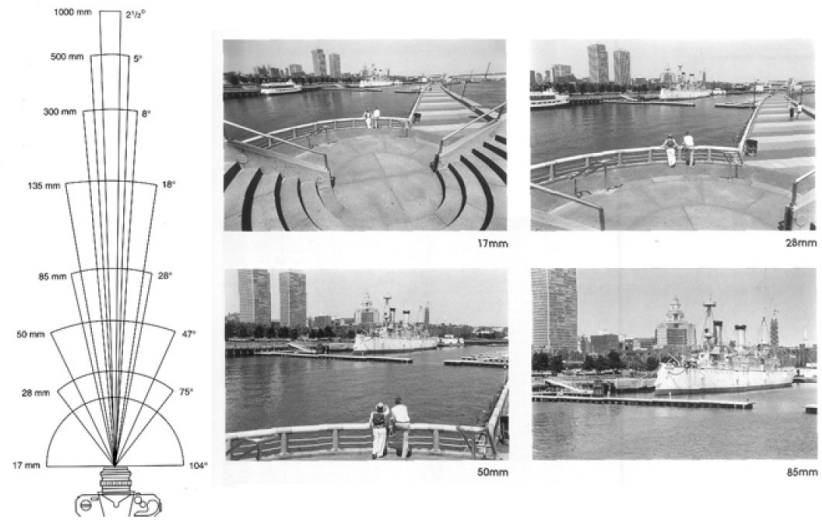
Slide by A.Efros 44

Controlling depth of field

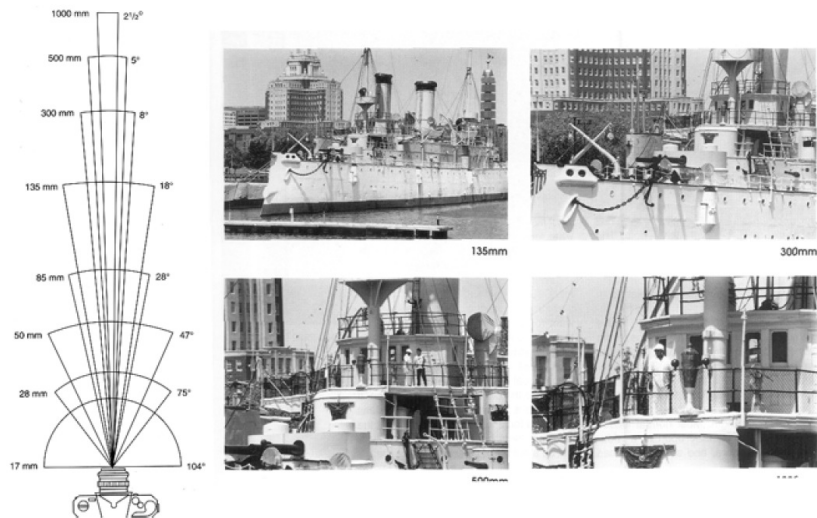


- ◆ Changing the aperture size affects the depth of field
 - ▶ A smaller aperture increases the range in which the object is approximately in focus
 - ▶ But small aperture reduces the amount of light — need to increase the exposure for contrast
 - ▶ Pinhole camera has an infinite depth of field

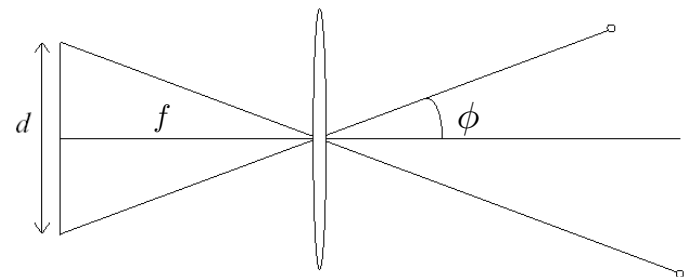
Field of view



Field of view



Field of view

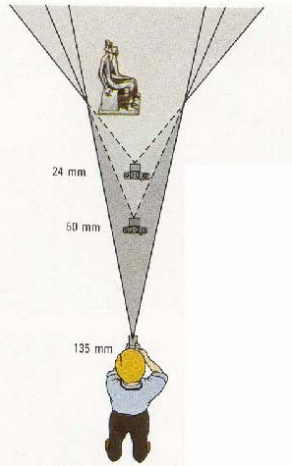


- ◆ Field of view (FOV) depends on the focal length and the size of the camera retina

$$\phi = \tan^{-1} \left(\frac{d}{2f} \right)$$

Larger focal length = smaller FOV

Field of view, focal length



$$\tan(\phi) \times 2f = d$$

$$\sim (\phi) \times 2f = d$$



Large FOV, small f — Camera close to the car



Small FOV, large f — Camera far from the car

Same effect for faces



wide-angle
(short focus)

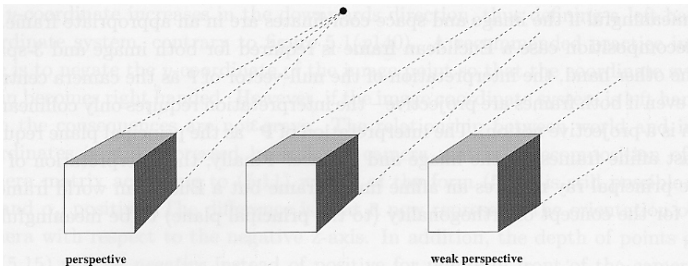


standard



telephoto
(long focus)

Approximating an orthographic camera

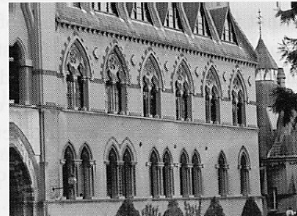
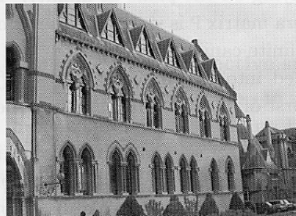


perspective

weak perspective

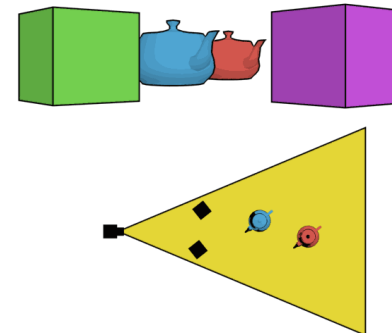
increasing focal length

increasing distance from camera



The dolly zoom

- Continuously adjusting the camera focal length while the camera moves away from (or towards) the subject



http://en.wikipedia.org/wiki/Dolly_zoom

The dolly zoom

- ◆ Continuously adjusting the camera focal length while the camera moves away from (or towards) the subject
- ◆ Also called as “Vertigo shot” or the “Hitchcock shot”



[Example of dolly zoom from Goodfellas](#)

[Example of dolly zoom from La Haine](#)

Image formation ...

Subhransu Maji

CMPCSCI 670: Computer Vision

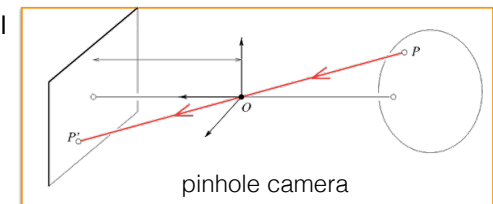
September 13, 2016

Administrivia

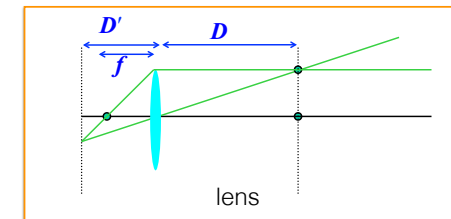
- ◆ **Homework 01** posted
 - ▶ Due Sept 15, 1pm (That's this **Thursday** before class)
 - ▶ Submissions as pdf via **Moodle** only
 - Any combination of Latex, Word, print + scan, etc.
- ◆ **Mini-project 1** posted
 - ▶ Due Sept 29
- ◆ Sign up on **Piazza** for announcements
 - ▶ I'll use this as the primary place for announcements
- ◆ Lecture slides and materials are posted on **webpage**
- ◆ **TA office hours**:
 - ▶ Wednesday 3-4PM, Location: CS 245
- ◆ **Waitlisted students?**
 - ▶ Definitely talk to me after class (OH: Today, 2:30 - 3:30pm, CS 274)

Recap of the last lecture

- ◆ The pinhole projection model
 - ▶ Qualitative properties
- ◆ **Cameras with lenses**
 - ▶ Depth of focus
 - ▶ Field of view
 - ▶ **Lens aberrations**
- ◆ **Digital cameras**
 - ▶ Sensors
 - ▶ Colors
 - ▶ Artifacts
- ◆ **Computational photography**
 - ▶ Novel sensors and cameras



pinhole camera

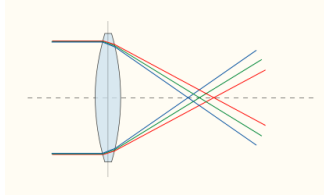


lens



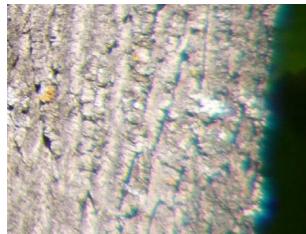
Lens flaws: Chromatic aberration

- ◆ Lens have different refractive indices ([Snell's law](#)) for different wavelengths: causes color fringing



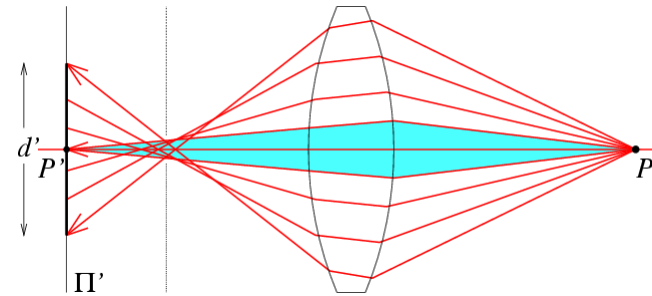
near lens center

near lens outer



Lens flaws: Spherical aberration

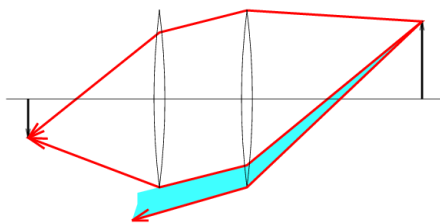
- ◆ Spherical lenses don't focus light perfectly (thin lens model)
 - ▶ Rays farther from the optical axis are focussed closer



objects lack sharpness

Lens flaws: Vignetting

- ◆ Reduction of image brightness in the periphery

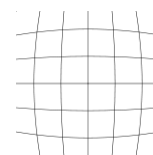


Not all rays reach the sensor

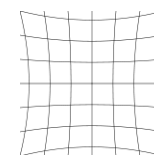


Lens flaws: Radial distortion

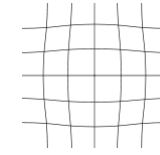
- ◆ Caused by asymmetry of lenses
- ◆ Deviations are most noticeable near the periphery



barrel distortion



pincushion distortion



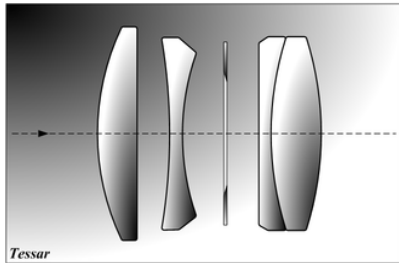
mustache distortion



Real photographic lens

- ◆ Many uses: cameras, telescopes, microscopes, etc

fixed focal length



Example of a prime lens - Carl Zeiss [Tessar](#)

adjustable zoom



[Nikkor](#) 28-200 mm zoom lens, extended to 200 mm at left and collapsed to 28 mm focal length at right.

http://en.wikipedia.org/wiki/Zoom_lens

Overview

- ◆ The pinhole projection model
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- ◆ Cameras with lenses
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- ◆ **Digital cameras**
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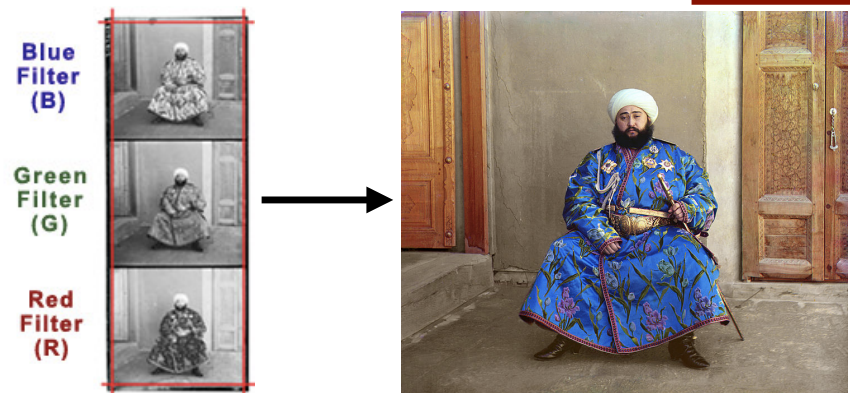
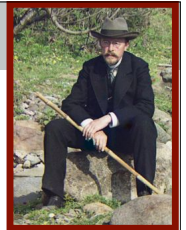
Measuring light

- ◆ Photographic film — strip of transparent plastic film base coated on one side with a gelatin emulsion containing light-sensitive materials
- ◆ Creates a latent image when exposed to light for short duration
- ◆ Films are then chemically developed to form a photograph
- ◆ Early films/photographic plates could only capture intensity



Early color photography

- ◆ Sergey Prokudin-Gorskii (1863-1944)
- ◆ Photographs of the Russian empire (1909-1916)



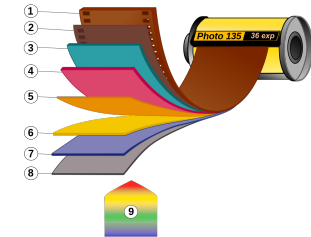
Only problem!



Homework 1: fix this by aligning the channels

Measuring light: color films

- ◆ Color photographic film — many layers of dyes and light sensitive materials to capture light of different frequencies simultaneously
 - Kodak pioneered color films for making paper prints
- ◆ Simultaneous measurement solves the alignment problem
 - But needs complex film design and development process



Digital images

- ◆ Color images are commonly represented using 3 channels [R, G, B]
 - The color of each pixel is given by the (r,g,b) value

```
>> im = imread('jelly.jpg');
>> whos im
Name      Size      Bytes Class  Attributes
im       428x570x3  731880 uint8
```

```
>> imshow(im);
>> imshow(im(:,:,1));
>> imshow(im(:,:,2));
>> imshow(im(:,:,3));
```



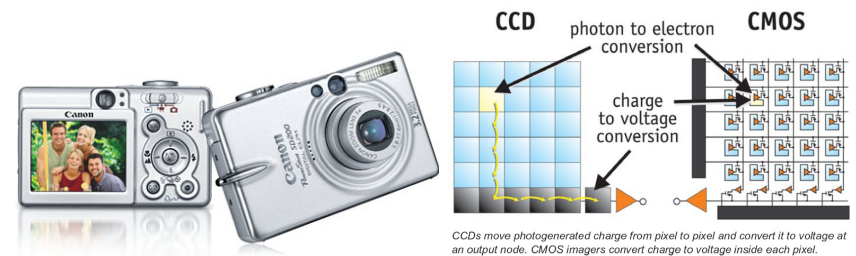
red

green

blue



Digital camera

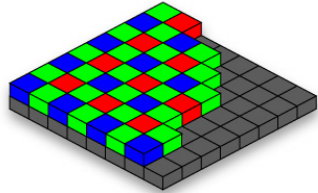


- ◆ A digital camera replaces the film with a sensor array
 - Each cell in the array is a light-sensitive diode that converts photons to electrons
 - Two common types of sensor arrays
 - Charge Coupled Device (CCD)
 - Complementary Metal Oxide Semiconductor (CMOS)

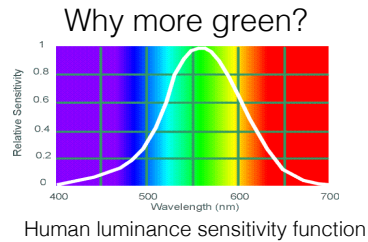
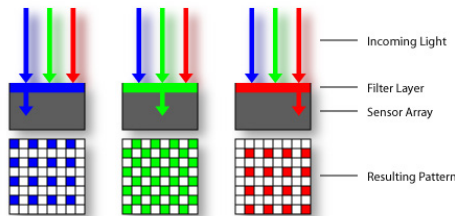
<http://electronics.howstuffworks.com/digital-camera.htm>

Color sensing in the camera

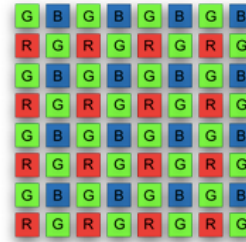
Color filter array
Bayer grid



Estimate missing components from neighboring values
(demosaicing)



Demosaicing

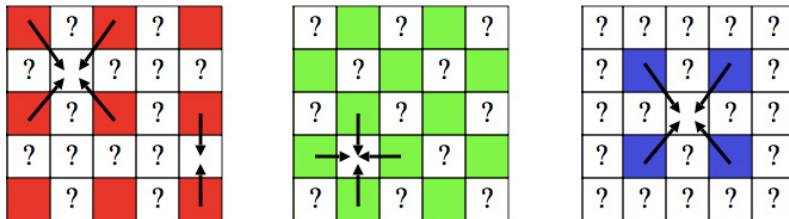


Red

Green

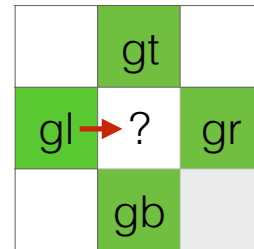
Blue

Demosaicing

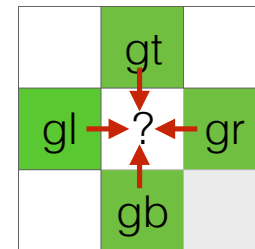


- ◆ **Problem:** guess the values of ? in each of the three channels
- ◆ Why is this even possible?

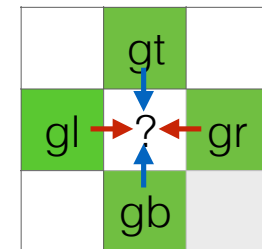
Interpolation



nearest neighbor
copy one of your neighbors
 $? \leftarrow gl$



linear interpolation
average values of your neighbors
 $? \leftarrow (gt+gl+gr+gb)/4$



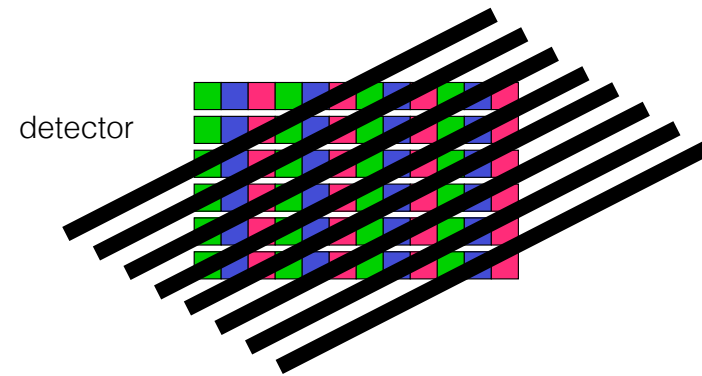
adaptive gradient
average based on nbhd. structure
if $|gt-gb| > |gl-gr|$
 $? \leftarrow (gl+gr)/2$
else
 $? \leftarrow (gt+gb)/2$

Similarly for the blue and red channels
Homework 1: implement this

Problem with demosaicing: color moiré

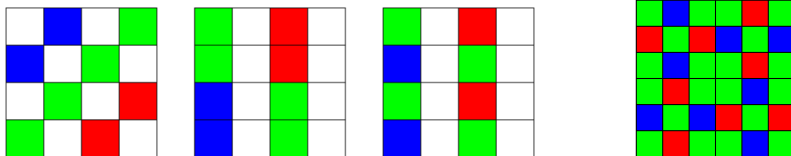


The cause of color moiré



Fine black and white detail in the image scene is misinterpreted as color information

Alternatives to Bayer filter



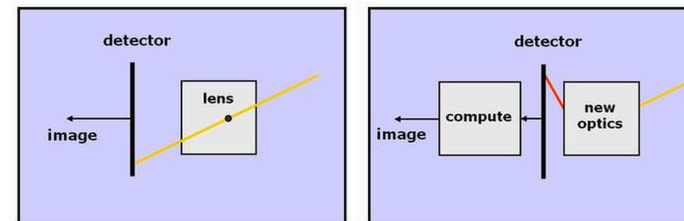
Three new Kodak RGBW filter patterns

Fujifilm "X-Trans" filter

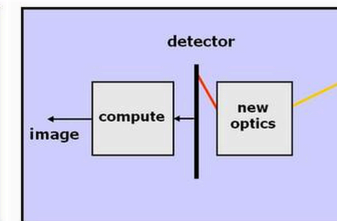
- ◆ White or "panchromatic" cells allow lights across all wavelengths
 - Better light efficiency
- ◆ How would you go about picking the best one?

Source: https://en.wikipedia.org/wiki/Bayer_filter

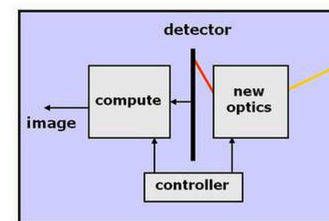
Computational cameras



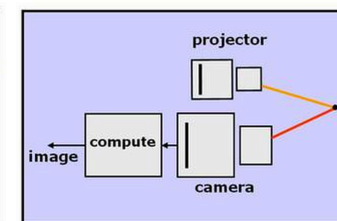
(a) Traditional Camera



(b) Computational Camera



(c) Programmable Imaging



(d) Programmable Flash

S.K. Nayar http://www1.cs.columbia.edu/CAVE/projects/what_is/

Computational color photography

- ◆ Goal: Design a **sampling pattern** + **interpolation algorithm** that archives the **best color reconstruction**
- ◆ Sampling patterns
 - ▶ Given a $n \times n$ filter array we have $4^{(n \times n)}$ possible choices
 - More choices if we allow different color filters
 - ▶ Some patterns are obviously bad for reconstruction
- ◆ Interpolation algorithms
 - ▶ Can't easily enumerate this space
 - ▶ Non trivial algorithms for interpolation

Rethinking Color Cameras

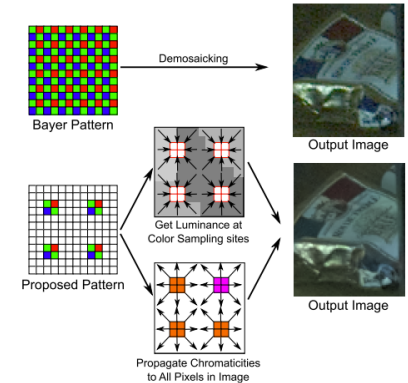
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Abstract

Digital color cameras make sub-sampled measurements of color at alternating pixel locations, and then “demosaic” these measurements to create full color images by up-sampling. This allows traditional cameras with restricted processing hardware to produce color images from a single shot, but it requires blocking a majority of the incident light and is prone to aliasing artifacts. In this paper, we introduce a computational approach to color photography, where the sampling pattern and reconstruction process are co-designed to enhance sharpness and photographic speed. The pattern is made predominantly panchromatic, thus avoiding excessive loss of light and aliasing of high spatial-frequency intensity variations. Color is sampled at a very sparse set of locations and then propagated throughout the image with guidance from the un-aliased luminance channel. Experimental results show that this approach often leads to significant reductions in noise and aliasing arti-



linearly interpolate color value using intensity-based affinities

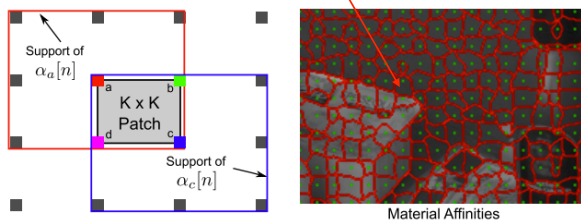
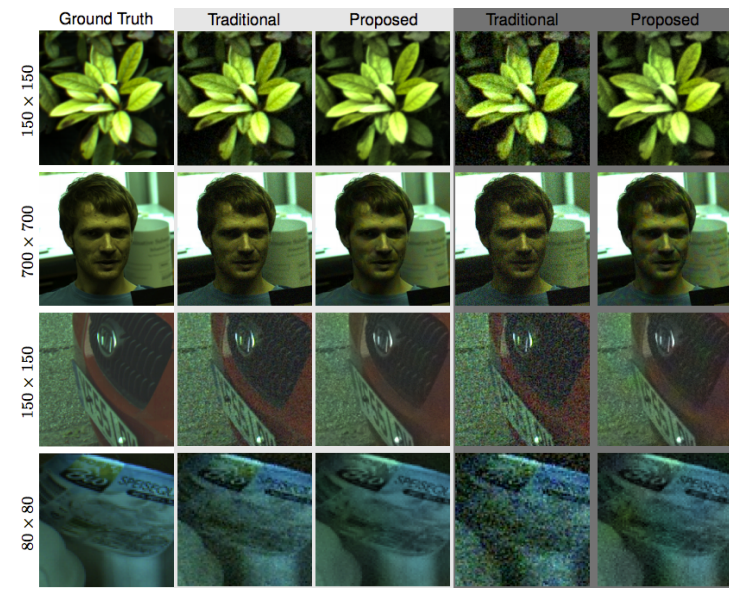


Figure 2. Propagating chromaticity with material affinities. *Left:* Chromaticities at pixels within each $K \times K$ patch are computed as convex combinations of chromaticities measured by the Bayer blocks at its corners. The combination weights are determined by four affinity maps $\alpha_j[n]$, one from each corner Bayer block j , that encode luminance edge information. *Right:* Affinity map showing regions of pixels with highest affinity to each block (marked in green), super-imposed on the corresponding luminance image.

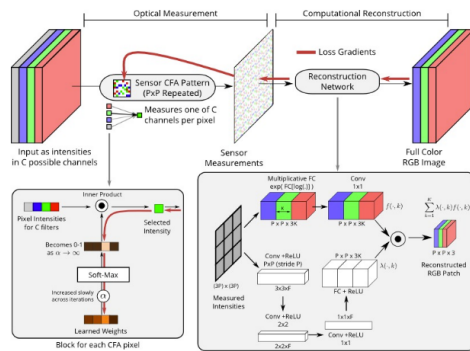
increasing noise level →



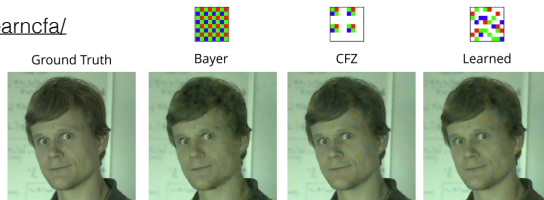
Learning Sensor Multiplexing Design through Back-propagation

Ayan Chakrabarti

To appear at NIPS'16



http://ttic.uchicago.edu/~ayanc/learn_cfa/



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Light Stage 6

- ◆ Sample over time, lighting, viewing direction, pose



Paul Debevec's group at USC-ICT

inside Light Stage 6

<http://ict.usc.edu/prototypes/light-stages/>

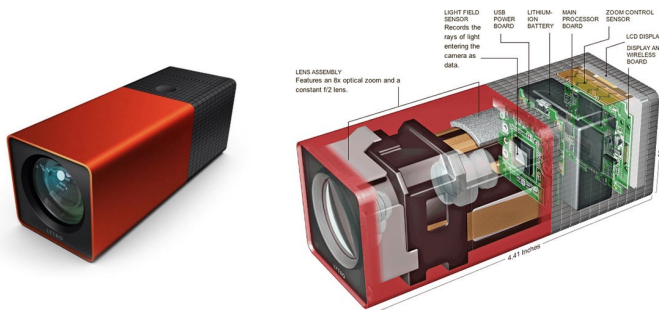
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Lytro camera

- ◆ Light field camera: capture intensity along each direction of the light
 - ▶ Traditional cameras integrate light coming from all directions
- ◆ A captured light field allows you re-render an image post-hoc
 - ▶ <https://pictures.lytro.com/lytro/collections/41/pictures/1088670>



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More readings and thoughts

- ◆ [History of optics](#), Wikipedia
- ◆ A. Torralba and W. Freeman, [Accidental Pinhole and Pinspeck Cameras](#), CVPR 2012
- ◆ DIY <http://www.pauldebevec.com/Pinhole>
- ◆ In MATLAB, compute the projection of a sphere using the perspective model and visualize the distortions
- ◆ Light stages over time <http://gl.ict.usc.edu/LightStages>
- ◆ Sergey Prokudin-Gorskii photographic collection at the Library of Congress <http://www.loc.gov/exhibits/empire/index.html>
- ◆ Richard Szeliski's book, Sections 2.2.3 - 2.3.2

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