

# Image formation

Subhransu Maji

CMPSCI 670: Computer Vision

September 13, 2016

# Administrivia and survey results

## ◆ Topics:

- deep learning, CNNs, machine learning, AI
- **Applications:** self driving cars, face detection/recognition, etc
- robotics, calibration, structure from motion
- graphics, text/natural language processing, speech,

## ◆ Goals:

- Learn fundamentals of CV/ML/image processing
- Do a supercool project
- Get an awesome industry job (e.g., space exploration @ NASA)

## ◆ Programming: 7.5 - 8.5, Math: 6.5 - 7.5

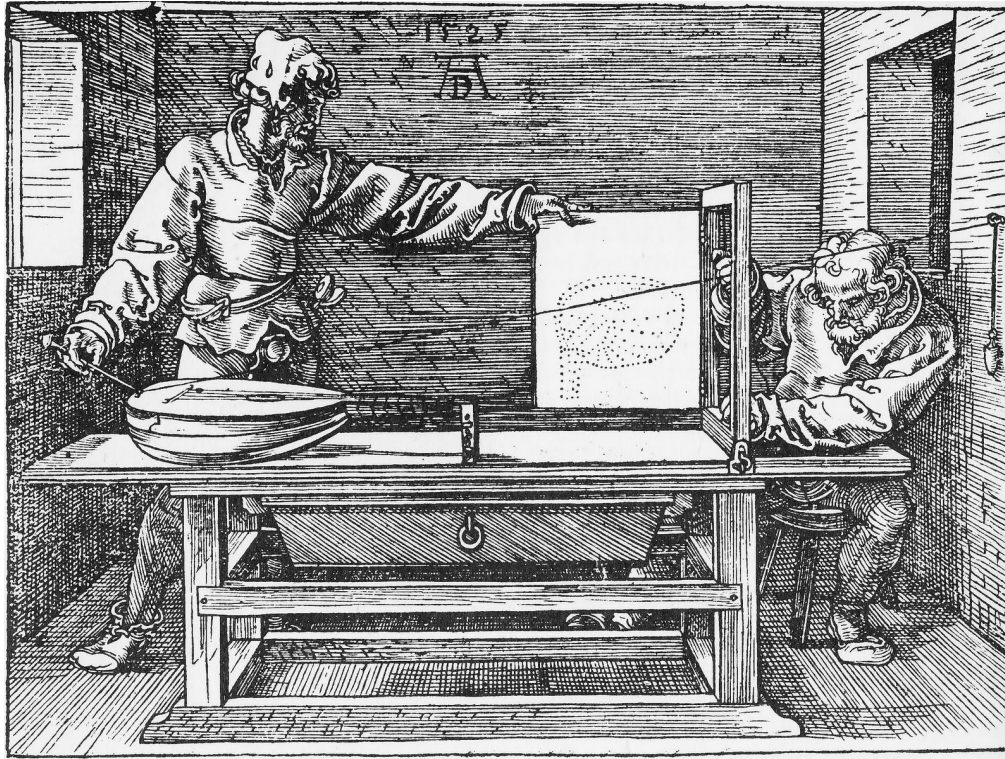
## ◆ Spire: waitlisted students? there are a few more open slots

## ◆ Resources for vector algebra and probability added to the webpage

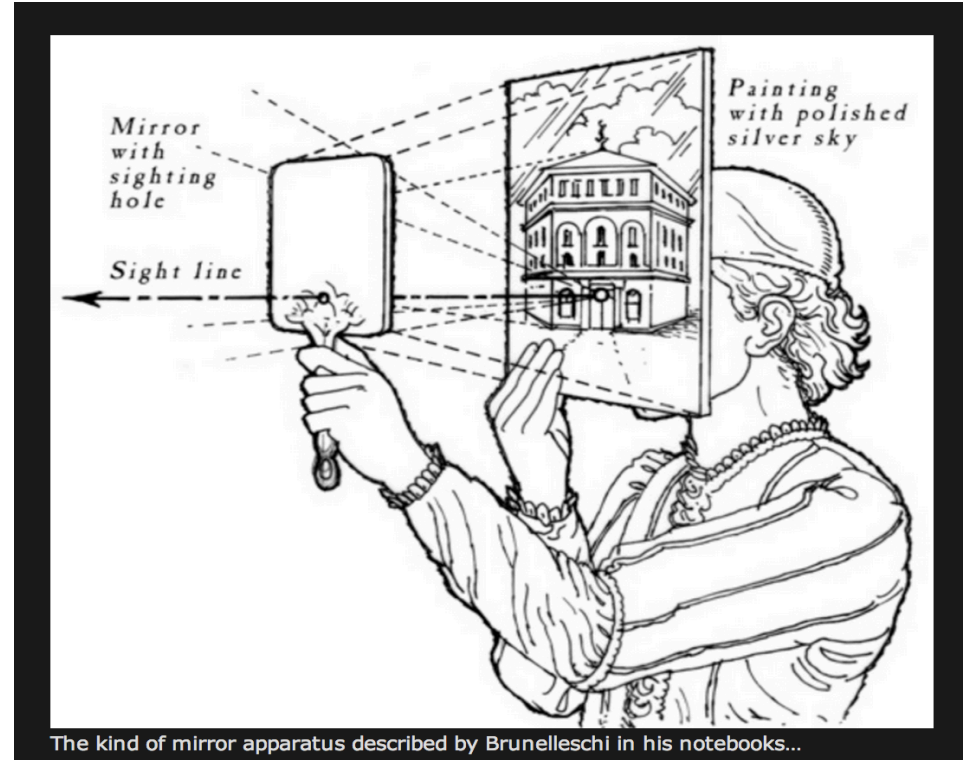
# Overview of the next two lectures

- ◆ The pinhole projection model
  - qualitative properties
- ◆ Cameras with lenses
  - Depth of focus
  - Field of view
  - Lens aberrations
- ◆ Digital cameras
  - Sensors
  - Colors
  - Artifacts
- ◆ Computational photography
  - Novel sensors and cameras

# Cameras



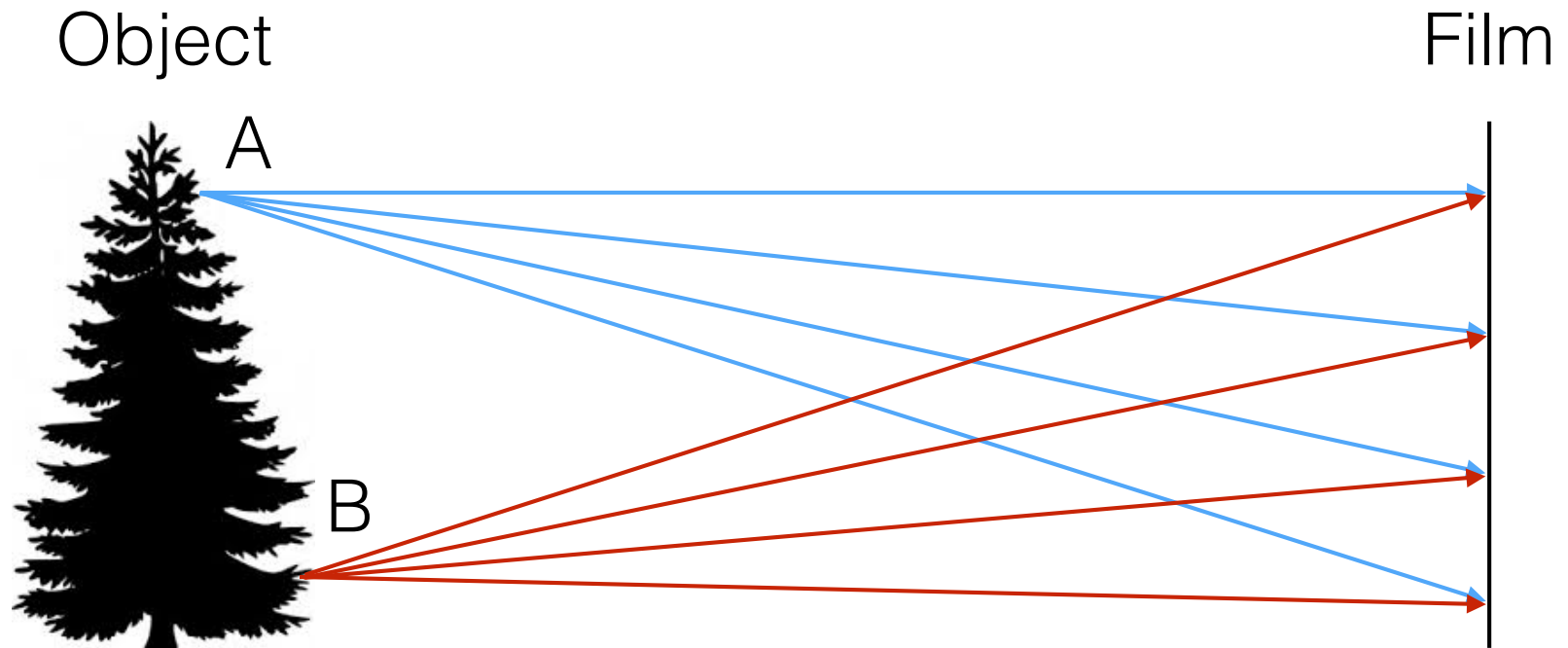
Albrecht Dürer early 1500s



Brunelleschi, early 1400s

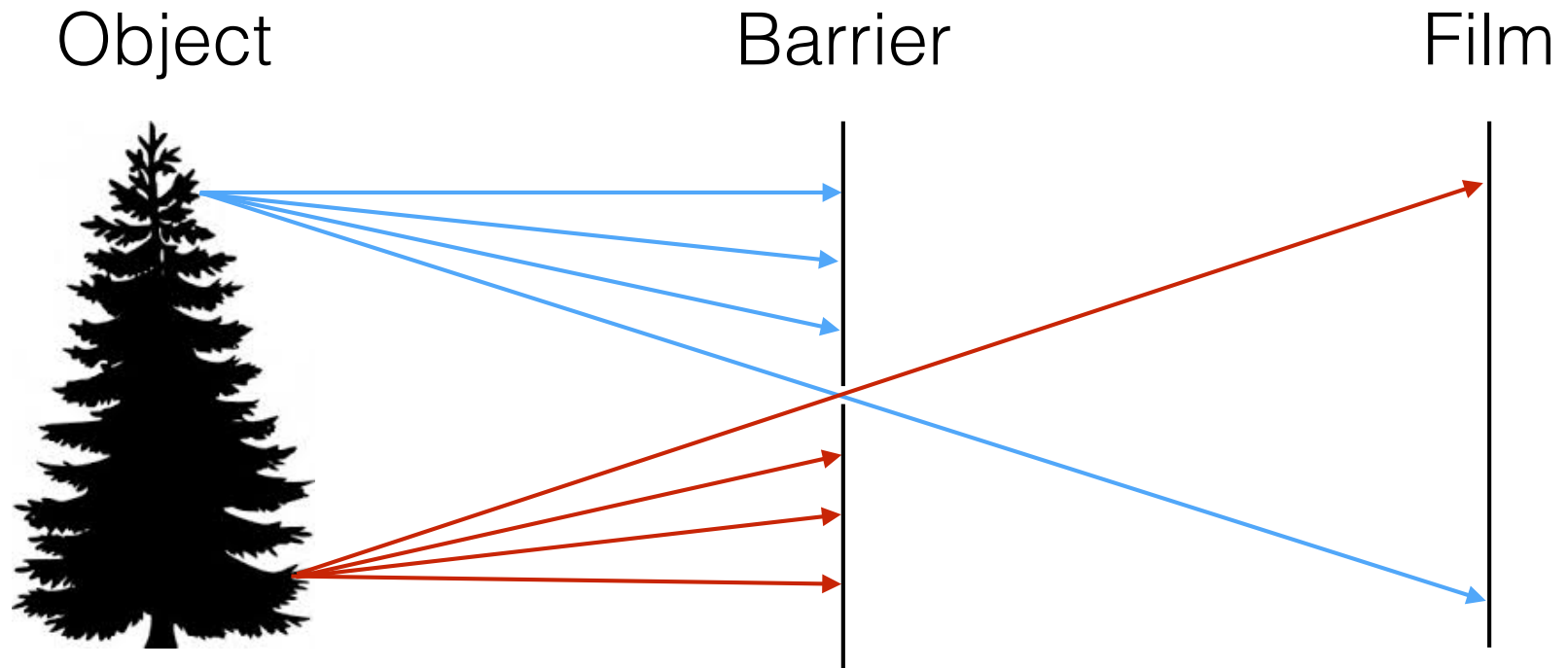


# Lets design a camera



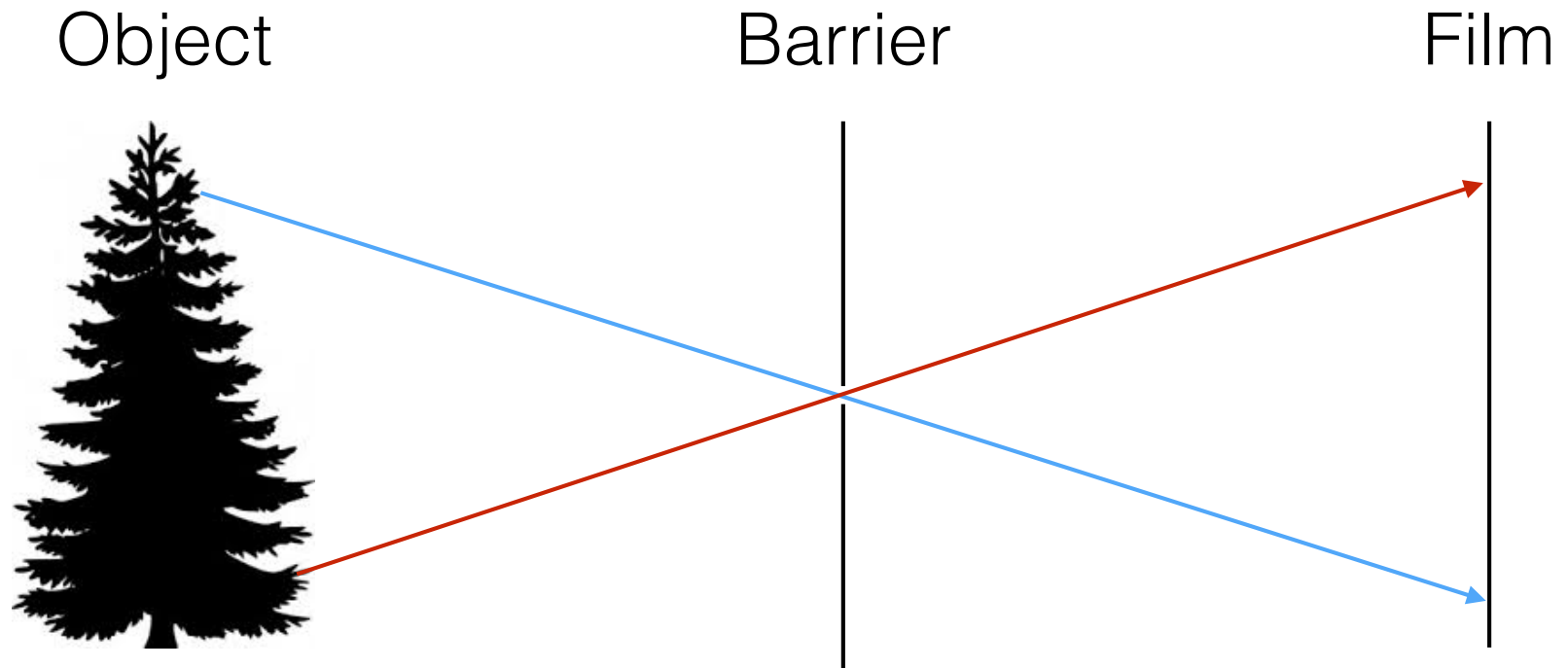
**Idea 1:** Lets put a film in front of an object  
Do we get a reasonable image?

# Pinhole camera



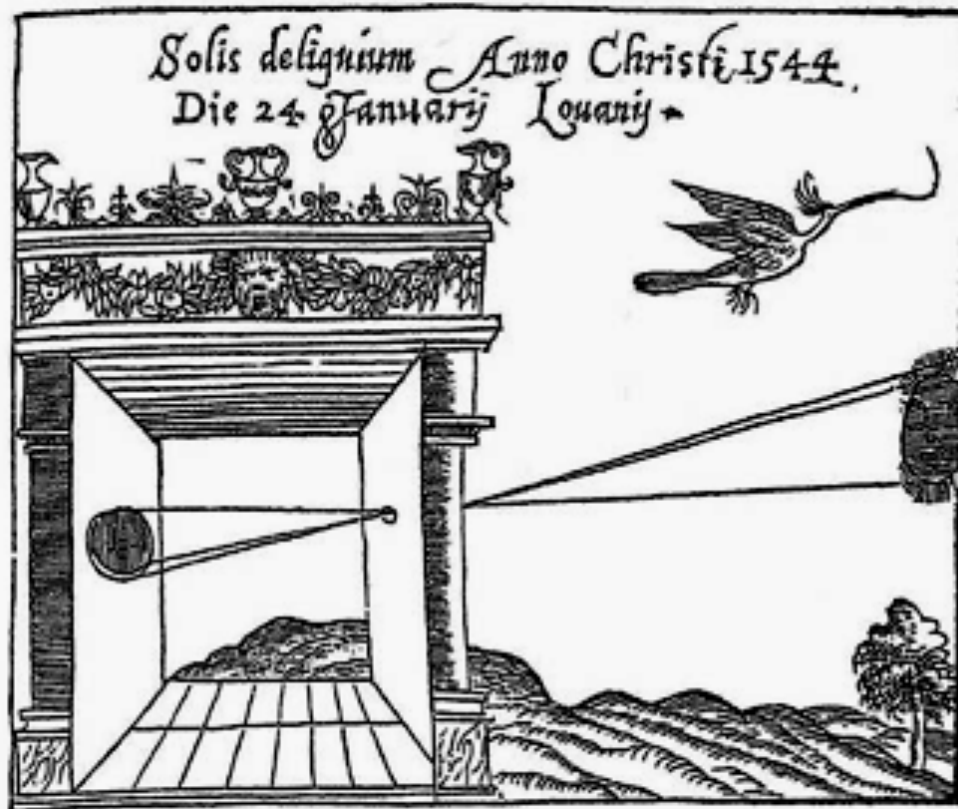
Add a barrier to block of most rays

# Pinhole camera



- Captures pencil of rays - all rays through a single point: **aperture**, **center of projection**, **focal point**, **camera center**
- The image is formed on the **image plane**

# Camera obscura



Gemma Frisius, 1558

- ◆ Basic principle known to Mozi (470-390 BCE), Aristotle (384-322 BCE)
- ◆ Drawing aids for artists: described by Leonardo Da Vinci (1452-1519 AD)

“Camera obscura” Latin for “darkened room”

# Pinhole cameras are everywhere



**Tree shadow during a solar eclipse**

photo credit: Nils van der Burg

<http://www.physicstogo.org/index.cfm>



# Accidental pinhole cameras

My hotel room,  
contrast enhanced.



The view from my window



Accidental pinholes produce images that are  
unnoticed or misinterpreted as shadows

A. Torralba and W. Freeman, [Accidental Pinhole and Pinspeck Cameras](#), CVPR 2012

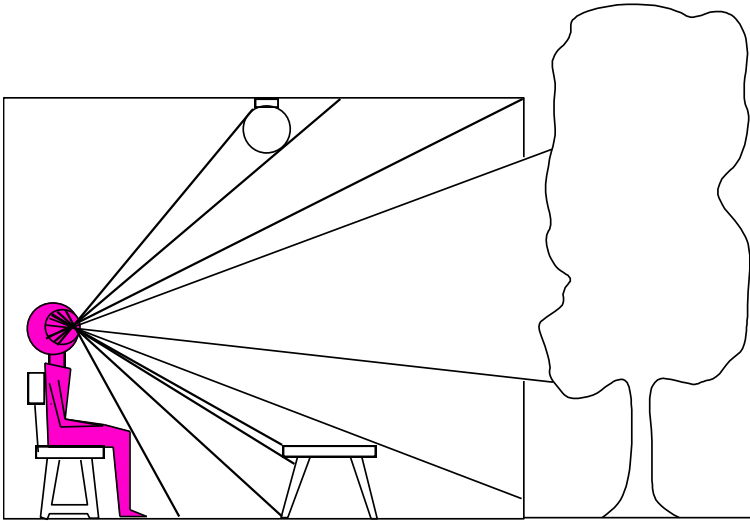
# Home-made pinhole camera



<http://www.pauldebevec.com/Pinhole>

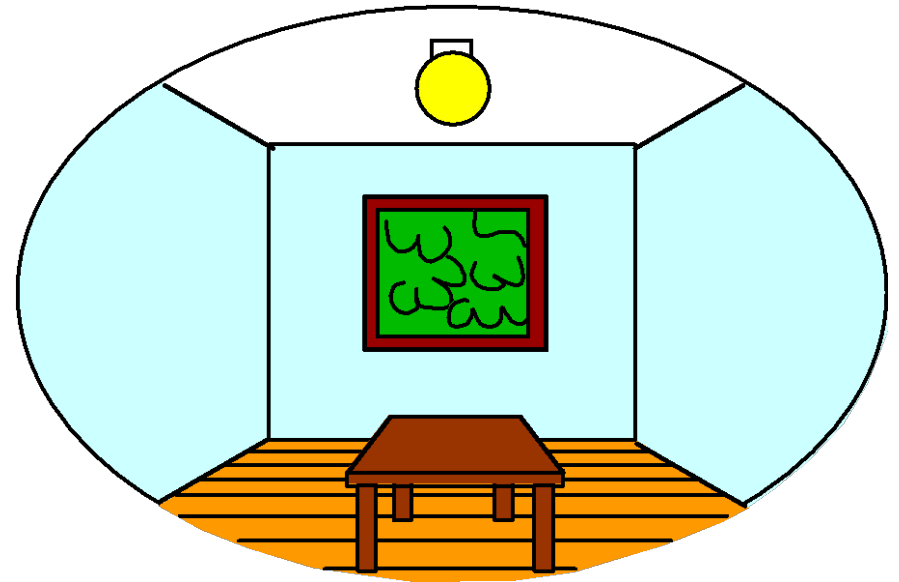
# Dimensionality reduction: 3D to 2D

3D world



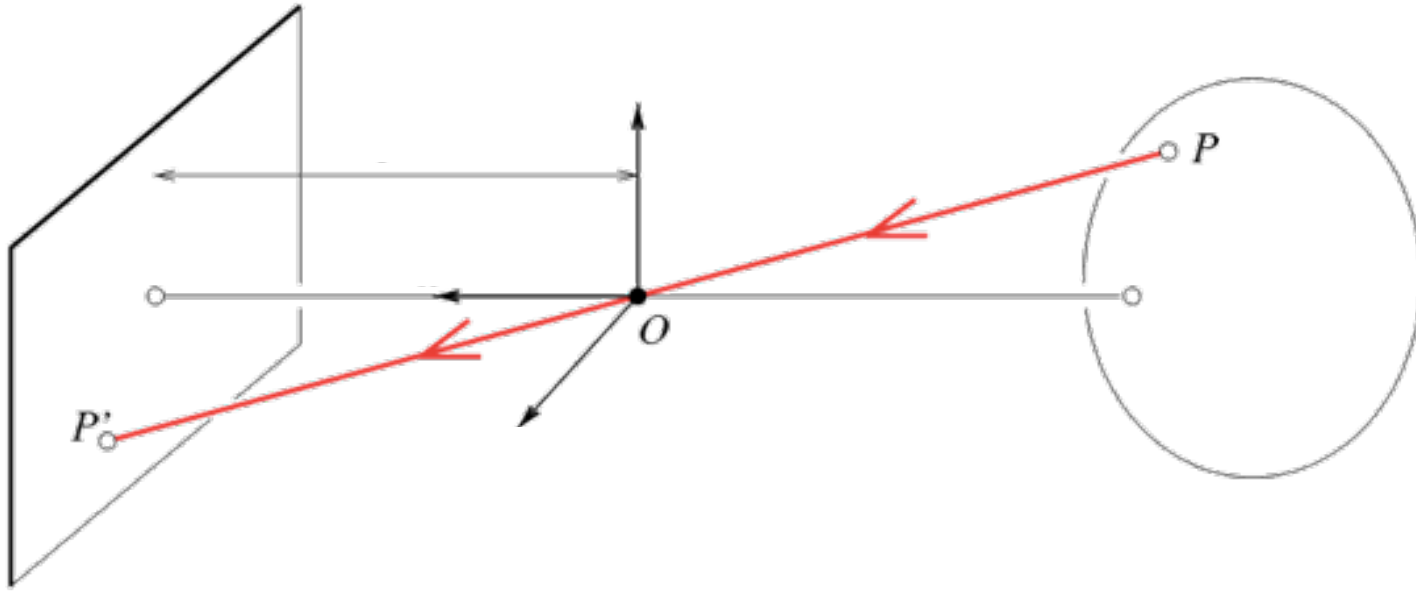
Point of observation

2D image



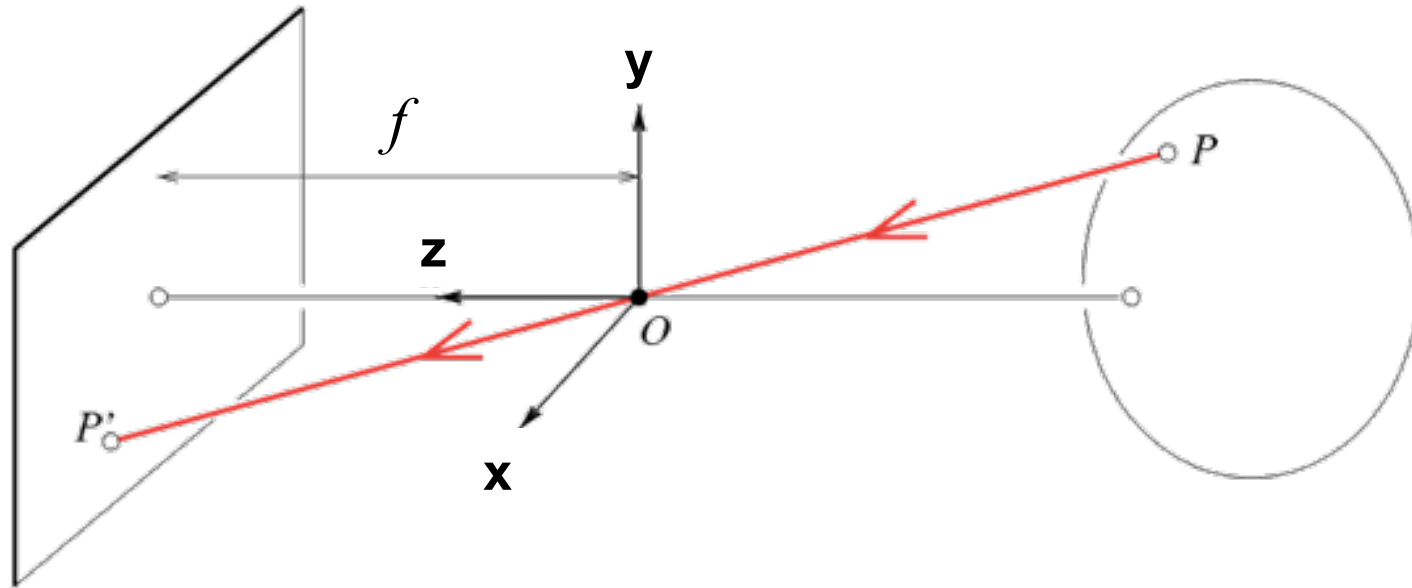
- **What is preserved?**
  - Straight lines, incidence
- **What is not preserved?**
  - Angles, lengths

# Modeling projection



- ◆ To compute the projection  $P'$  of a scene point  $P$ , form a **visual ray** connection  $P$  to the camera center  $O$  and find where it intersects the image plane
  - ▶ All scene points that lie on this visual ray have the same projection on the image
  - ▶ Are there points for which this projection is not defined?

# Modeling projection



## ◆ The coordinate system

- ▶ The optical center ( $\mathbf{O}$ ) is at the origin
- ▶ The image plane is parallel to the  $xy$ -plane (perpendicular to the  $z$  axis)

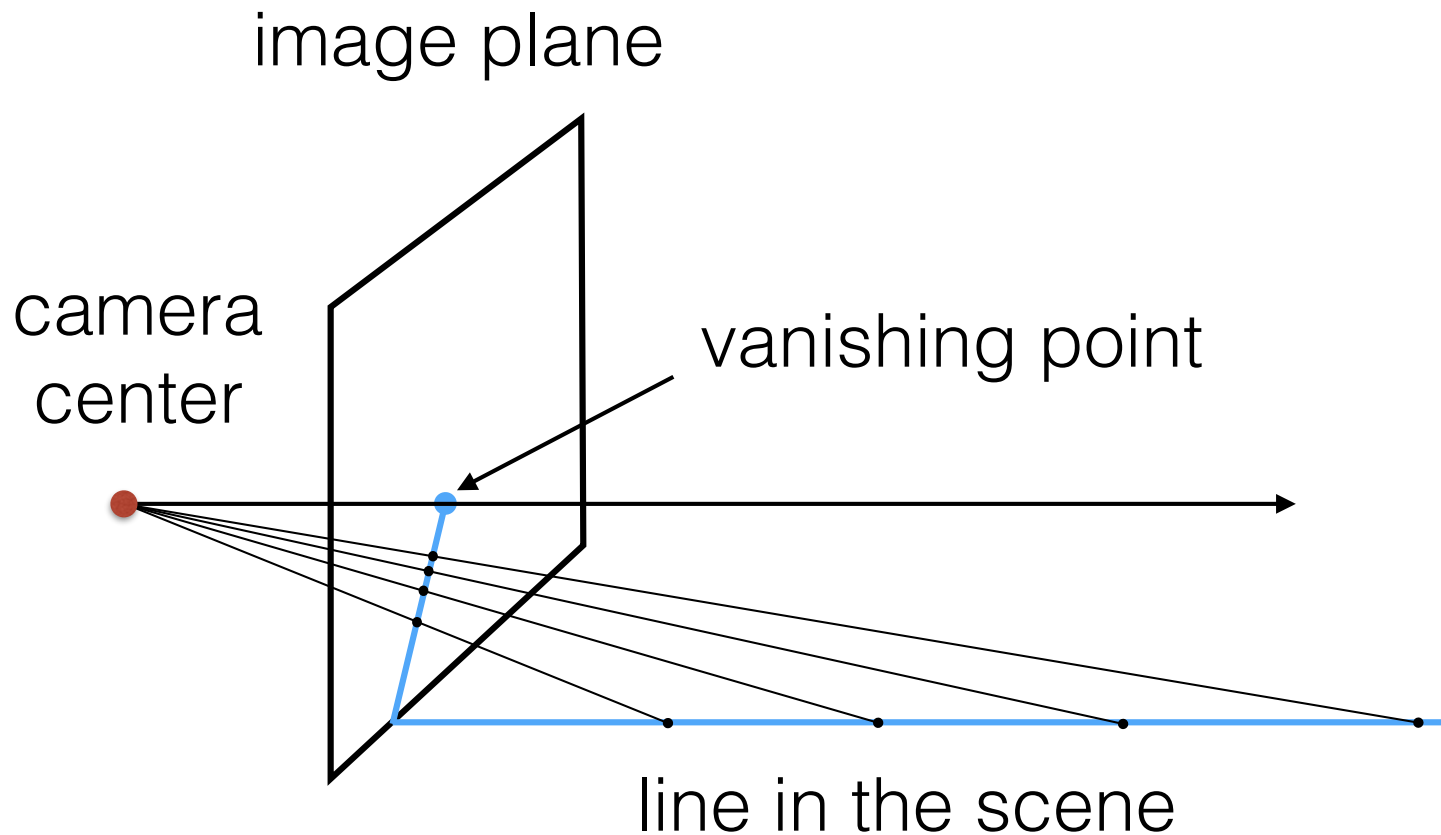
## ◆ Projection equations

- ▶ Derive using similar triangles

$$(x, y, z) \rightarrow \left(f \frac{x}{z}, f \frac{y}{z}\right)$$



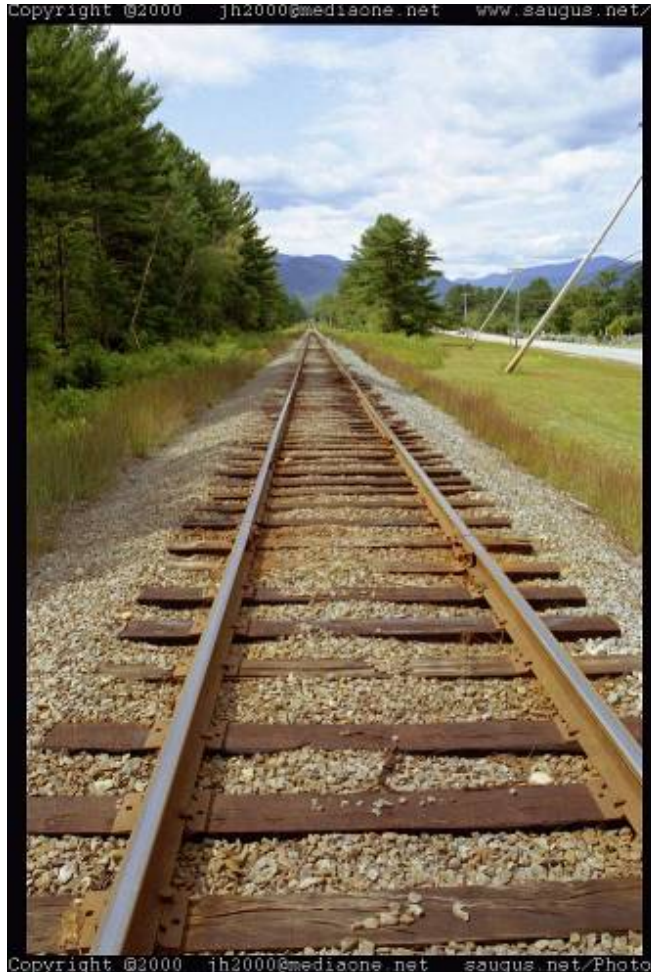
# Projection of a line



- What if we add another line parallel to the first one?

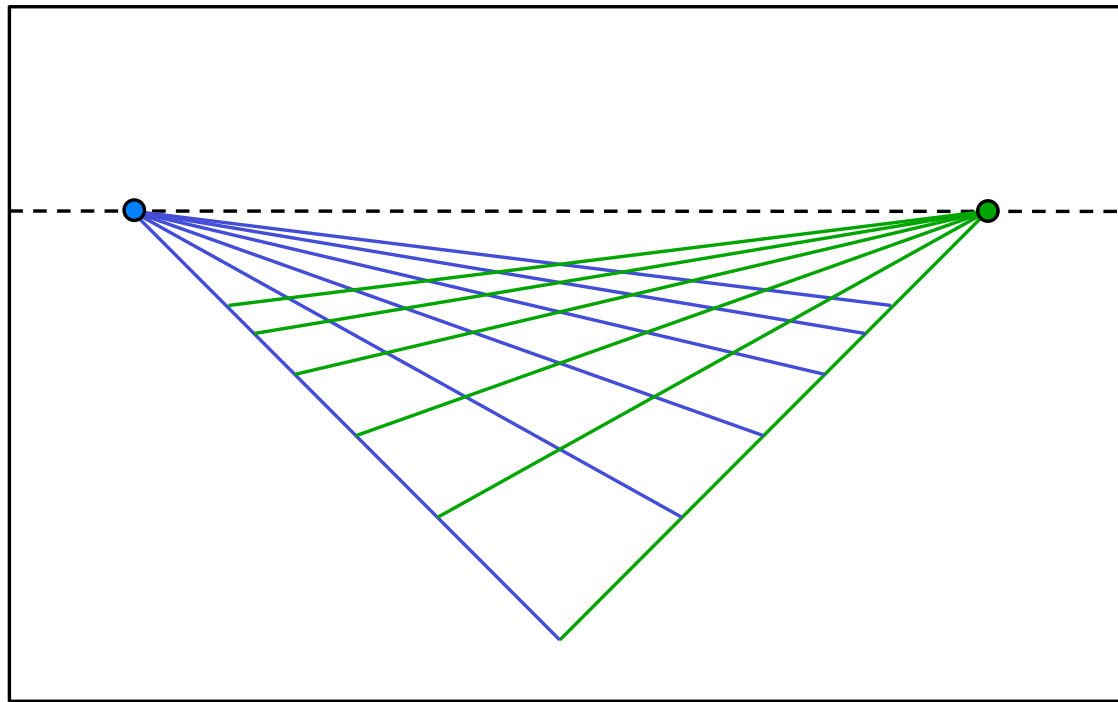
# Vanishing points

- ◆ Each direction in space has its own vanishing point
  - ▶ All lines going in the that direction converge at that point
- **Exception:** directions that are parallel to the image plane

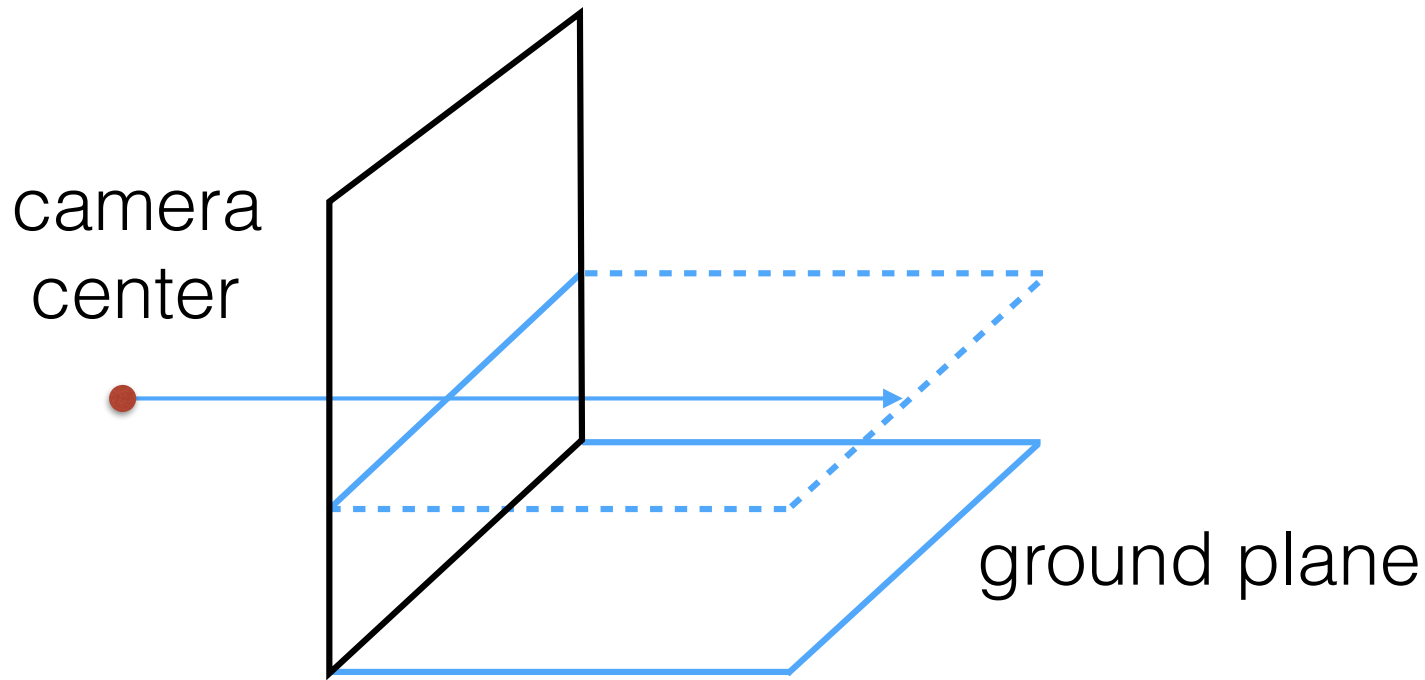


# Vanishing points

- ◆ Each direction in space has its own vanishing point
  - ▶ All lines going in the that direction converge at that point
- **Exception:** directions that are parallel to the image plane
- What about the vanishing point of a plane?



# The horizon



## ◆ Vanishing line of the ground plane

- ▶ All points at the same height of the camera project to the horizon
- ▶ Points above the camera project above the horizon
- ▶ Provides a way of comparing heights of objects

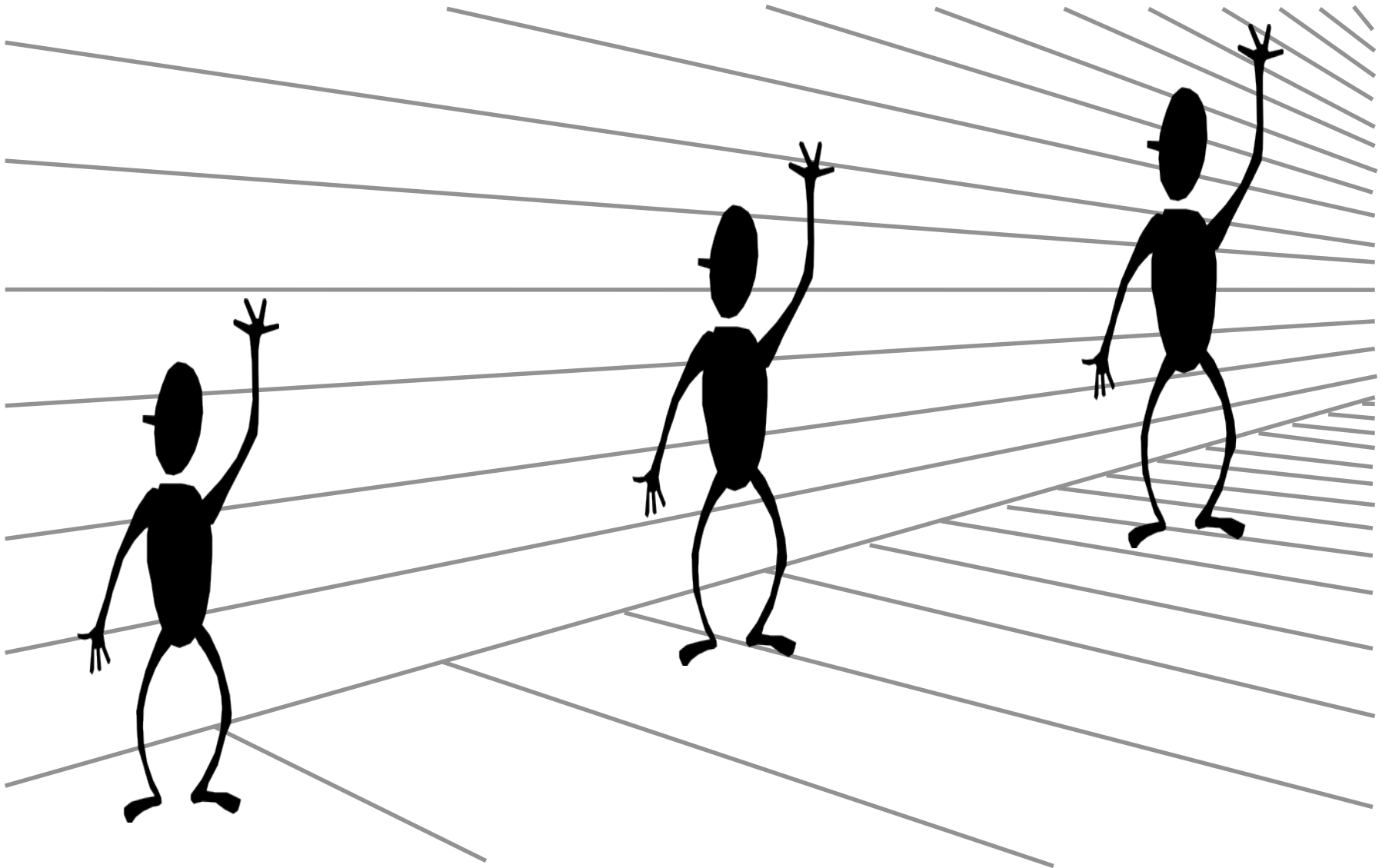
# The horizon



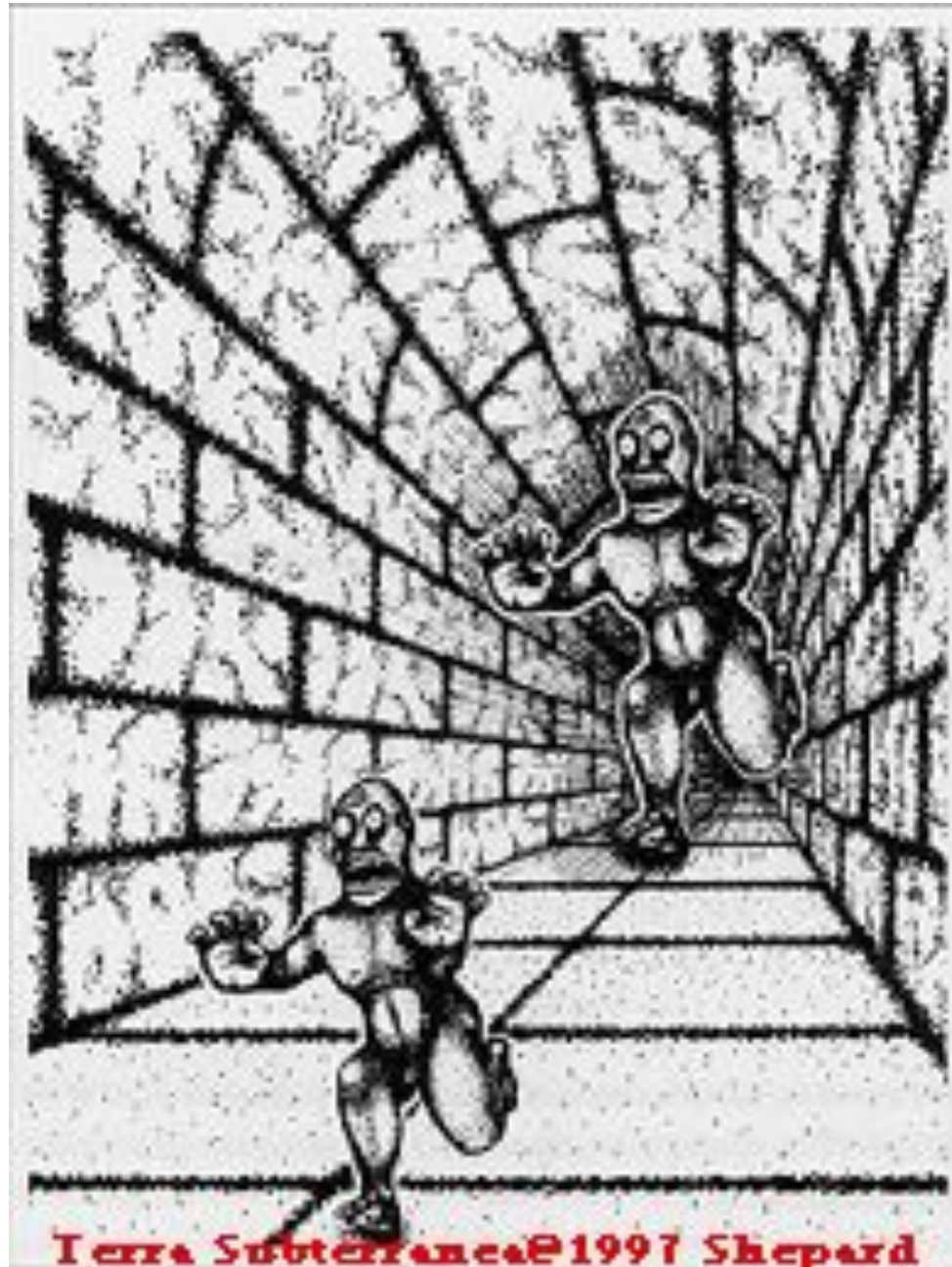
Is the person above or below the viewer?



# Perspective cues

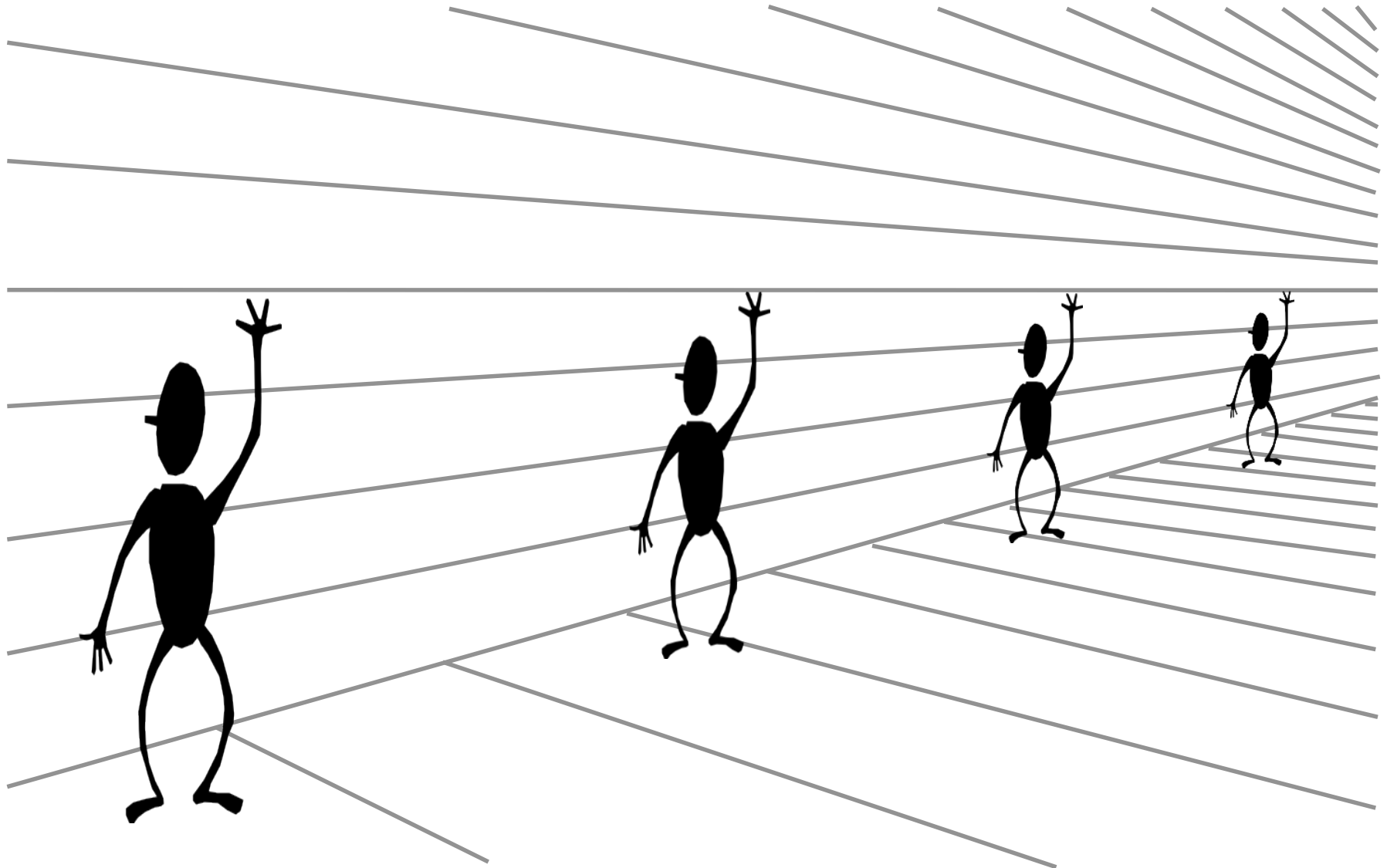


# Perspective cues

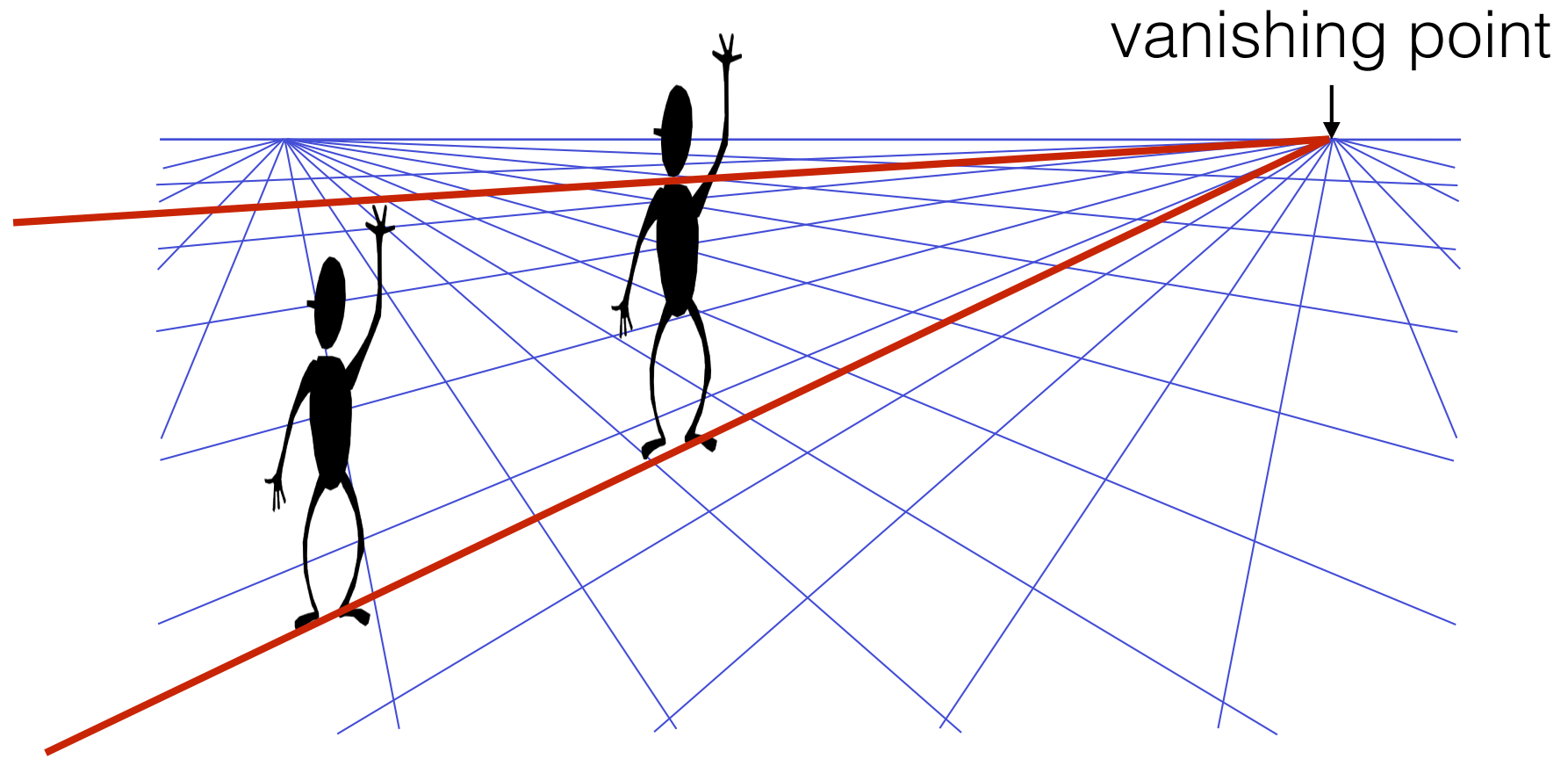


Terra Subterranea ©1997 Shepard

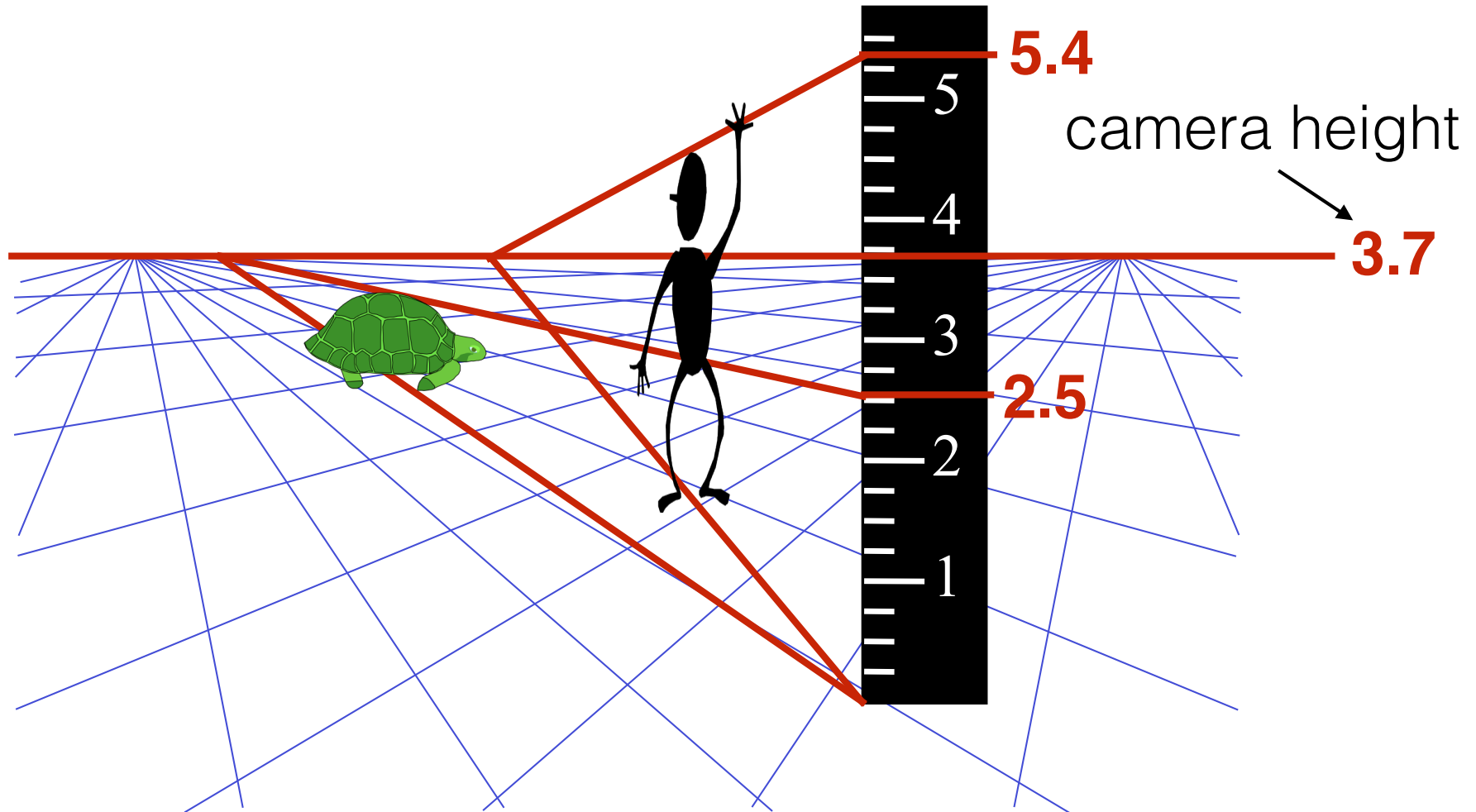
# Perspective cues



# Comparing heights



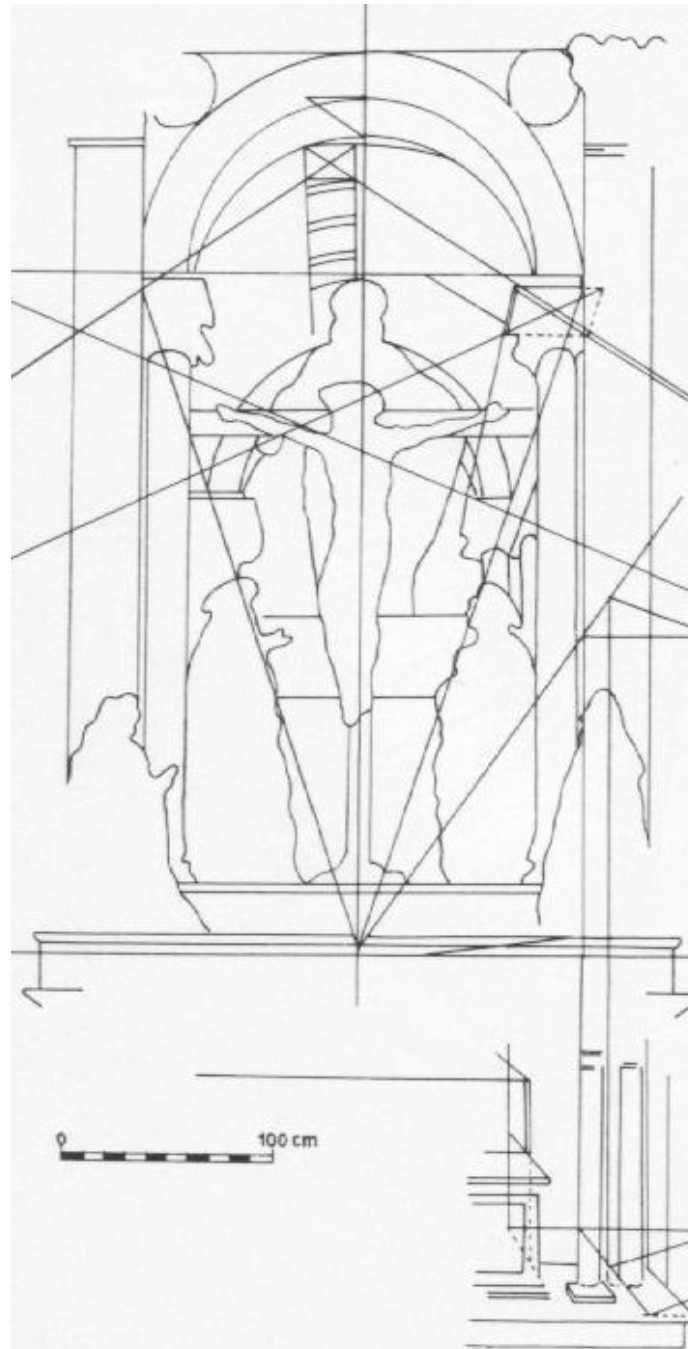
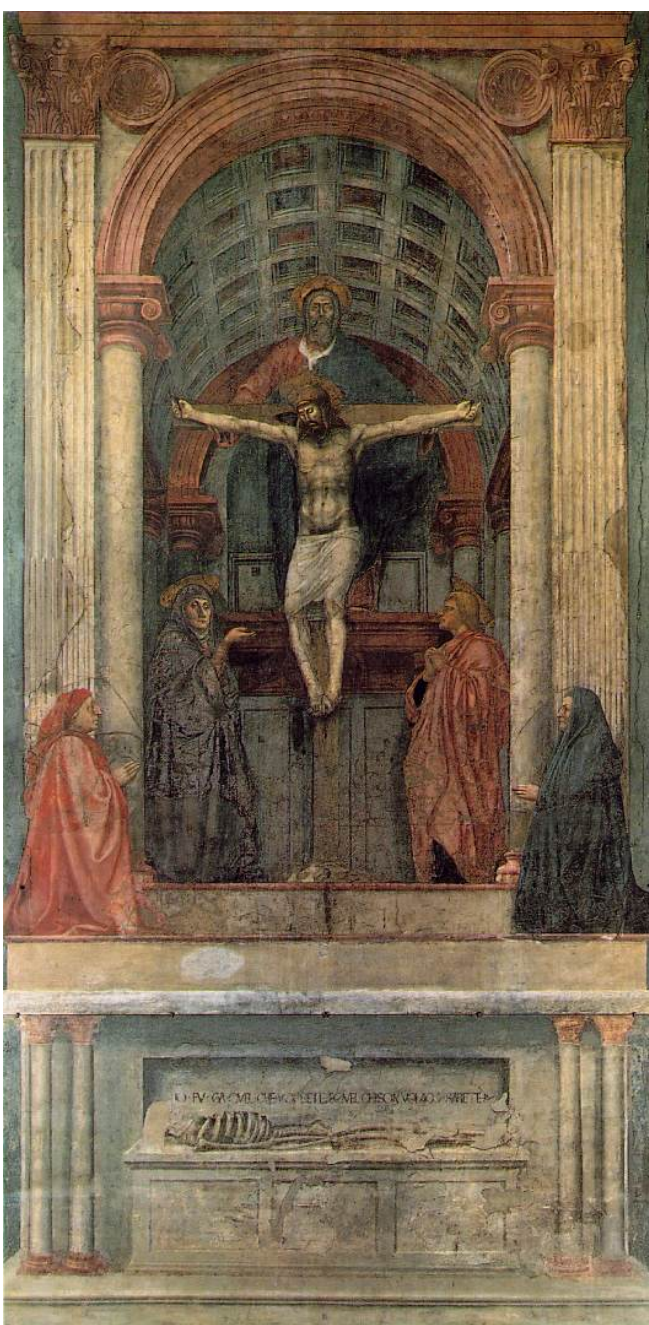
# Measuring heights



What is the height of the camera?



# Perspective in art



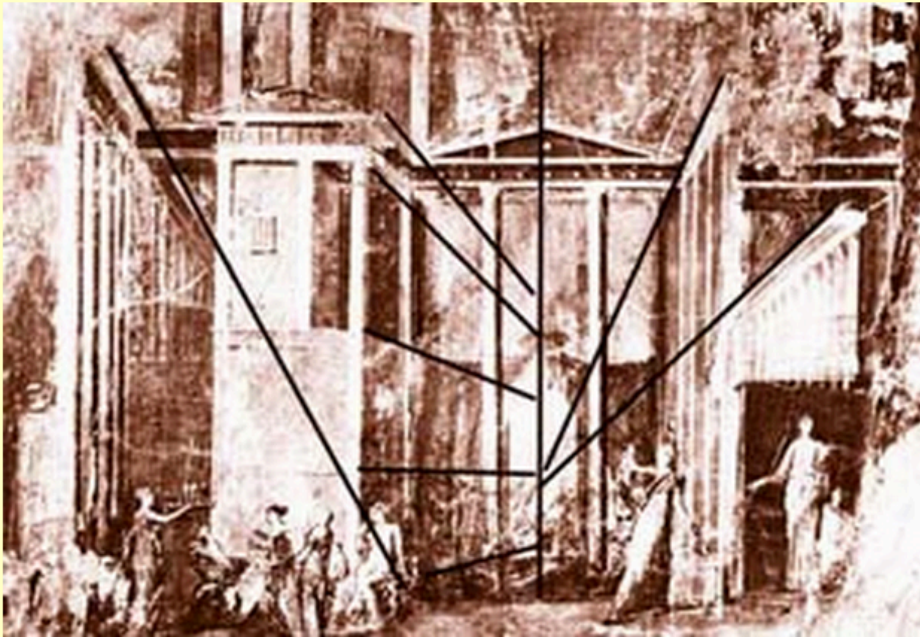
Masaccio,  
*Trinity*, Santa  
Maria Novella,  
Florence,  
1425-28

One of the first  
consistent  
uses of  
perspective in  
Western art

# Perspective in art

(At least partial) Perspective projections in art well before the Renaissance

Several Pompeii wallpaintings show the fragmentary use of linear perspective:

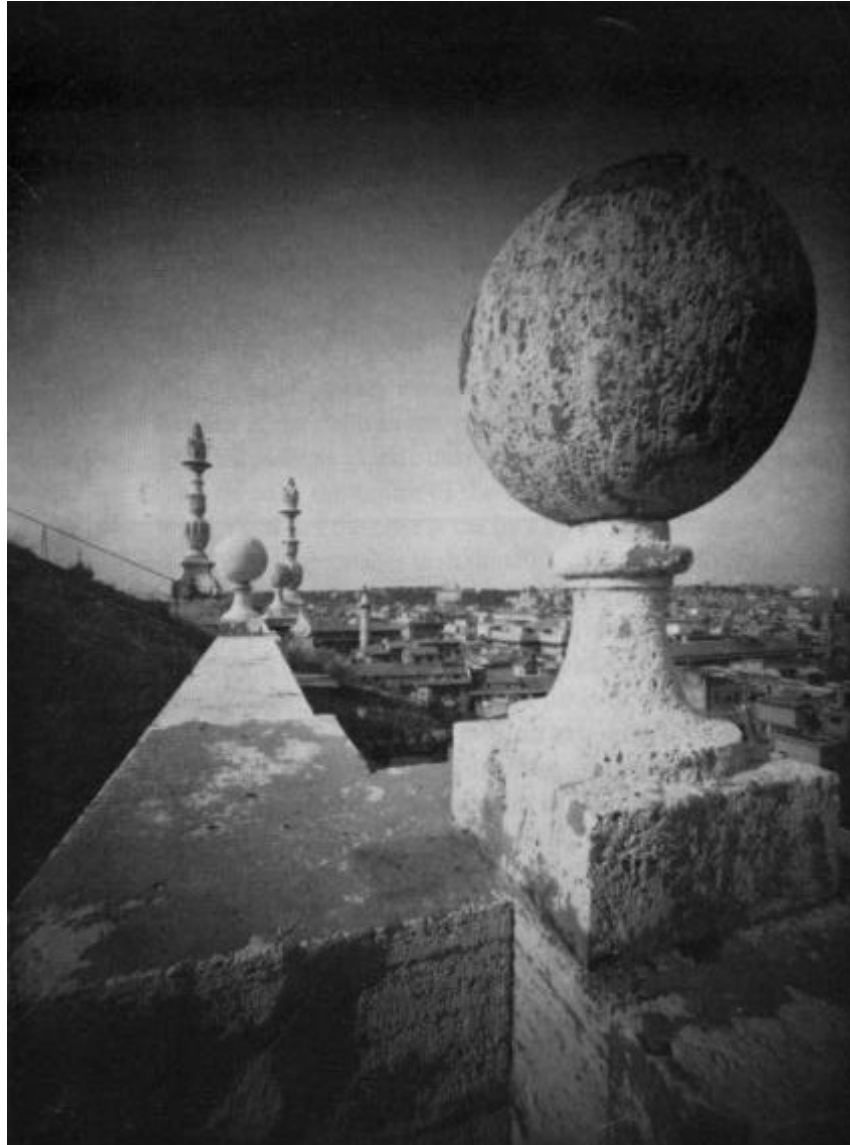


From [ottobwiersma.nl](http://ottobwiersma.nl)

Also some Greek examples,  
So apparently pre-renaissance...

# Perspective distortion

- ◆ What does a sphere project to?



M. H. Pirenne

Subhransu Maji (UMass, Fall 16)

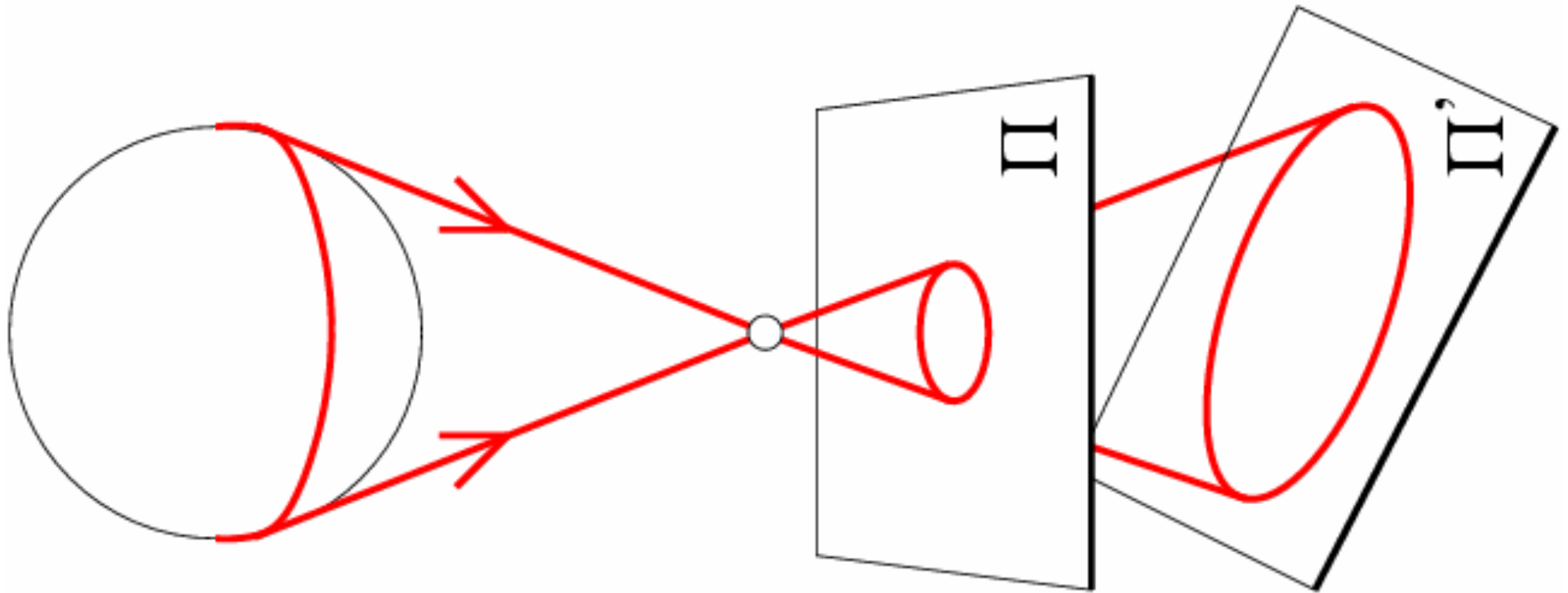
Slide by Steve Seitz

27



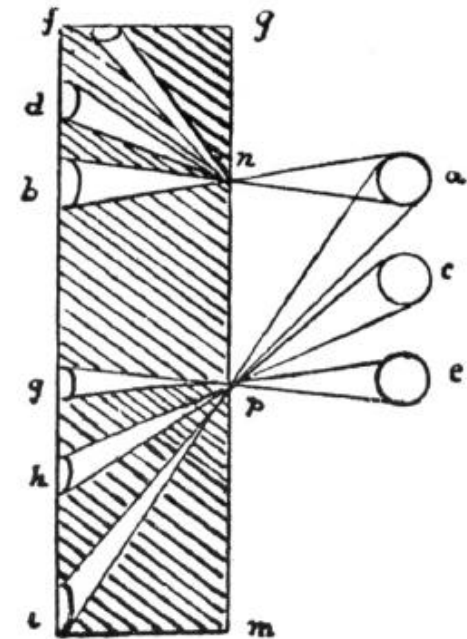
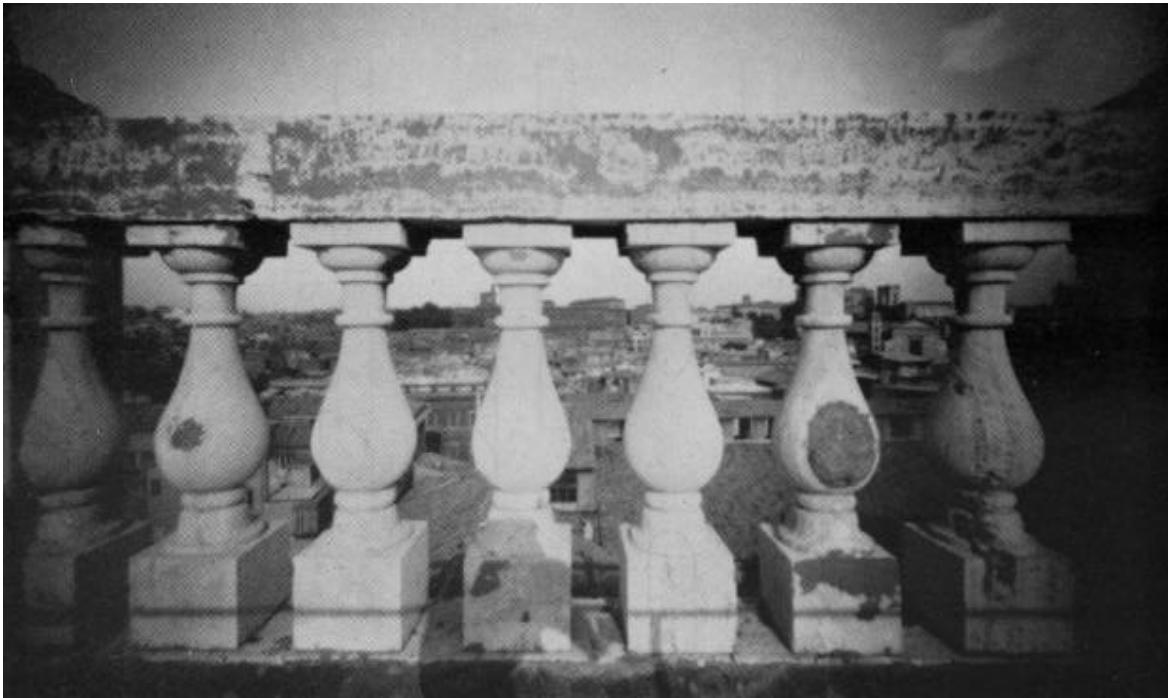
# Perspective distortion

- ◆ What does a sphere project to?



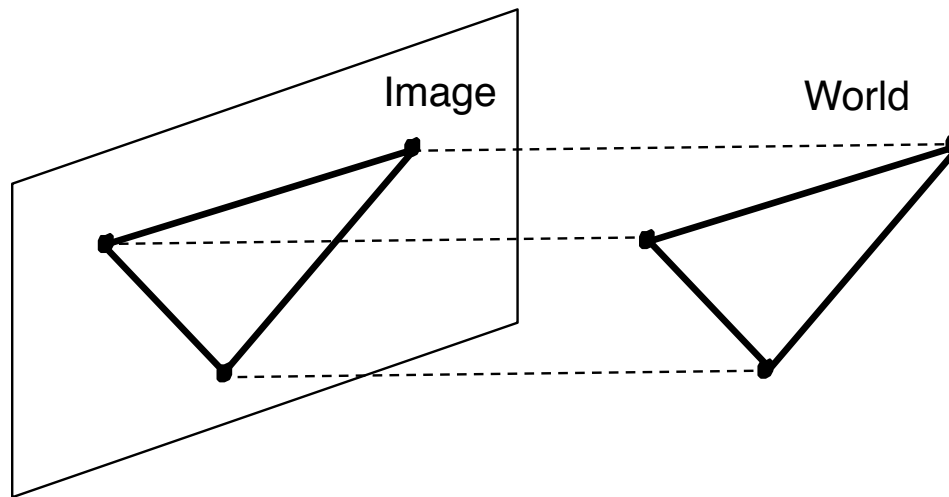
# Perspective distortion

- ◆ The exterior looks bigger
- ◆ The distortion is not due to lens flaws
- ◆ Problem pointed out by Da Vinci



# Orthographic projection

- ◆ Special case of perspective projection
  - ▶ Distance of the object from the image plane is infinite
  - ▶ Also called the “parallel projection”





# Orthographic projection

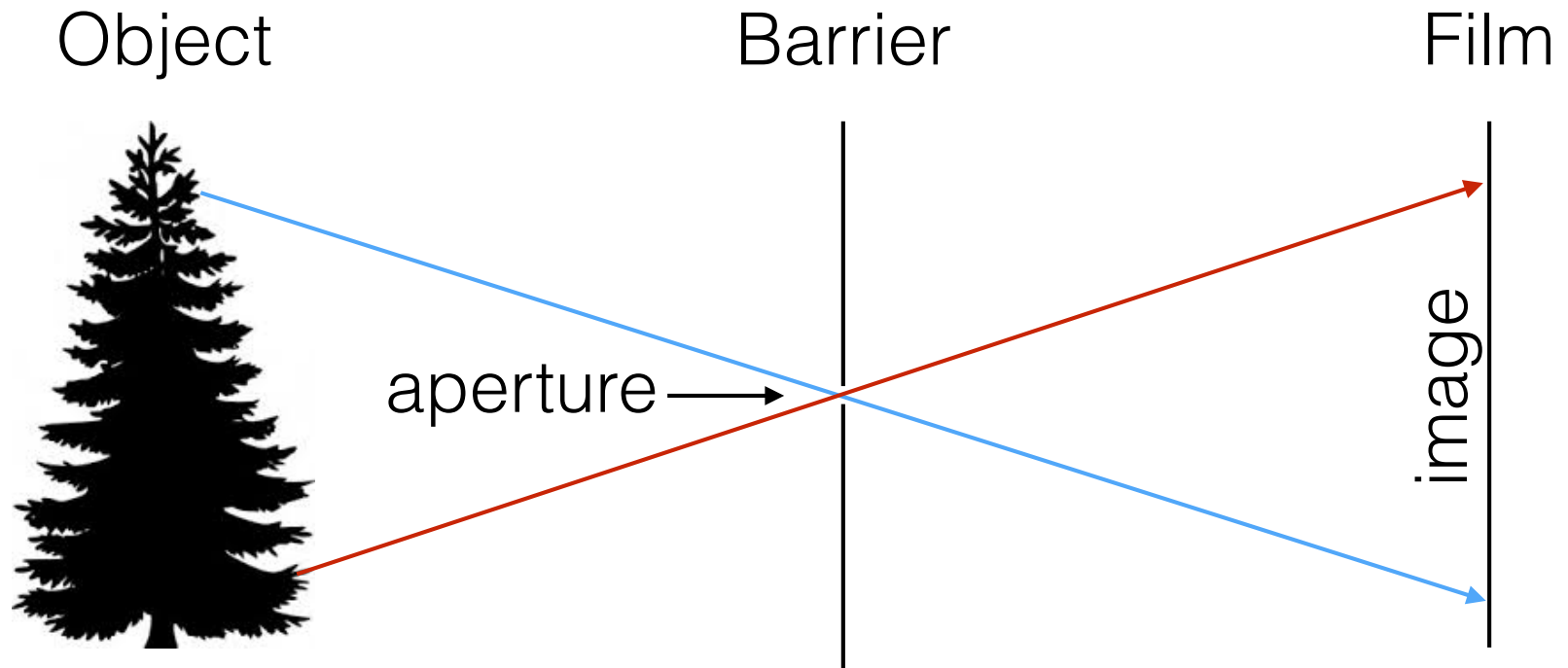
- ◆ Special case of perspective projection
  - ▶ Distance of the object from the image plane is infinite
  - ▶ Also called the “parallel projection”



# Overview of the next two lectures

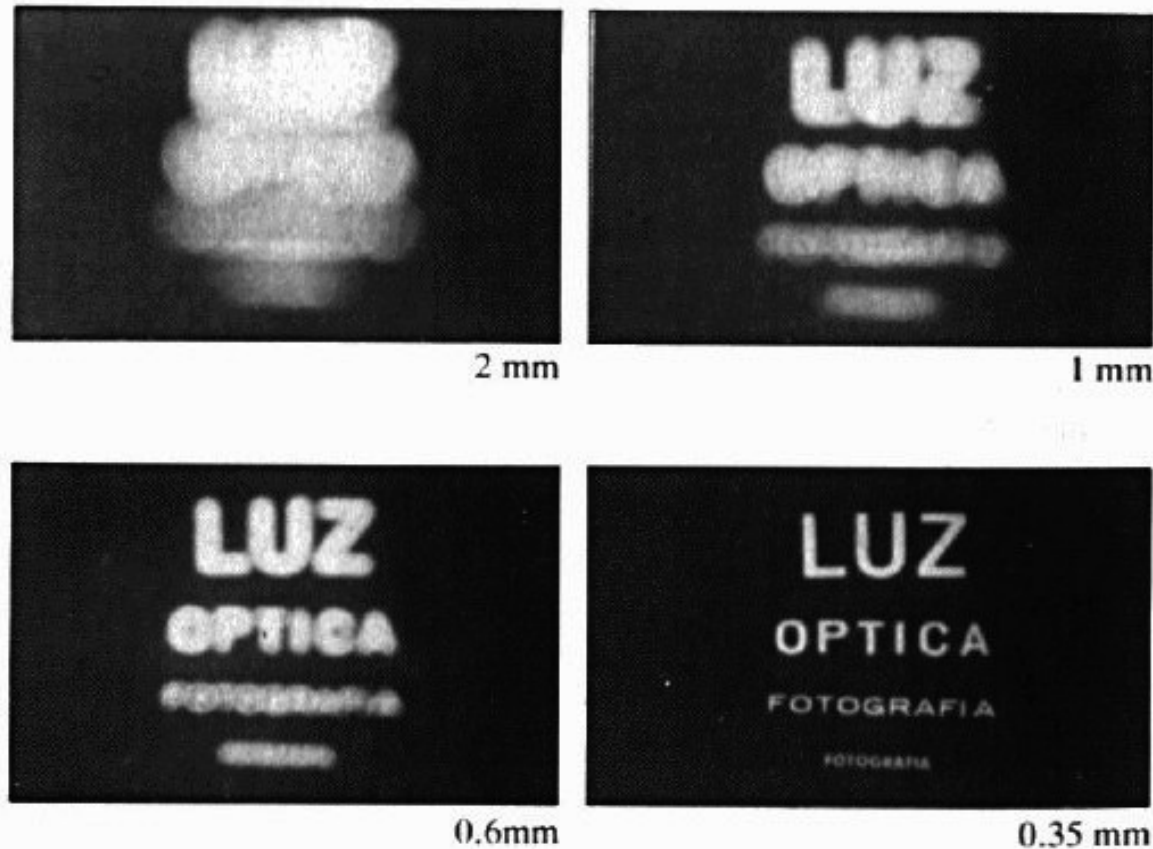
- ◆ The pinhole projection model
  - ▶ Qualitative properties
- ◆ Cameras with lenses
  - ▶ Depth of focus
  - ▶ Field of view
  - ▶ Lens aberrations
- ◆ Digital cameras
  - ▶ Sensors
  - ▶ Colors
  - ▶ Artifacts
- ◆ Novel cameras
  - ▶ Computational photography

# Pinhole camera



- Captures **pencil of rays** - all rays through a single point:  
**aperture, center of projection, focal point, camera center**
- The image is formed on the **image plane**

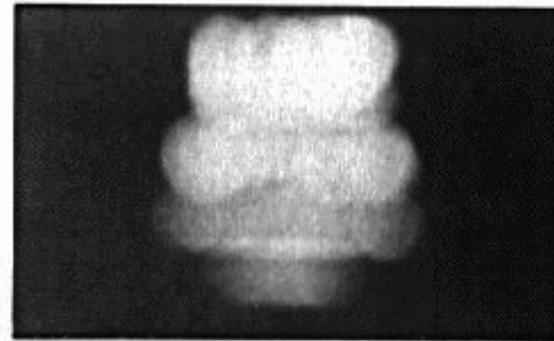
# Shrinking the aperture



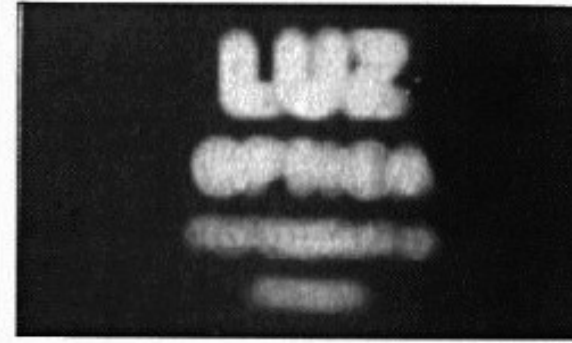
- ◆ Why not make the aperture as small as possible?
  - ▶ Less light gets through
  - ▶ Diffraction effects



# Shrinking the aperture



2 mm



1 mm



0.6mm



0.35 mm

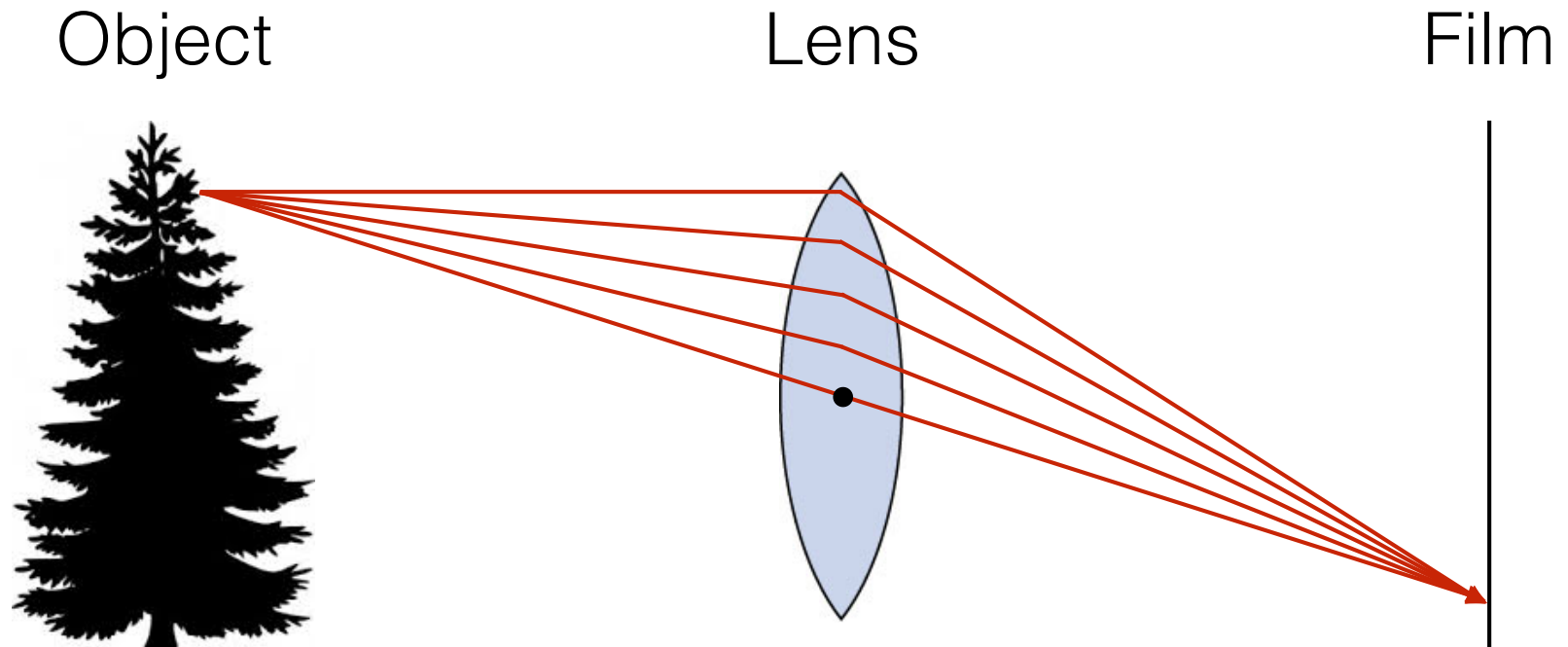


0.15 mm



0.07 mm

# Adding a lens



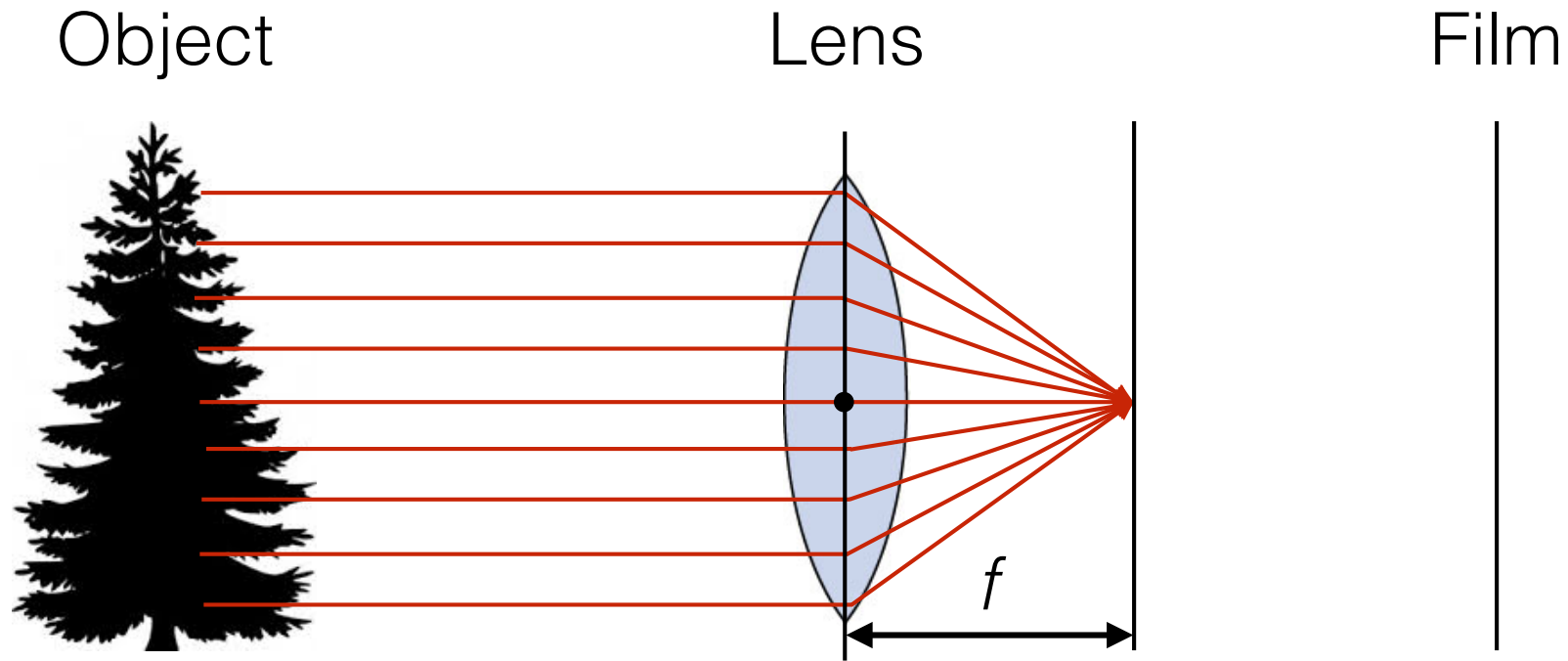
◆ A lens focuses light on to the film

▶ **Thin lens model:**

➔ Rays passing through the center are not deviated (pinhole projection model still holds)



# Adding a lens

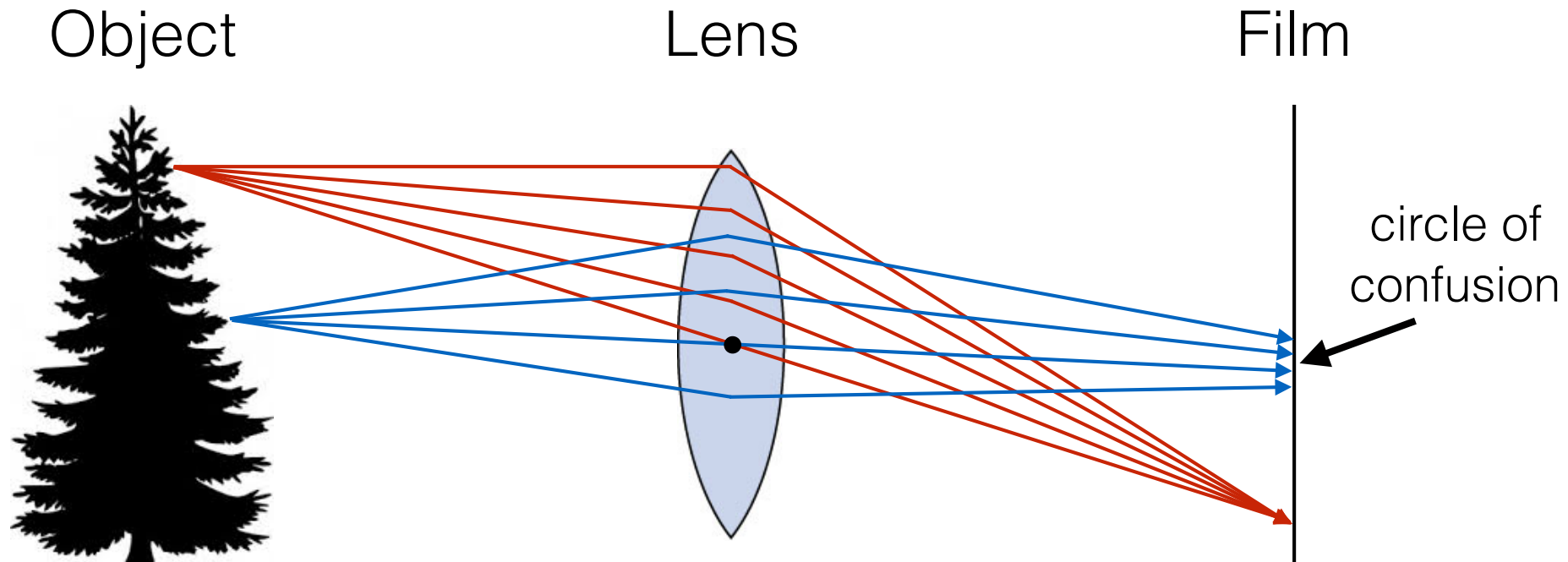


- ◆ A lens focuses light on to the film

- ▶ **Thin lens model:**

- ➔ Rays passing through the center are not deviated (pinhole projection model still holds)
- ➔ All parallel rays converge to one point on a plane located at the *focal length*  $f$

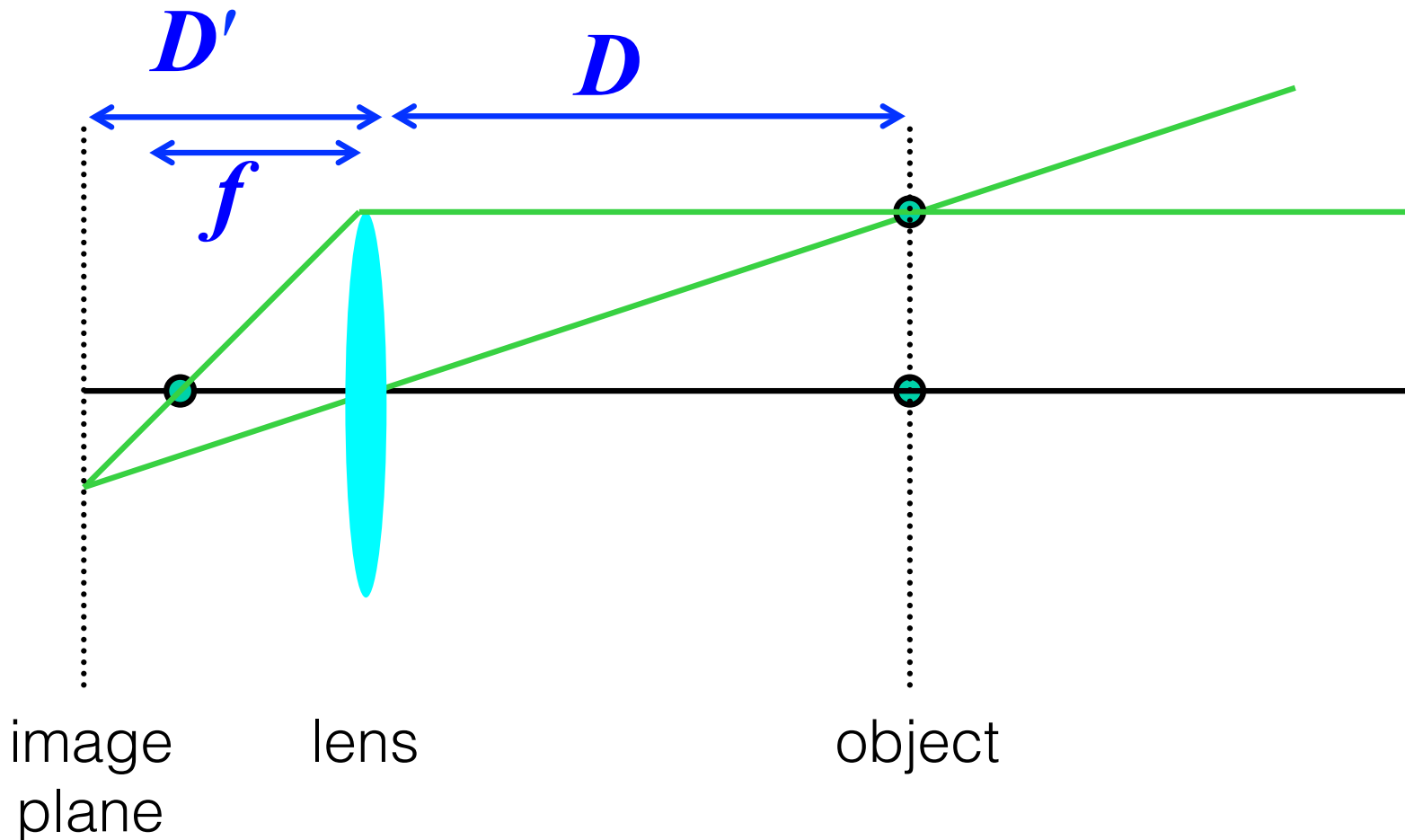
# Adding a lens



- ◆ A lens focuses light on to the film
  - ▶ There is a specific distance at which objects are “in focus”
    - ➔ other points project on to a “circle of confusion” in the image

# Thin lens formula

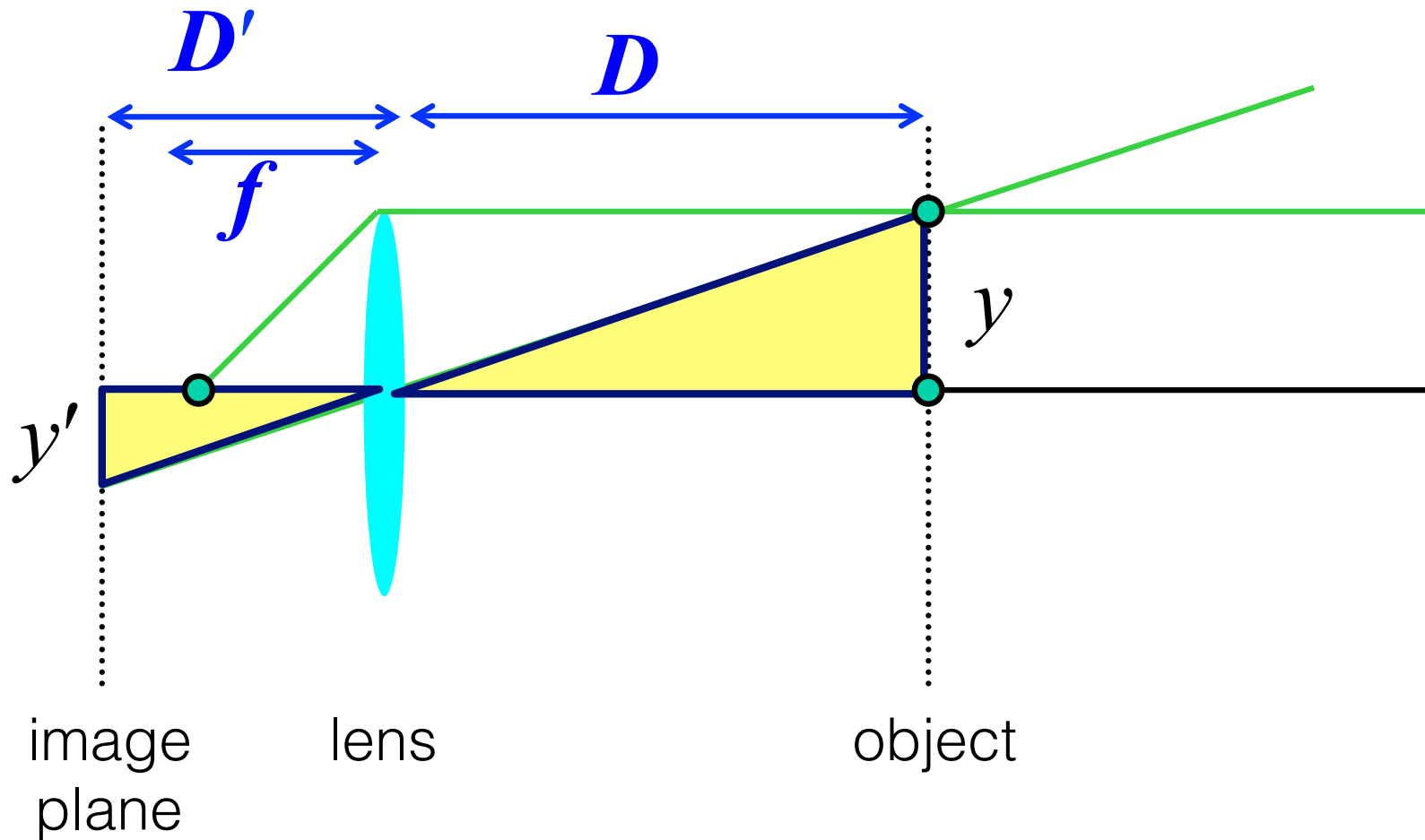
- ◆ What is the relation between the focal length ( $f$ ), the distance of the object from the optical center ( $D$ ) and the distance at which the object will be in focus ( $D'$ )?



# Thin lens formula

- ◆ Similar triangles everywhere!

$$y'/y = D'/D$$

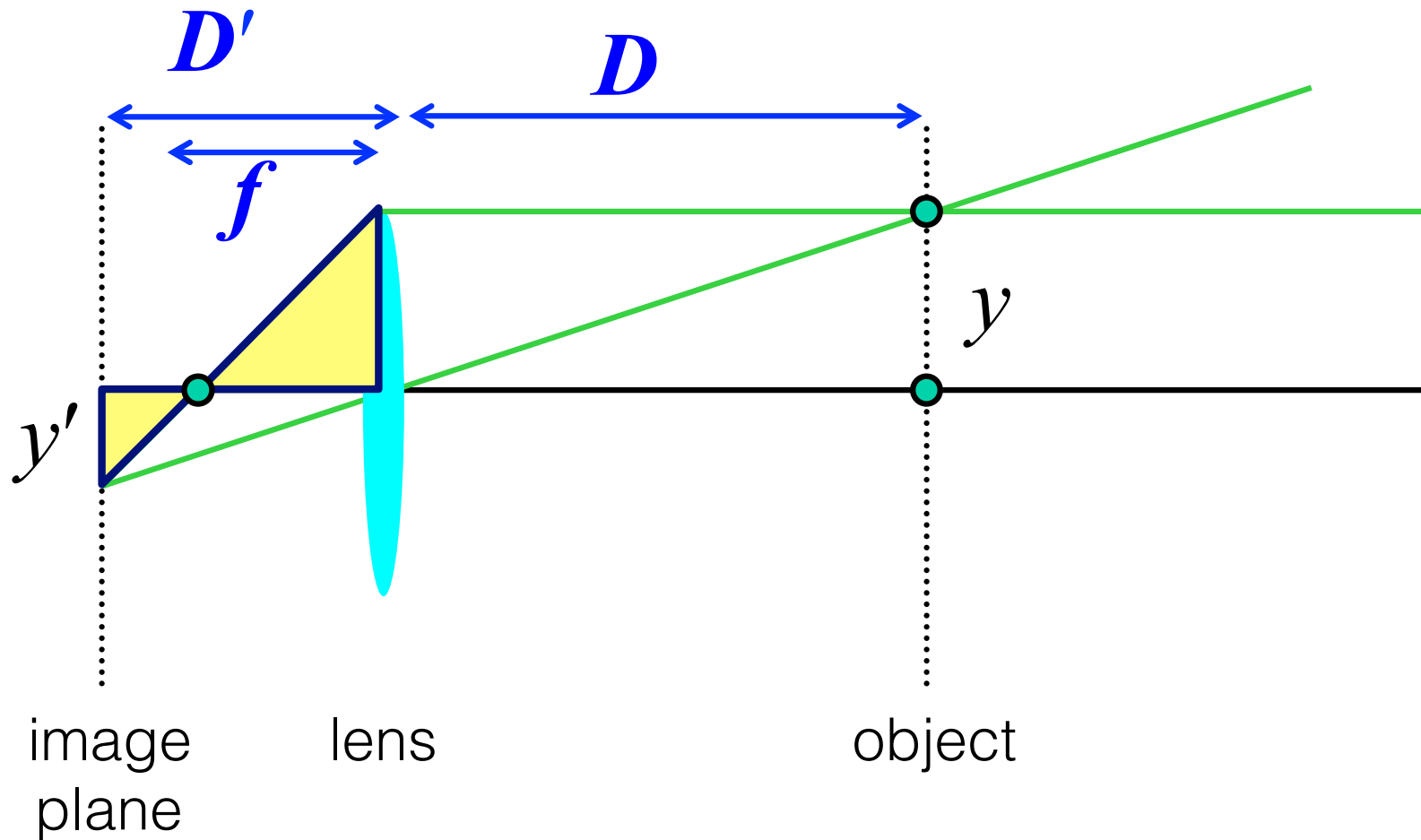


# Thin lens formula

- ◆ Similar triangles everywhere!

$$y'/y = D'/D$$

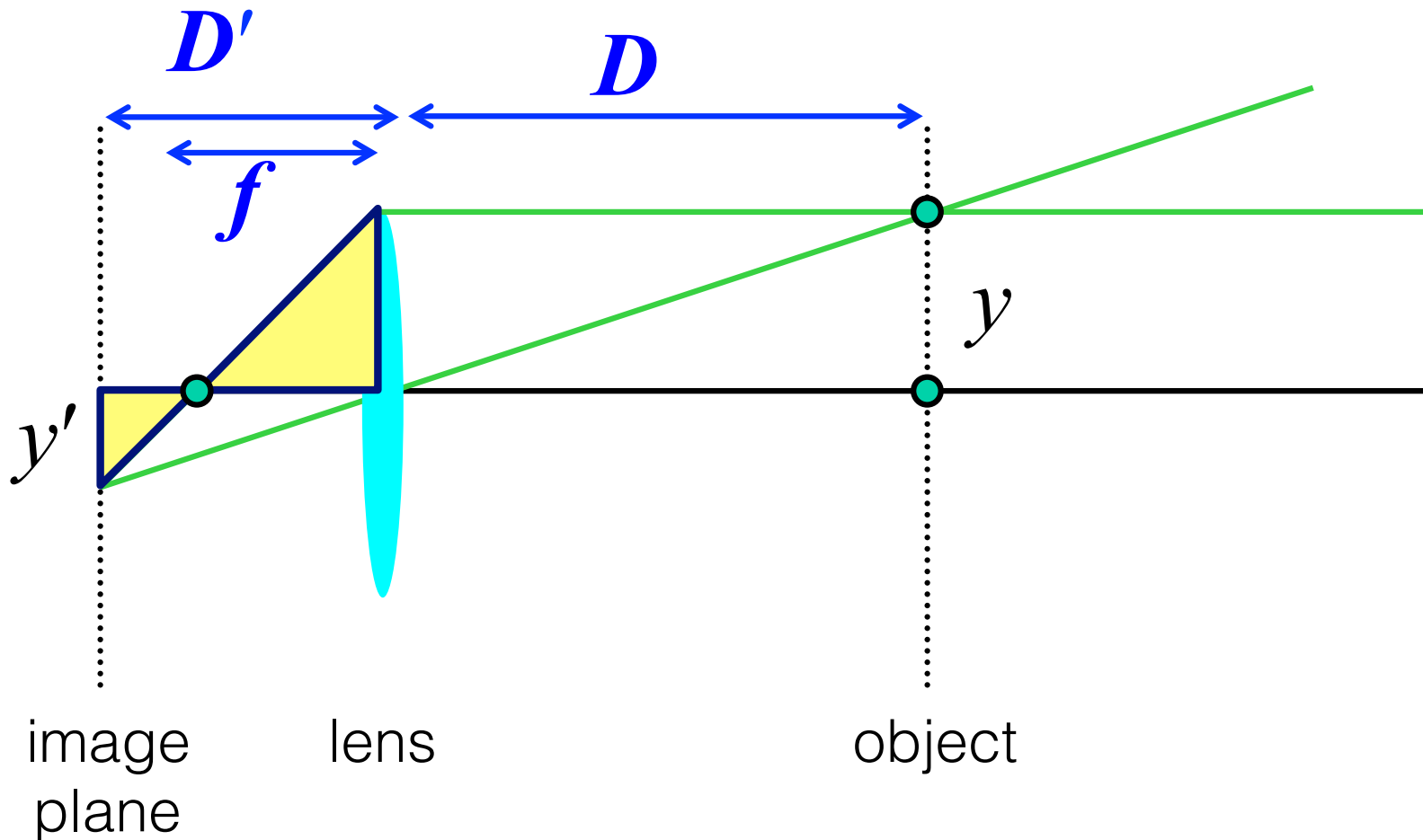
$$y'/y = (D' - f)/f$$



# Thin lens formula

$$\frac{1}{D'} + \frac{1}{D} = \frac{1}{f}$$

Any point satisfying the thin lens equation is in focus





# Depth of field



<http://www.cambridgeincolour.com/tutorials/depth-of-field.htm>

DOF is the distance between the nearest and farthest objects in a scene that appear acceptably sharp in an image

# Varying the aperture

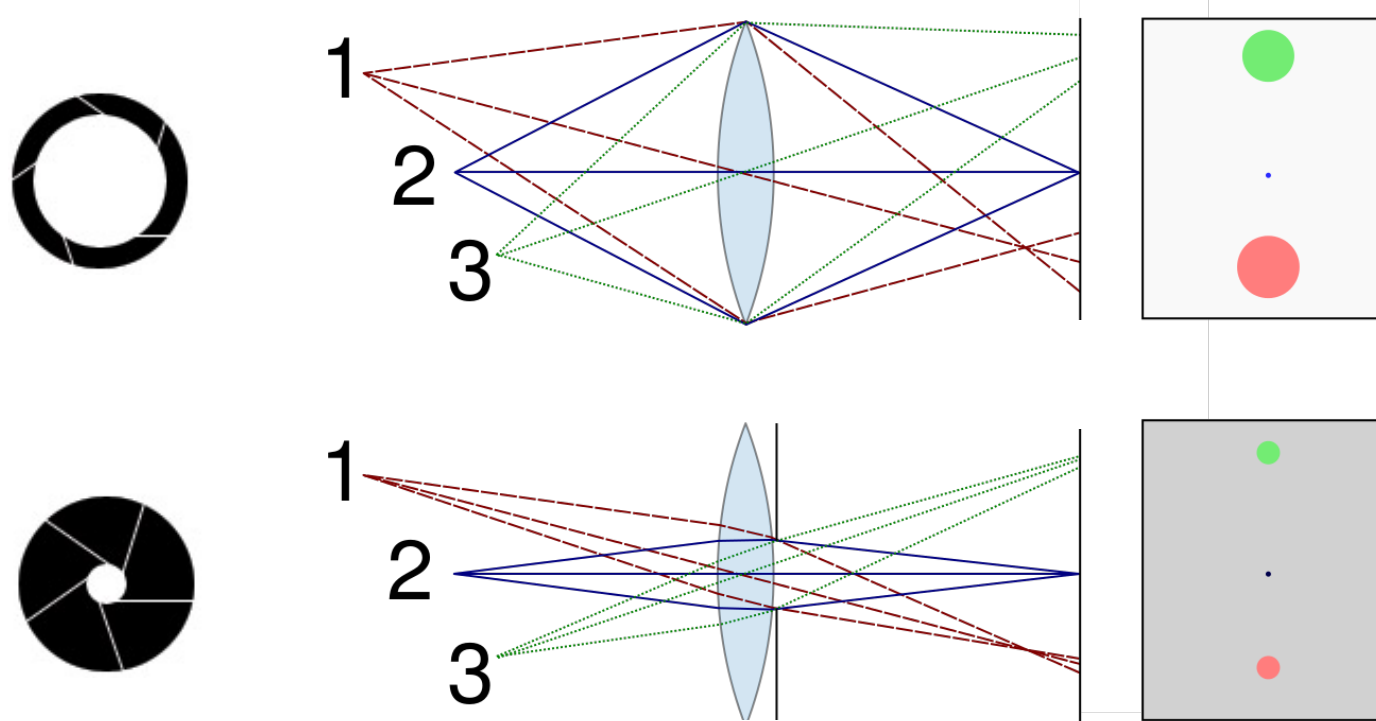


Large aperture = small DOF



Small aperture = large DOF

# Controlling depth of field

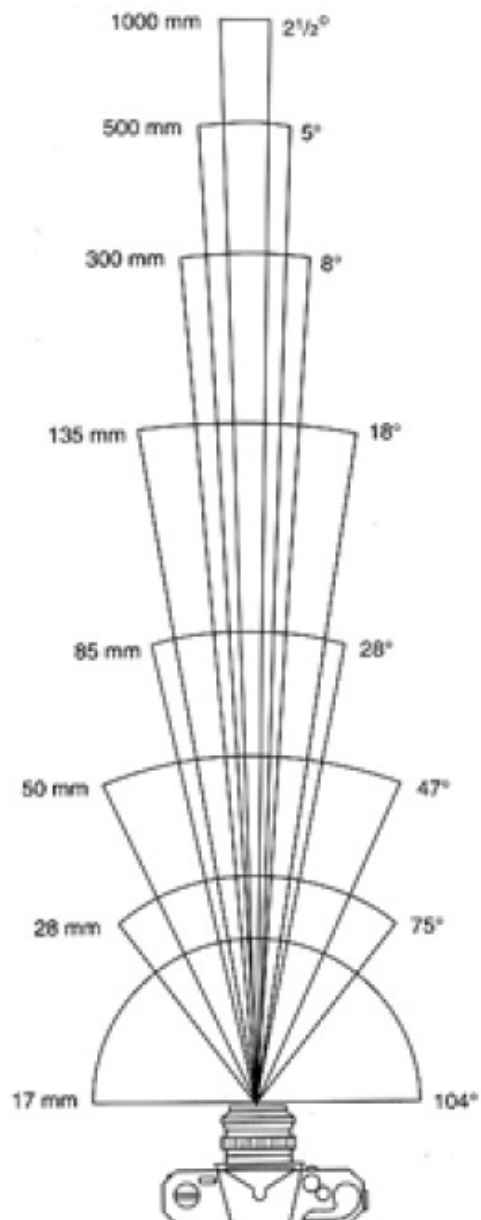


## ◆ Changing the aperture size affects the depth of field

- ▶ A smaller aperture increases the range in which the object is approximately in focus
- ▶ But small aperture reduces the amount of light — need to increase the exposure for contrast
- ▶ Pinhole camera has an infinite depth of field



# Field of view



17mm



28mm

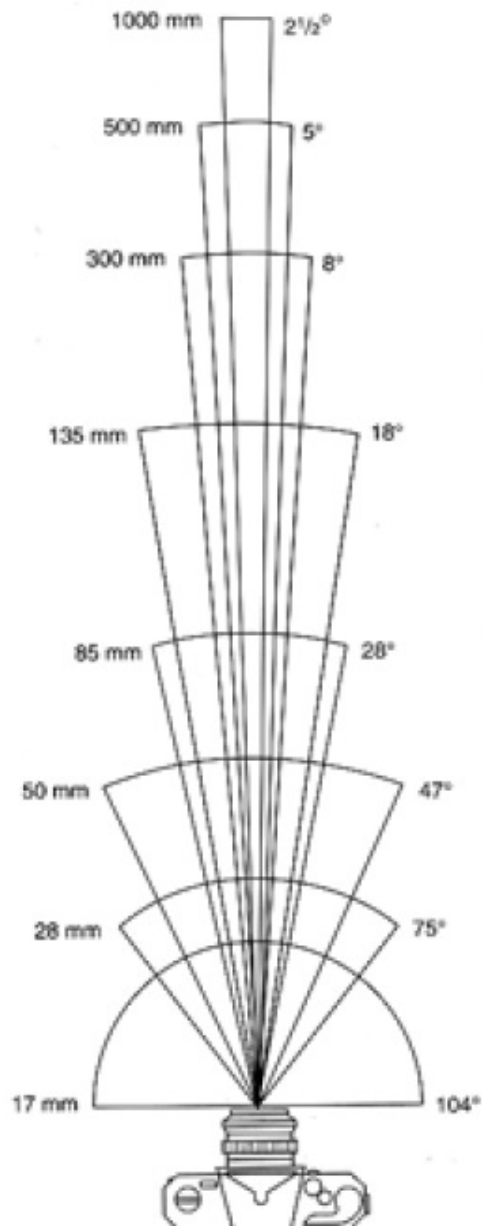


50mm

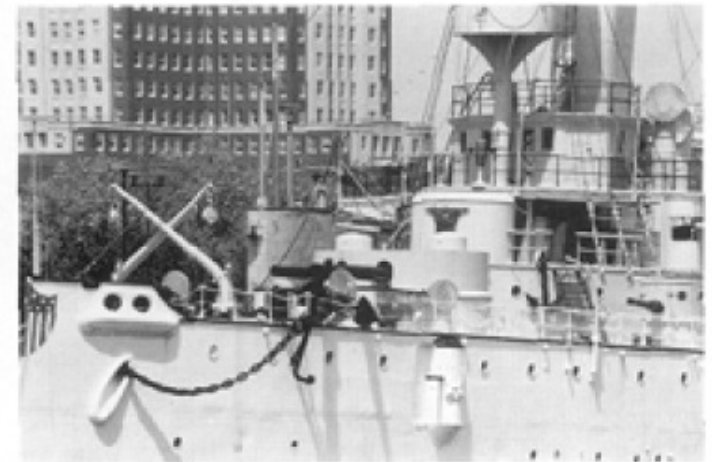


85mm

# Field of view



135mm



300mm

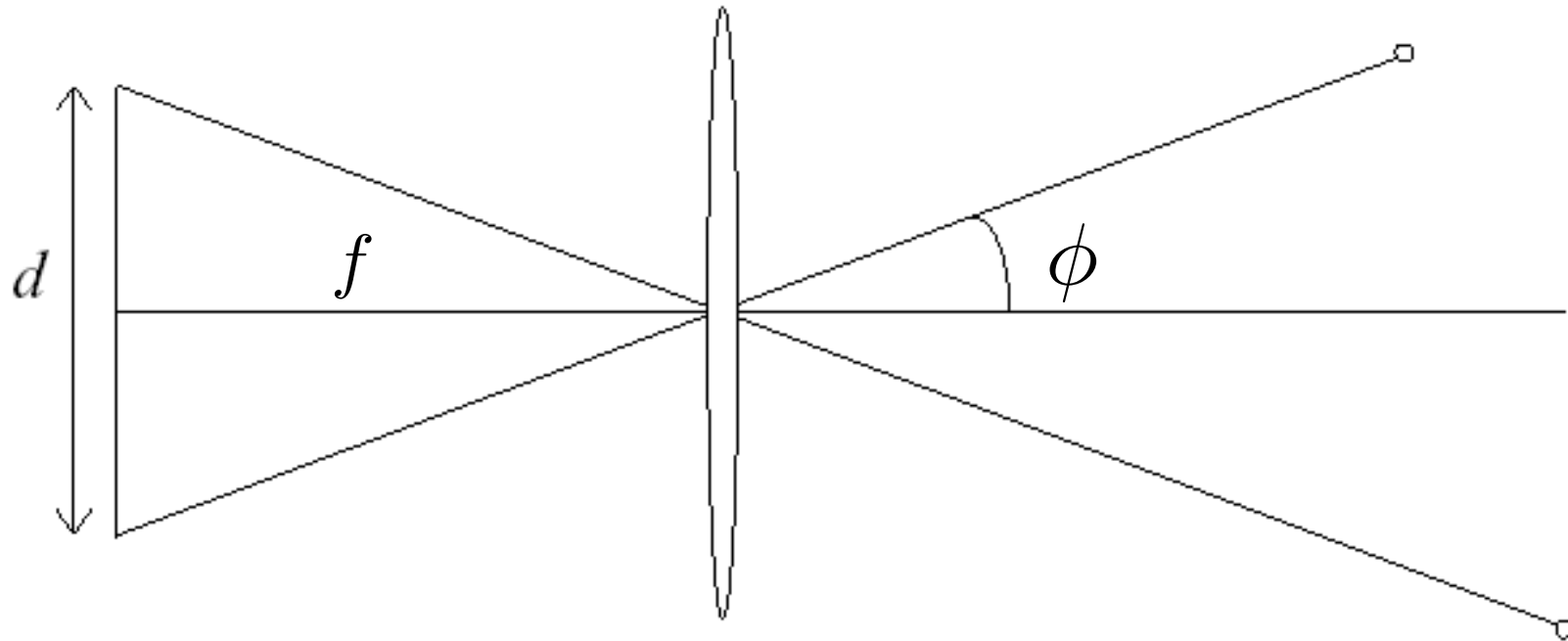


50mm



28mm

# Field of view



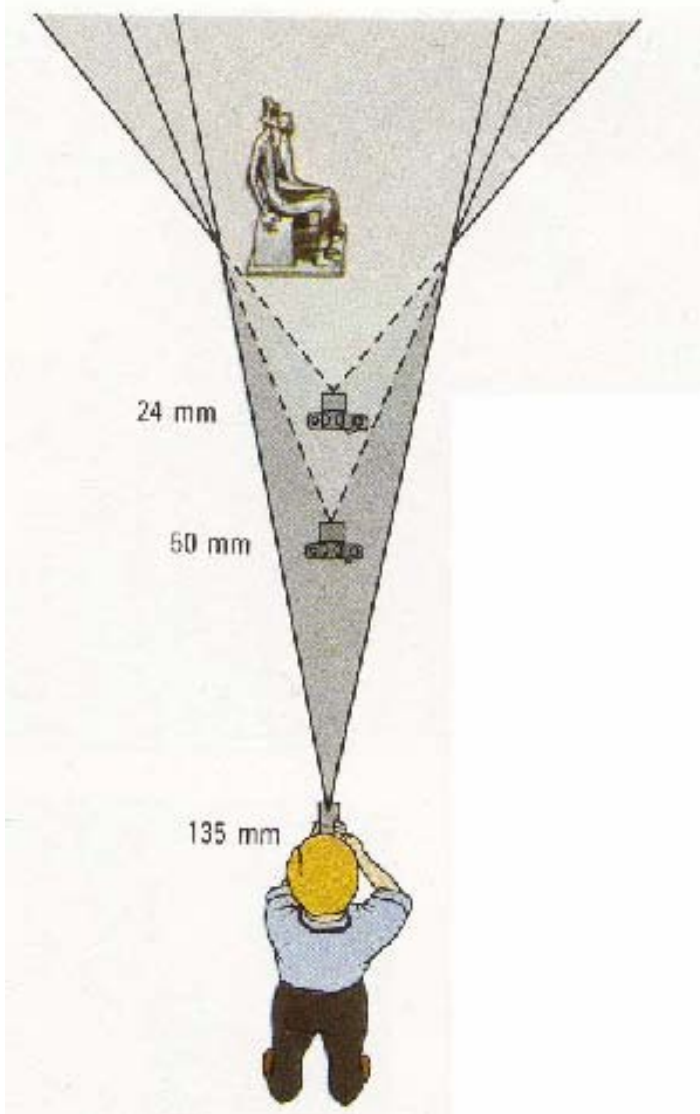
- ◆ Field of view (FOV) depends on the focal length and the size of the camera retina

$$\phi = \tan^{-1} \left( \frac{d}{2f} \right)$$

Larger focal length = smaller FOV



# Field of view, focal length



$$\tan(\phi) \times 2f = d$$

$$\sim (\phi) \times 2f = d$$



Large FOV, small  $f$  — Camera close to the car



Small FOV, large  $f$  — Camera far from the car

# Same effect for faces



wide-angle  
(short focus)



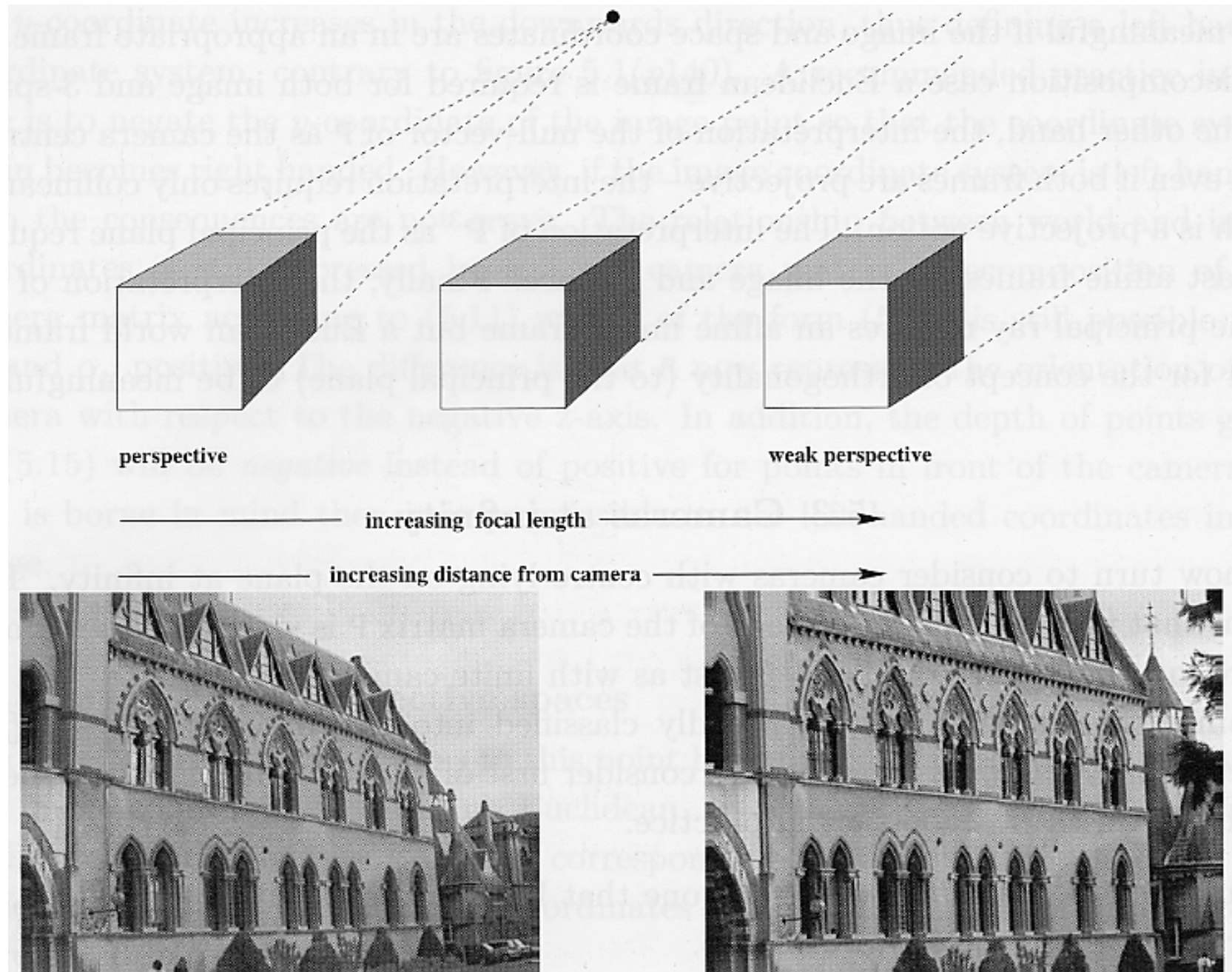
standard



telephoto  
(long focus)

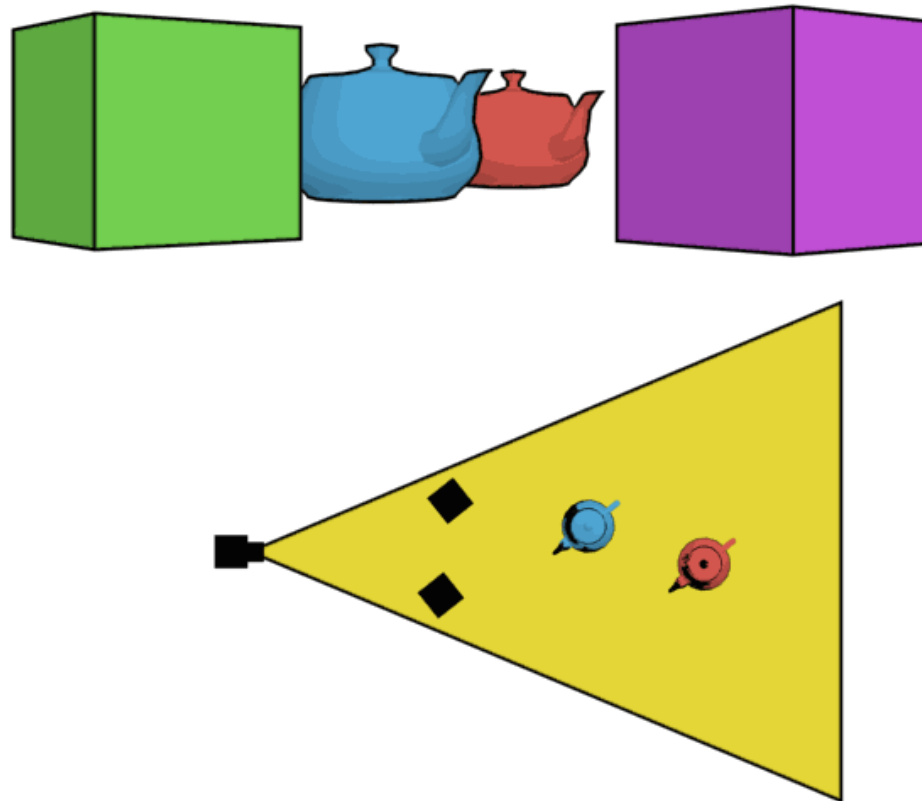


# Approximating an orthographic camera



# The dolly zoom

- ◆ Continuously adjusting the camera focal length while the camera moves away from (or towards) the subject



[http://en.wikipedia.org/wiki/Dolly\\_zoom](http://en.wikipedia.org/wiki/Dolly_zoom)

# The dolly zoom

- ◆ Continuously adjusting the camera focal length while the camera moves away from (or towards) the subject
- ◆ Also called as “Vertigo shot” or the “Hitchcock shot”



[Example of dolly zoom from Goodfellas](#)

[Example of dolly zoom from La Haine](#)

# Image formation ...

Subhransu Maji

CMPSCI 670: Computer Vision

September 13, 2016

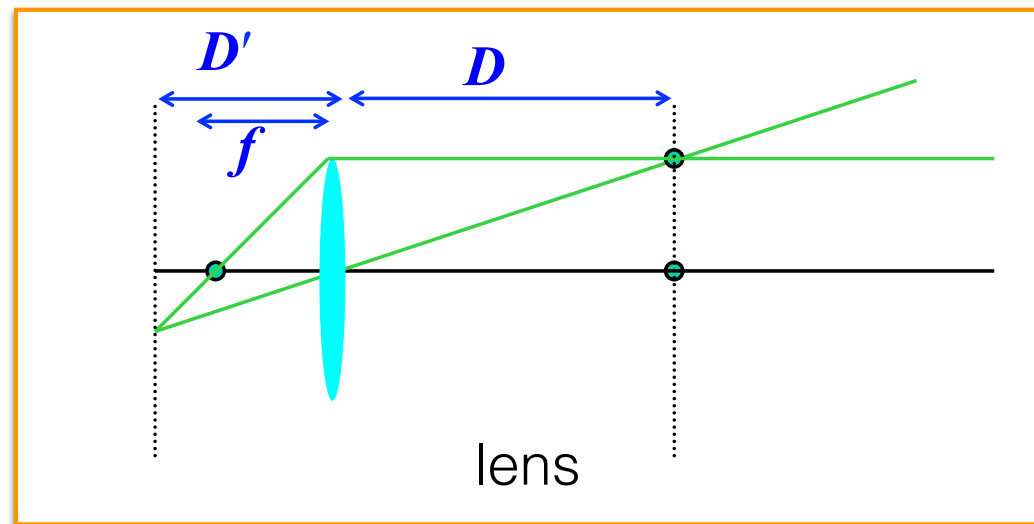
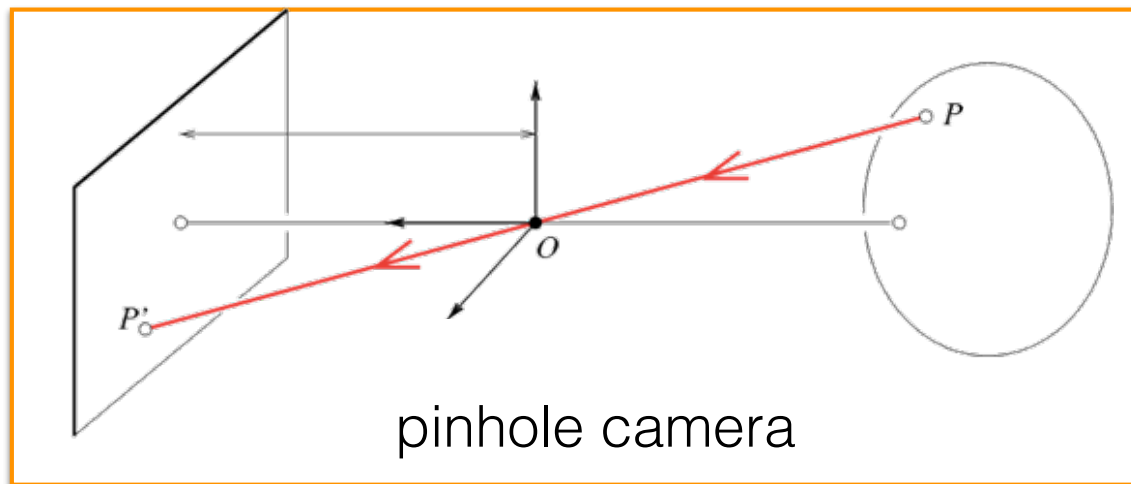


# Administrivia

- ◆ **Homework 01** posted
  - ▶ Due Sept 15, 1pm (That's this **Thursday** before class)
  - ▶ Submissions as pdf via **Moodle** only
    - ➔ Any combination of Latex, Word, print + scan, etc.
- ◆ **Mini-project 1** posted
  - ▶ Due Sept 29
- ◆ Sign up on **Piazza** for announcements
  - ▶ I'll use this as the primary place for announcements
- ◆ Lecture slides and materials are posted on **webpage**
- ◆ **TA office hours**:
  - ▶ Wednesday 3-4PM, Location: CS 245
- ◆ Waitlisted students?
  - ▶ Definitely talk to me after class (OH: Today, 2:30 - 3:30pm, CS 274)

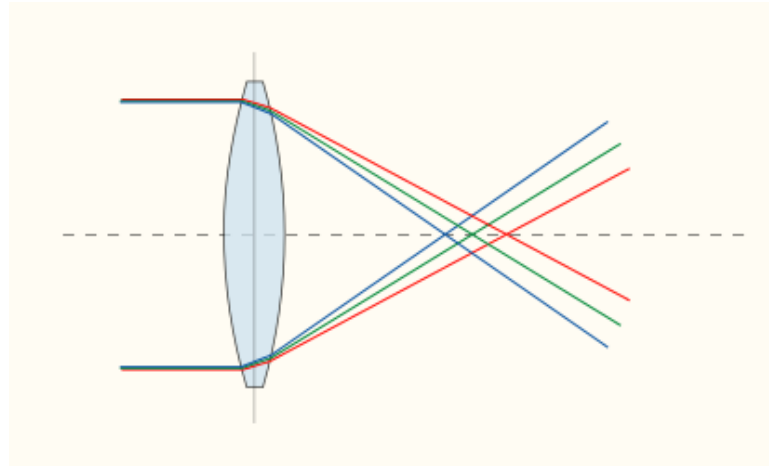
# Recap of the last lecture

- ◆ The pinhole projection model
  - Qualitative properties
- ◆ Cameras with lenses
  - Depth of focus
  - Field of view
  - Lens aberrations
- ◆ Digital cameras
  - Sensors
  - Colors
  - Artifacts
- ◆ Computational photography
  - Novel sensors and cameras



# Lens flaws: Chromatic aberration

- ◆ Lens have different refractive indices ([Snell's law](#)) for different wavelengths: causes color fringing



near lens center

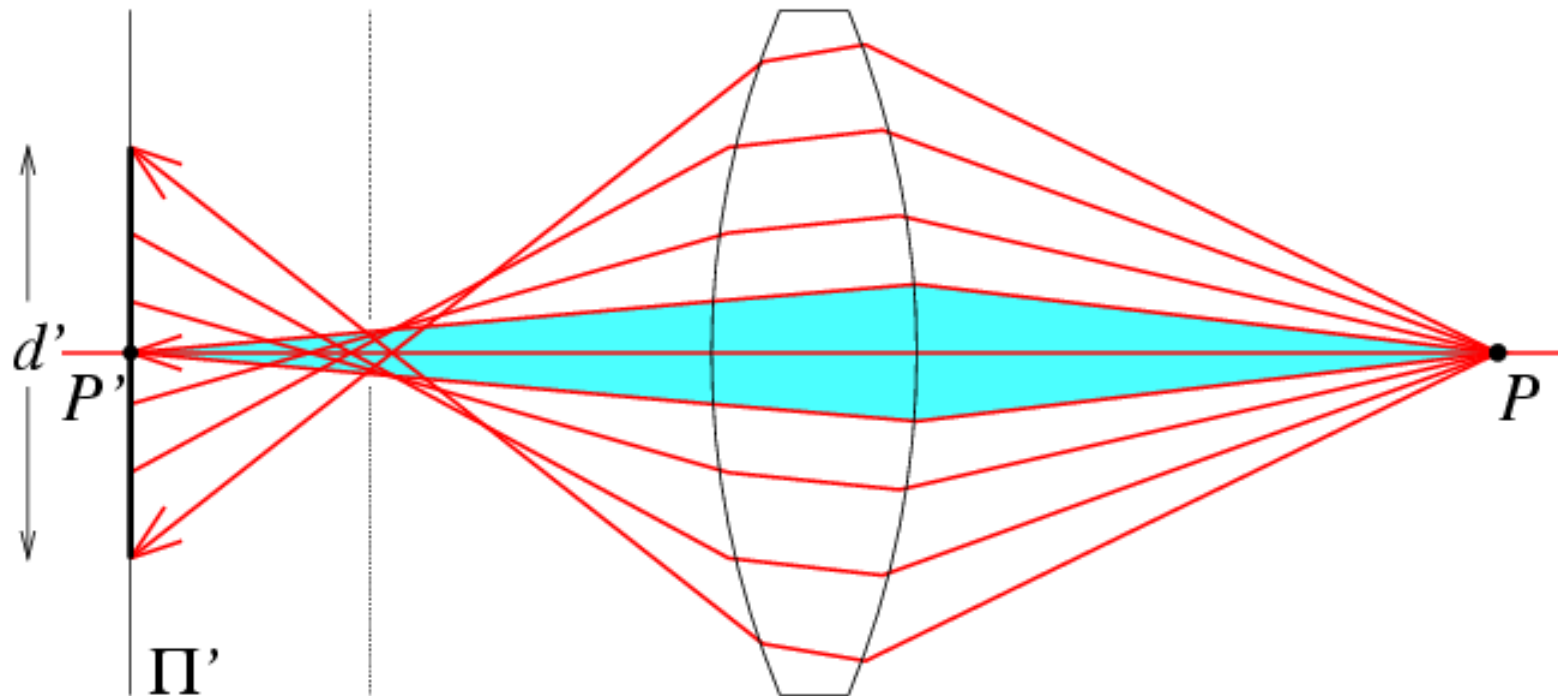


near lens outer



# Lens flaws: Spherical aberration

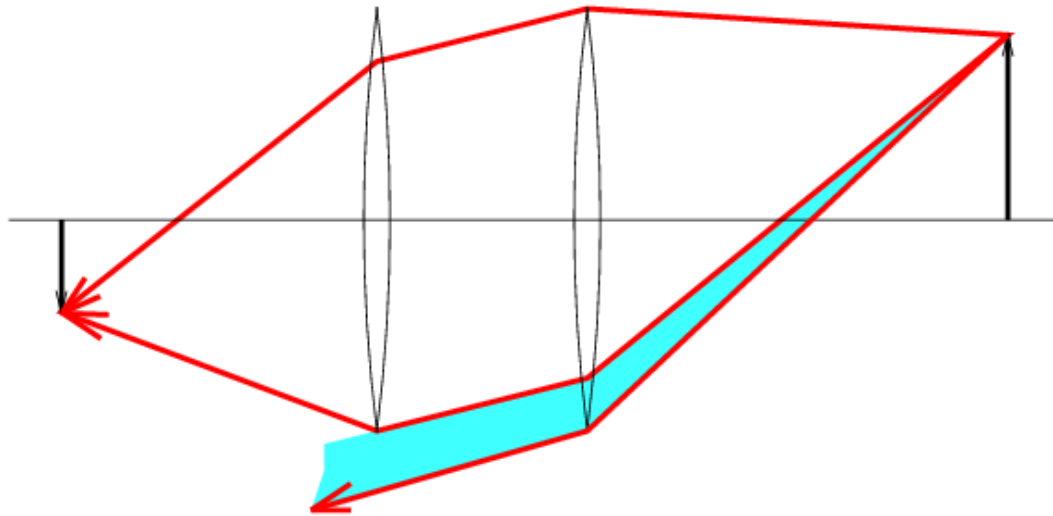
- ◆ Spherical lenses don't focus light perfectly (thin lens model)
  - ▶ Rays farther from the optical axis are focussed closer



objects lack sharpness

# Lens flaws: Vignetting

- ◆ Reduction of image brightness in the periphery



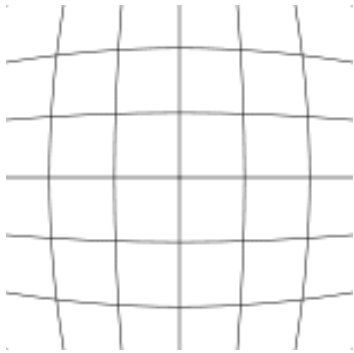
Not all rays  
reach the sensor



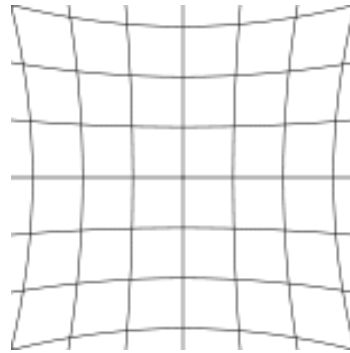


# Lens flaws: Radial distortion

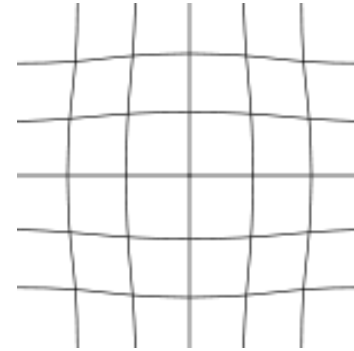
- ◆ Caused by asymmetry of lenses
- ◆ Deviations are most noticeable near the periphery



**barrel distortion**



**pincushion distortion**



**mustache distortion**

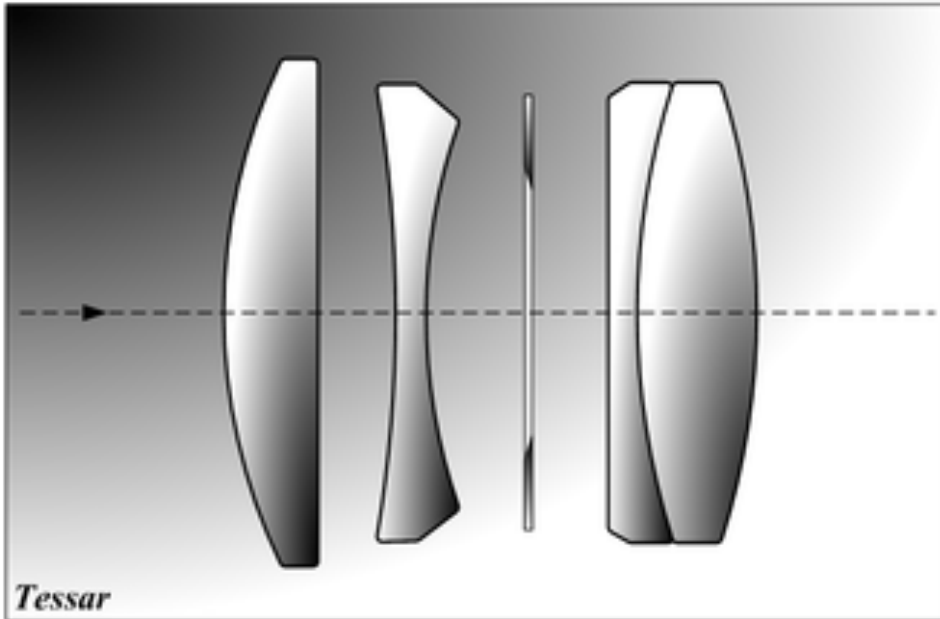




# Real photographic lens

- ◆ Many uses: cameras, telescopes, microscopes, etc

fixed focal length



Example of a prime lens - Carl Zeiss [Tessar](#)

adjustable zoom



[Nikor](#) 28-200 mm zoom lens, extended to 200 mm at left and collapsed to 28 mm focal length at right.

[http://en.wikipedia.org/wiki/Zoom lens](http://en.wikipedia.org/wiki/Zoom_lens)

# Overview

- ◆ The pinhole projection model
  - qualitative properties
- ◆ Cameras with lenses
  - Depth of focus
  - Field of view
  - Lens aberrations
- ◆ Digital cameras
  - Sensors
  - Colors
  - Artifacts
- ◆ Novel cameras
  - Computational photography

# Measuring light

- ◆ **Photographic film** — strip of transparent plastic film base coated on one side with a gelatin emulsion containing light-sensitive materials
- ◆ Creates a latent image when exposed to light for short duration
- ◆ Films are then chemically developed to form a photograph
- ◆ Early films/photographic plates could only capture intensity



# Early color photography

- ◆ Sergey Prokudin-Gorskii (1863-1944)
- ◆ Photographs of the Russian empire (1909-1916)





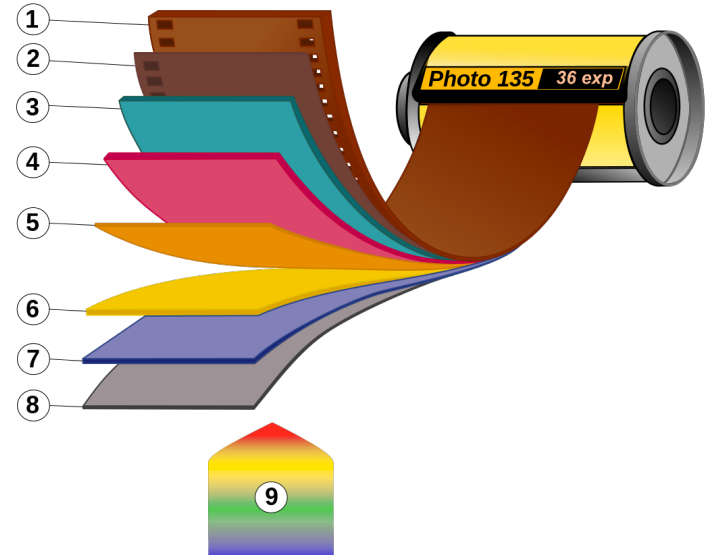
# Only problem!



Homework 1: fix this by aligning the channels

# Measuring light: color films

- ◆ Color photographic film — many layers of dyes and light sensitive materials to capture light of different frequencies simultaneously
  - ▶ Kodak pioneered color films for making paper prints
- ◆ Simultaneous measurement solves the alignment problem
  - ▶ But needs complex film design and development process





# Digital images

- ◆ Color images are commonly represented using 3 channels [R, G, B]
  - ▶ The color of each pixel is given by the (r,g,b) value

```
>> im = imread('jelly.jpg');  
>> whos im  
Name           Size           Bytes   Class   Attributes  
  
im             428x570x3         731880  uint8  
  
>> imshow(im);  
>> imshow(im(:,:,1));  
>> imshow(im(:,:,2));  
>> imshow(im(:,:,3));
```



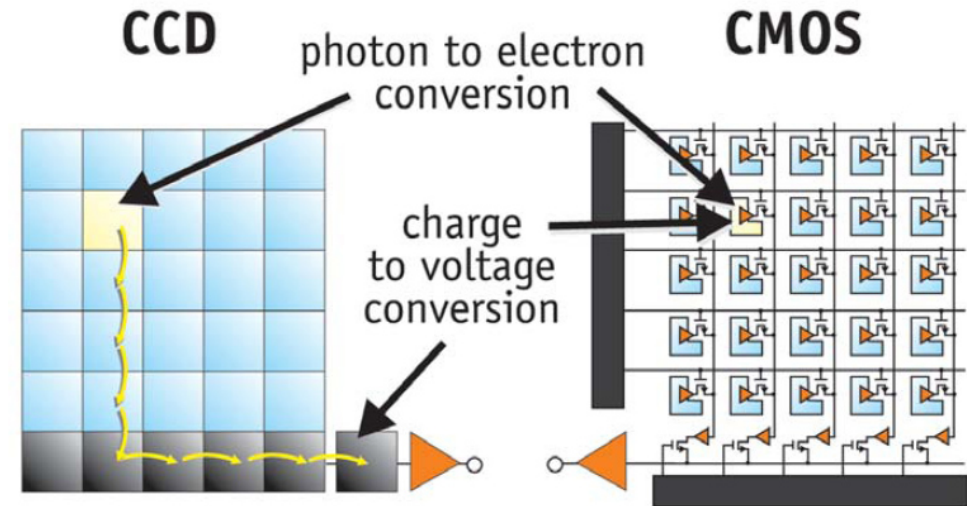
red

green

blue



# Digital camera



CCDs move photogenerated charge from pixel to pixel and convert it to voltage at an output node. CMOS imagers convert charge to voltage inside each pixel.

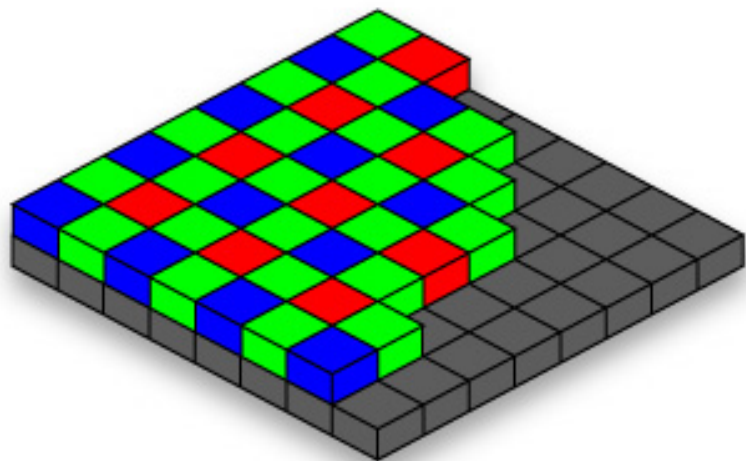
- ◆ A digital camera replaces the film with a sensor array
  - ▶ Each cell in the array is a light-sensitive diode that converts photons to electrons
  - ▶ Two common types of sensor arrays
    - ➔ Charge Coupled Device (CCD)
    - ➔ Complementary Metal Oxide Semiconductor (CMOS)

<http://electronics.howstuffworks.com/digital-camera.htm>

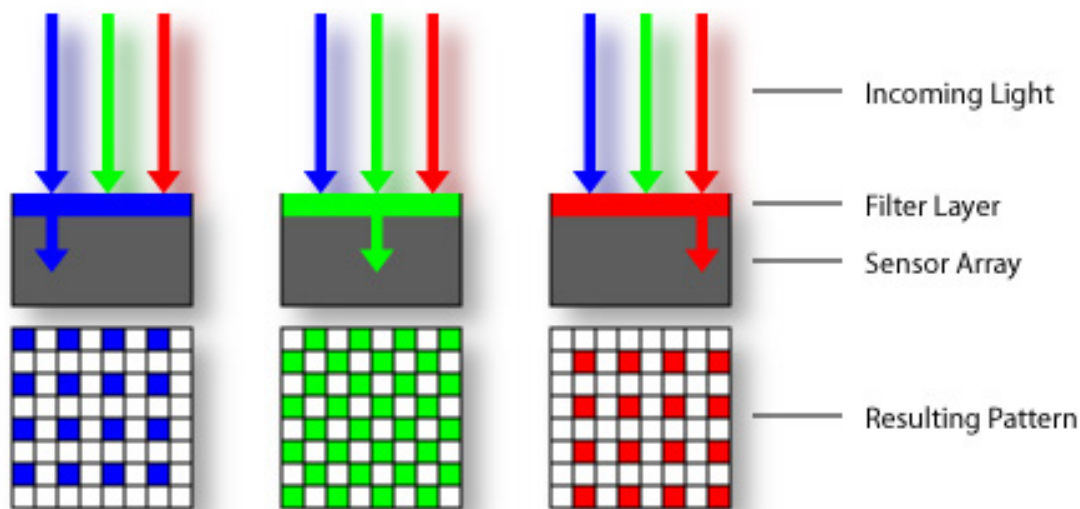
# Color sensing in the camera

Color filter array

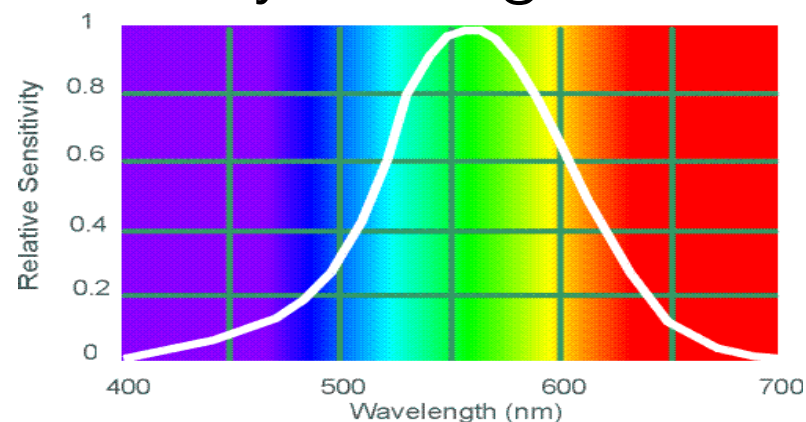
Bayer grid



Estimate missing components from neighboring values  
(**demosiacing**)



Why more green?

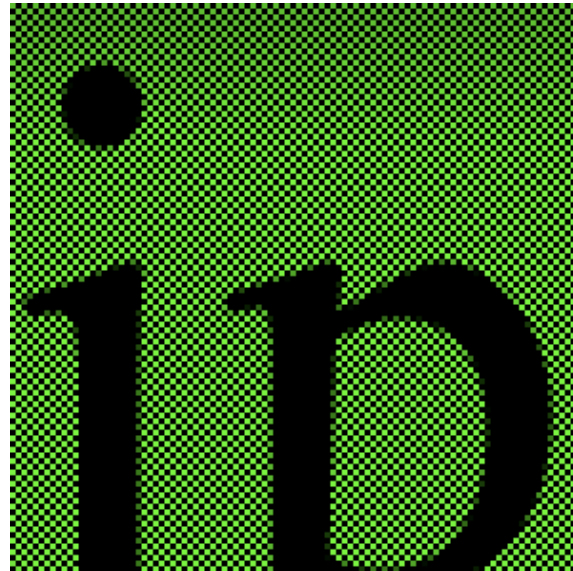


Human luminance sensitivity function

# Demosaicing



Red



Green

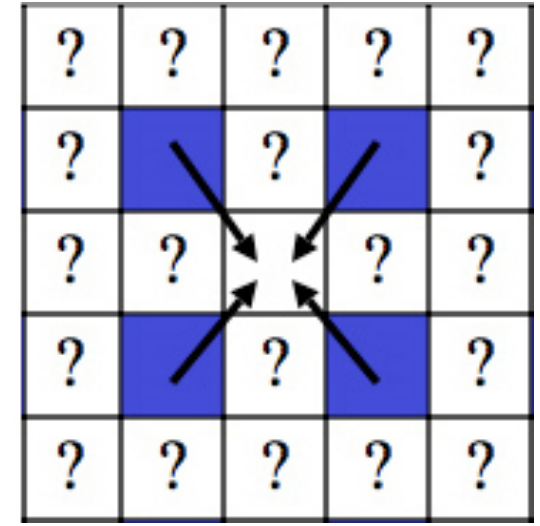
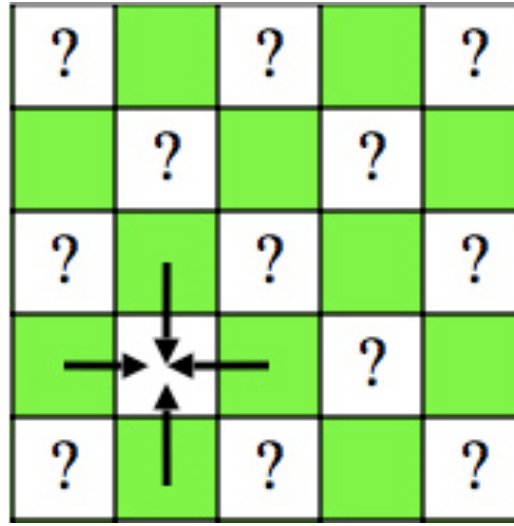
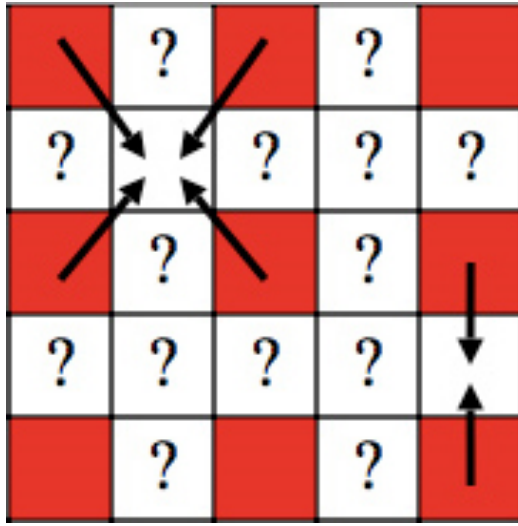


Blue

Subhransu Maji (UMass, Fall 16)

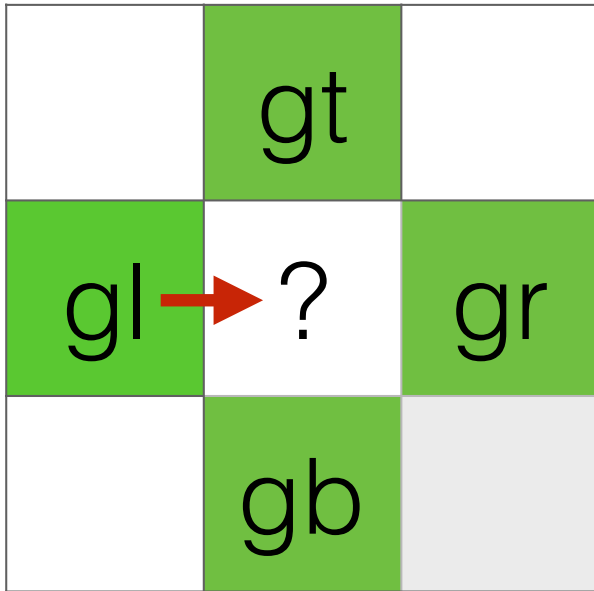


# Demosaicing



- ◆ Problem: guess the values of ? in each of the three channels
- ◆ Why is this even possible?

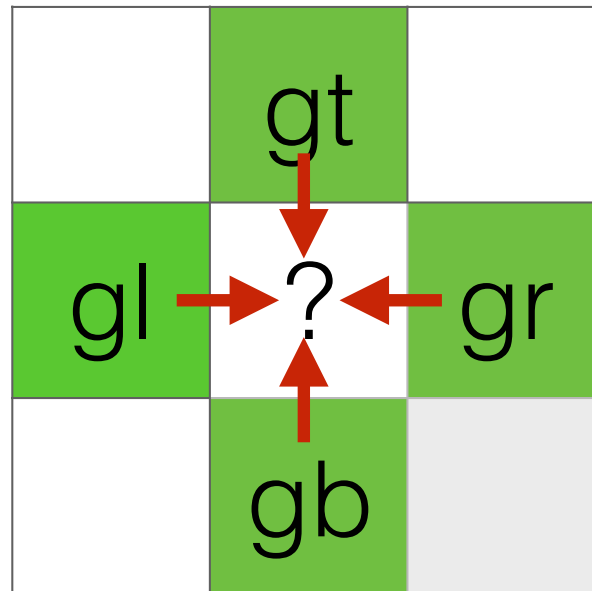
# Interpolation



## nearest neighbor

copy one of your neighbors

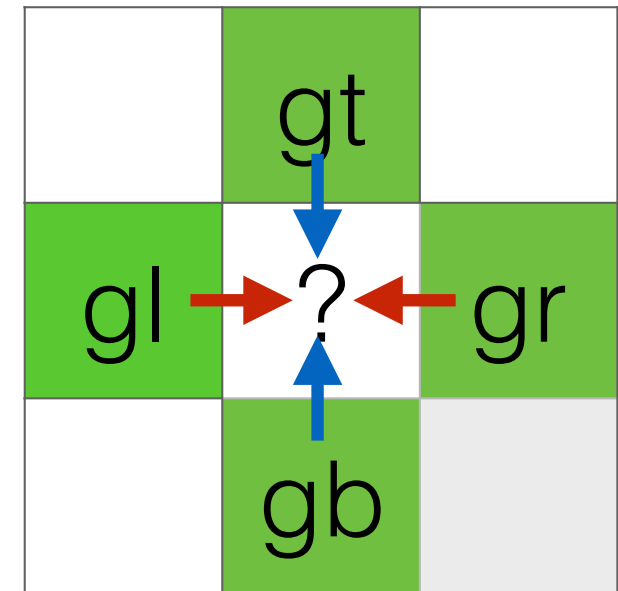
$$? \leftarrow gl$$



## linear interpolation

average values of your neighbors

$$? \leftarrow (gt+gl+gr+gb)/4$$



## adaptive gradient

average based on nbhd. structure

if  $|gt-gb| > |gl-gr|$

$$? \leftarrow (gl+gr)/2$$

else

$$? \leftarrow (gt+gb)/2$$

Similarly for the blue and red channels

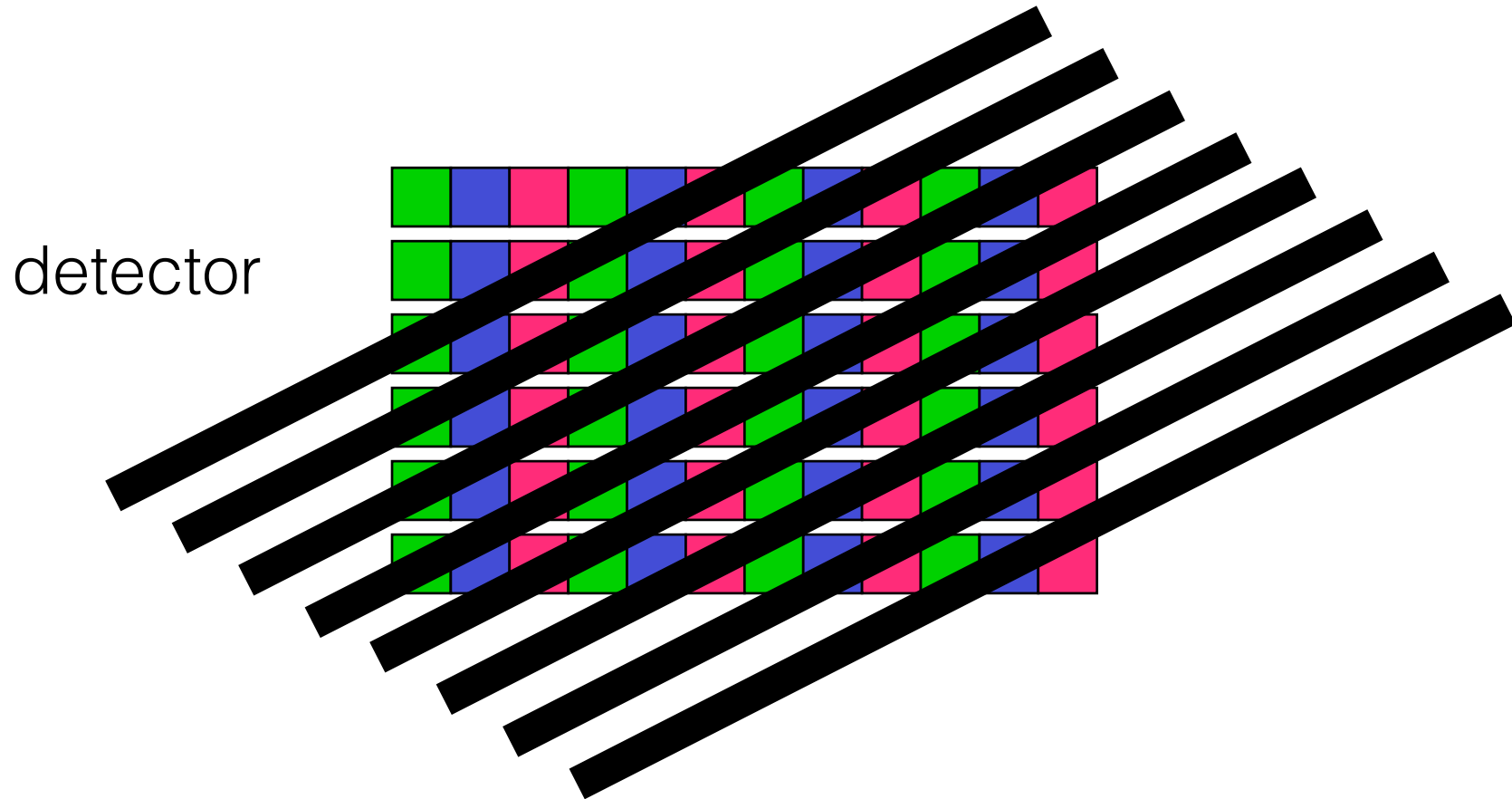
**Homework 1:** implement this



# Problem with demosaicing: color moiré

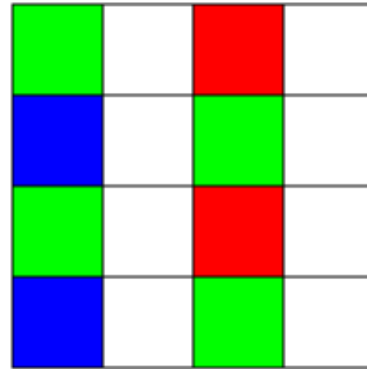
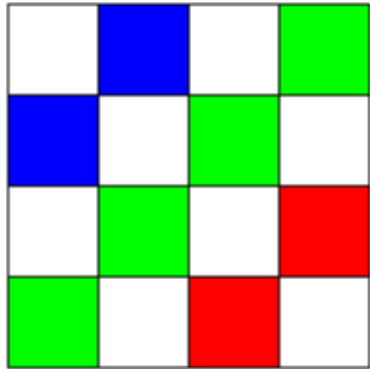


# The cause of color moiré

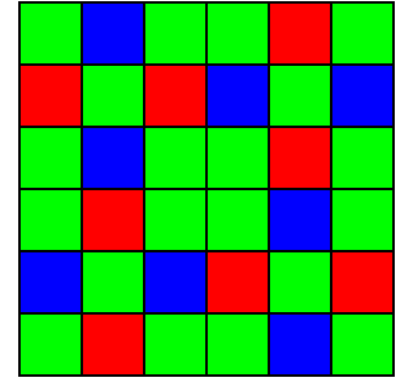


Fine black and white detail in the image scene  
is misinterpreted as color information

# Alternatives to Bayer filter



Three new Kodak RGBW filter patterns

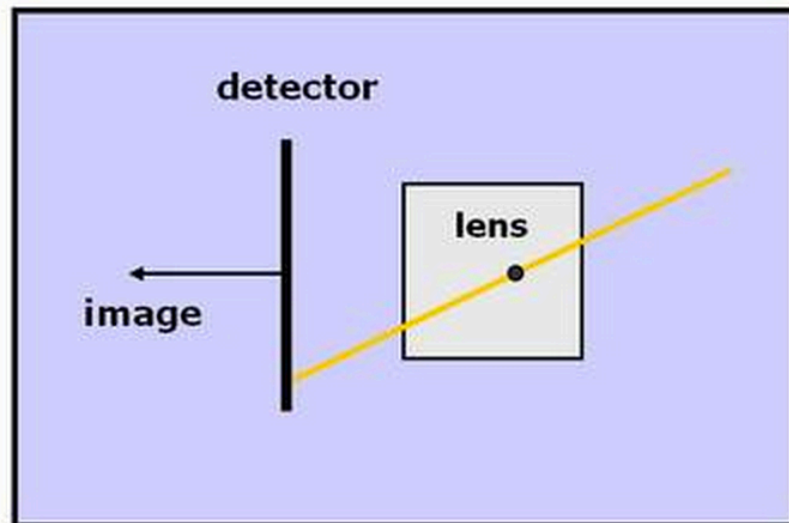


Fujifilm "X-Trans" filter

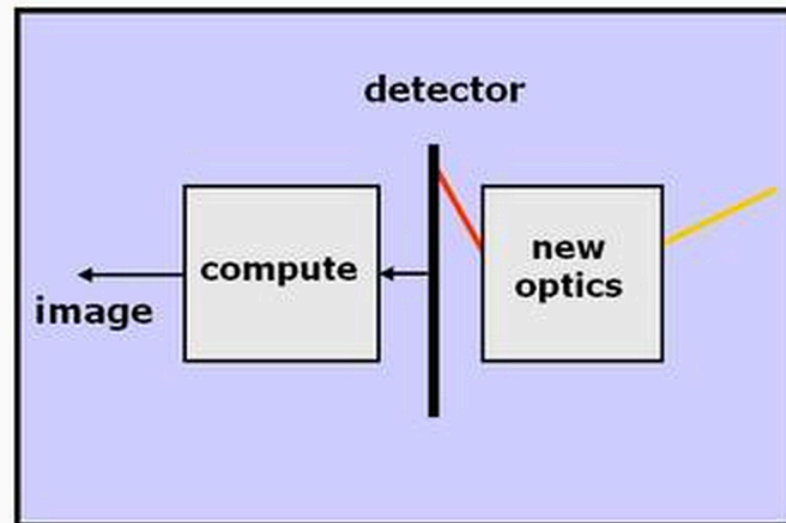
- ◆ White or “panchromatic” cells allow lights across all wavelengths
  - Better light efficiency
- ◆ How would you go about picking the best one?

Source: [https://en.wikipedia.org/wiki/Bayer\\_filter](https://en.wikipedia.org/wiki/Bayer_filter)

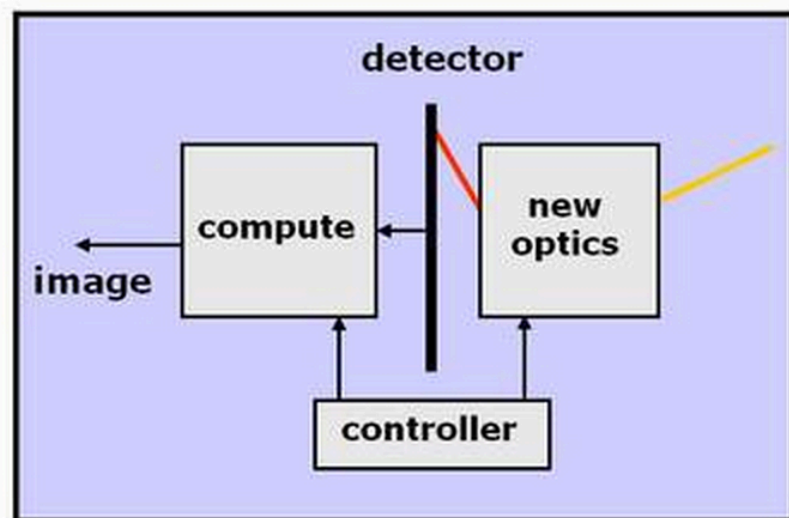
# Computational cameras



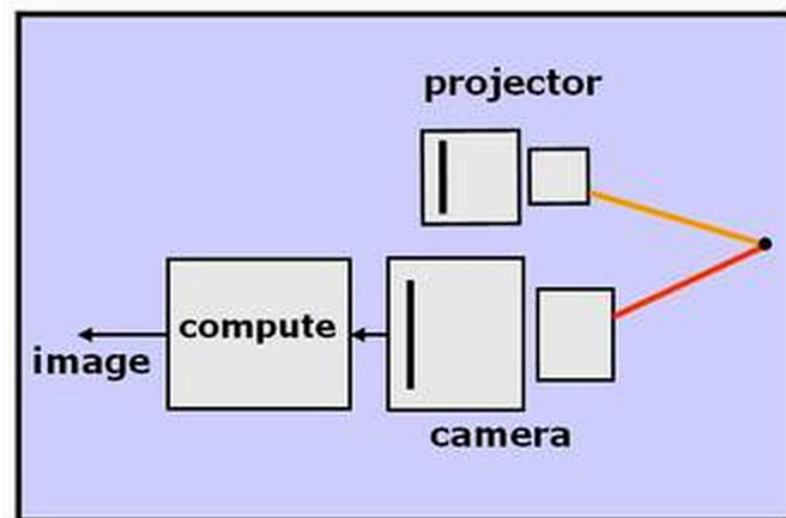
(a) Traditional Camera



(b) Computational Camera



(c) Programmable Imaging



(d) Programmable Flash

S.K. Nayar [http://www1.cs.columbia.edu/CAVE/projects/what\\_is/](http://www1.cs.columbia.edu/CAVE/projects/what_is/)

# Computational color photography

- ◆ Goal: Design a **sampling pattern** + **interpolation algorithm** that archives the **best color reconstruction**
- ◆ Sampling patterns
  - ▶ Given a  $n \times n$  filter array we have  $4^{(n \times n)}$  possible choices
    - ➔ More choices if we allow different color filters
  - ▶ Some patterns are obviously bad for reconstruction
- ◆ Interpolation algorithms
  - ▶ Can't easily enumerate this space
  - ▶ Non trivial algorithms for interpolation



# Rethinking Color Cameras

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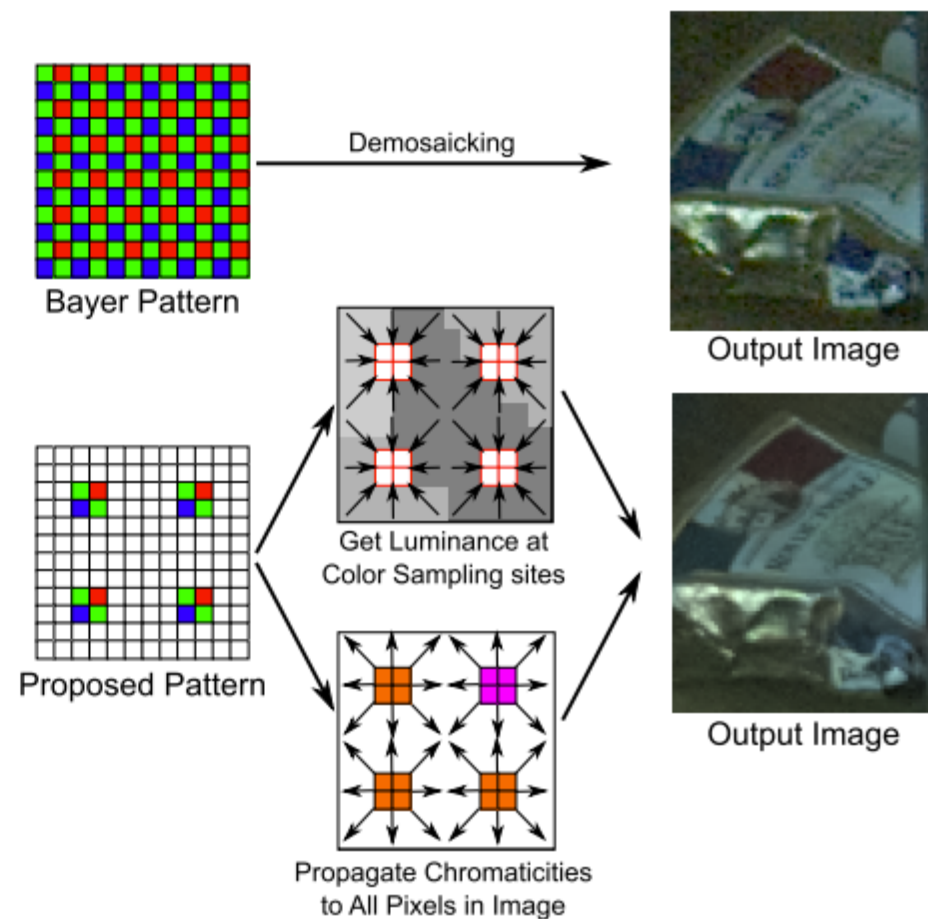
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## Abstract

*Digital color cameras make sub-sampled measurements of color at alternating pixel locations, and then “demo-saick” these measurements to create full color images by up-sampling. This allows traditional cameras with restricted processing hardware to produce color images from a single shot, but it requires blocking a majority of the incident light and is prone to aliasing artifacts. In this paper, we introduce a computational approach to color photography, where the sampling pattern and reconstruction process are co-designed to enhance sharpness and photographic speed. The pattern is made predominantly panchromatic, thus avoiding excessive loss of light and aliasing of high spatial-frequency intensity variations. Color is sampled at a very sparse set of locations and then propagated throughout the image with guidance from the un-aliased luminance channel. Experimental results show that this approach often leads to significant reductions in noise and aliasing arti-*



linearly interpolate color value using intensity-based affinities

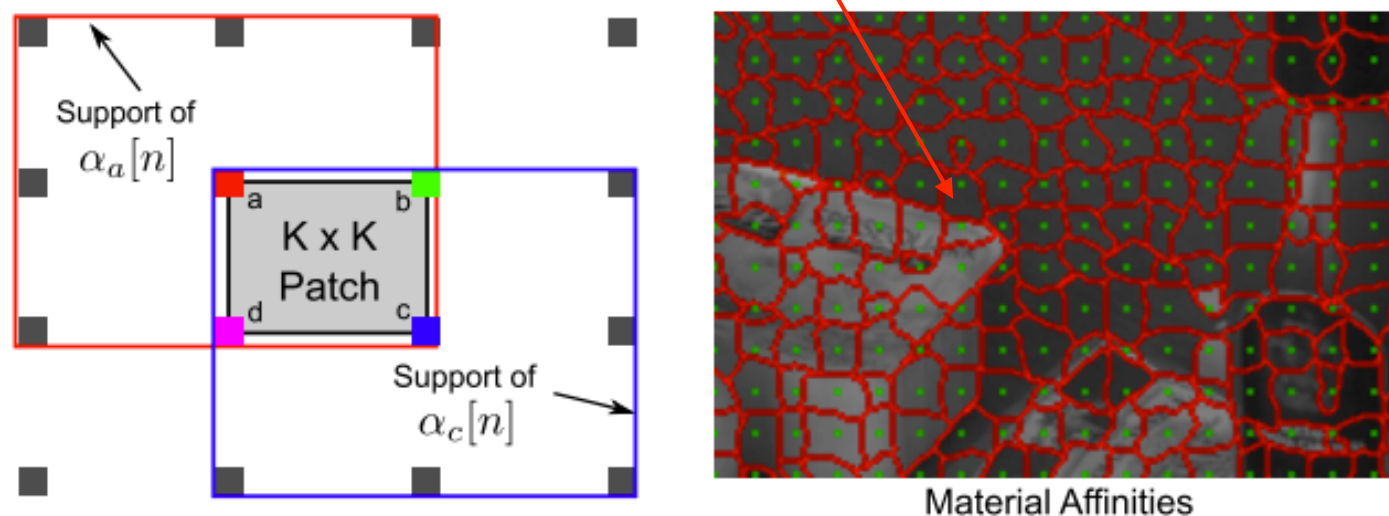
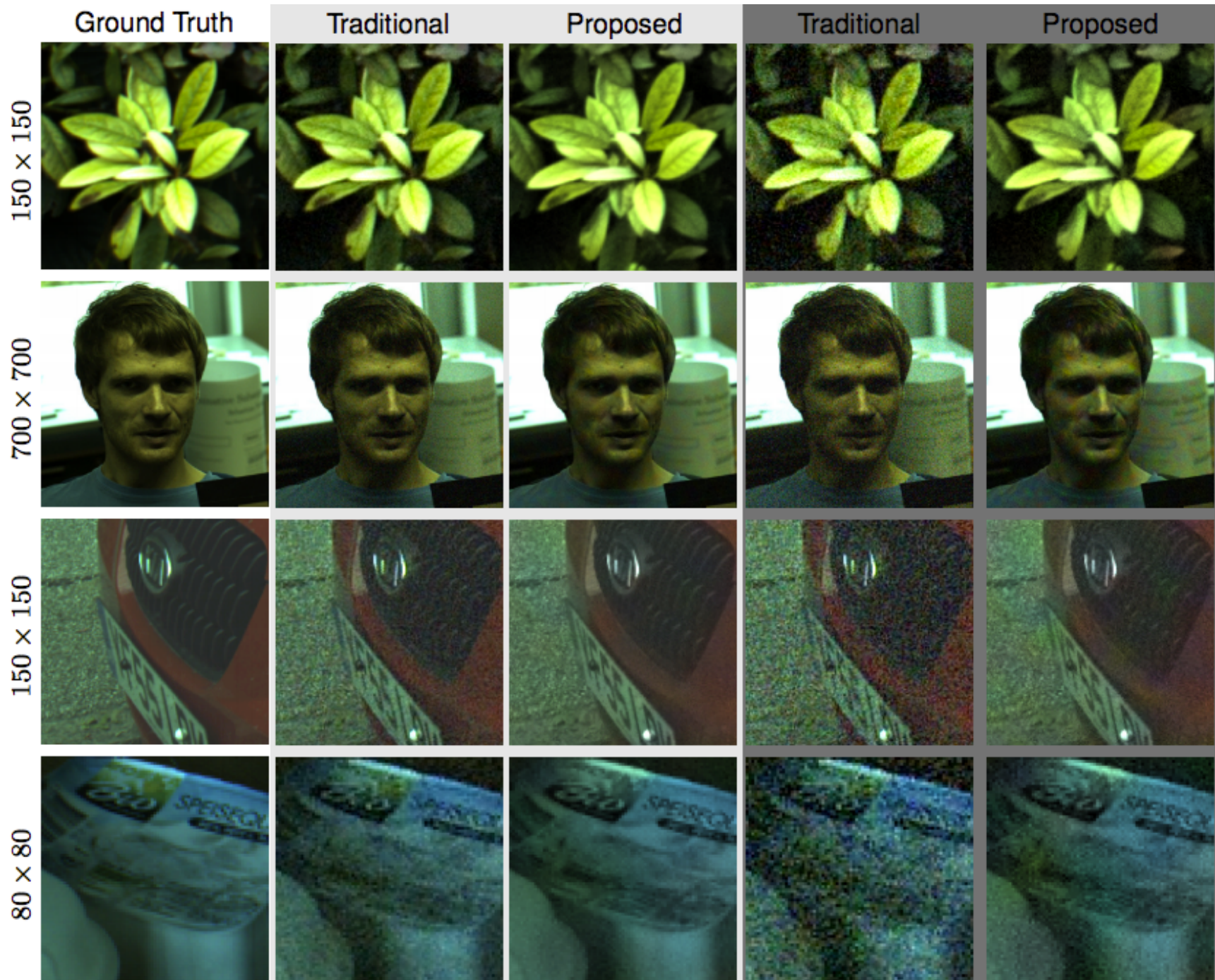
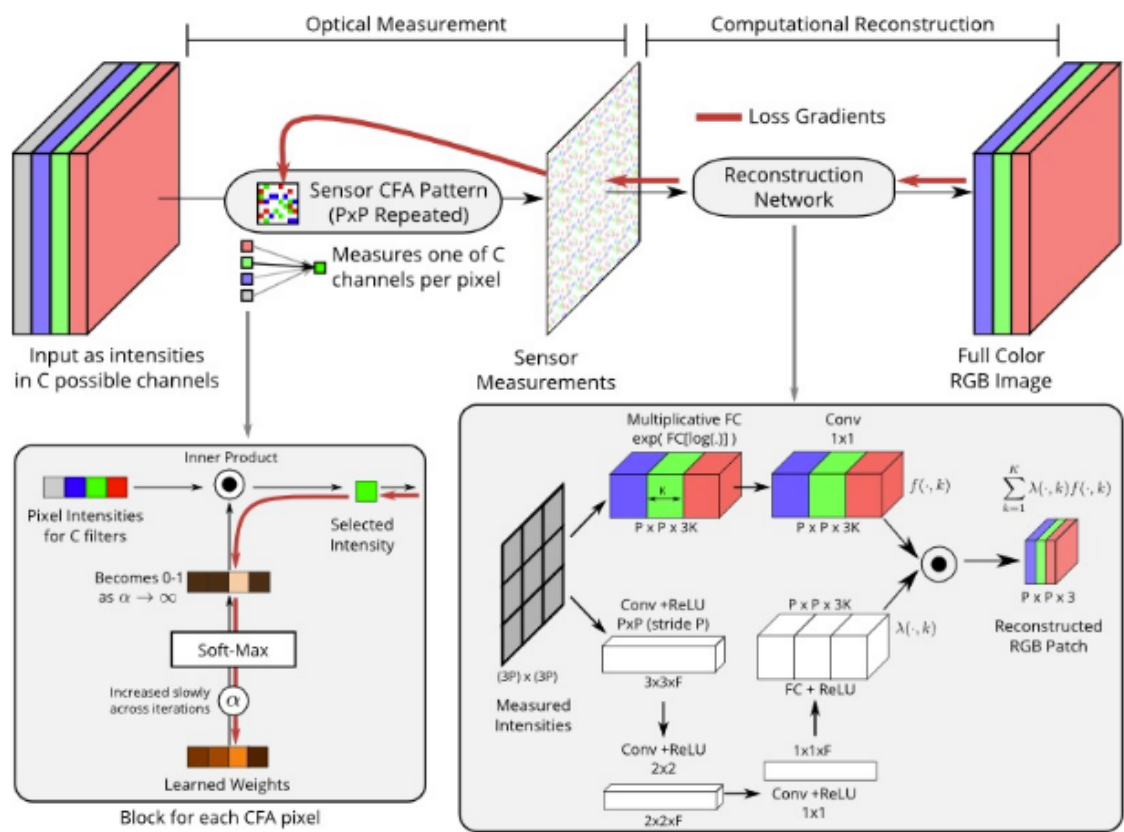


Figure 2. Propagating chromaticity with material affinities. *Left:* Chromaticities at pixels within each  $K \times K$  patch are computed as convex combinations of chromaticities measured by the Bayer blocks at its corners. The combination weights are determined by four affinity maps  $\alpha_j[n]$ , one from each corner Bayer block  $j$ , that encode luminance edge information. *Right:* Affinity map showing regions of pixels with highest affinity to each block (marked in green), super-imposed on the corresponding luminance image.

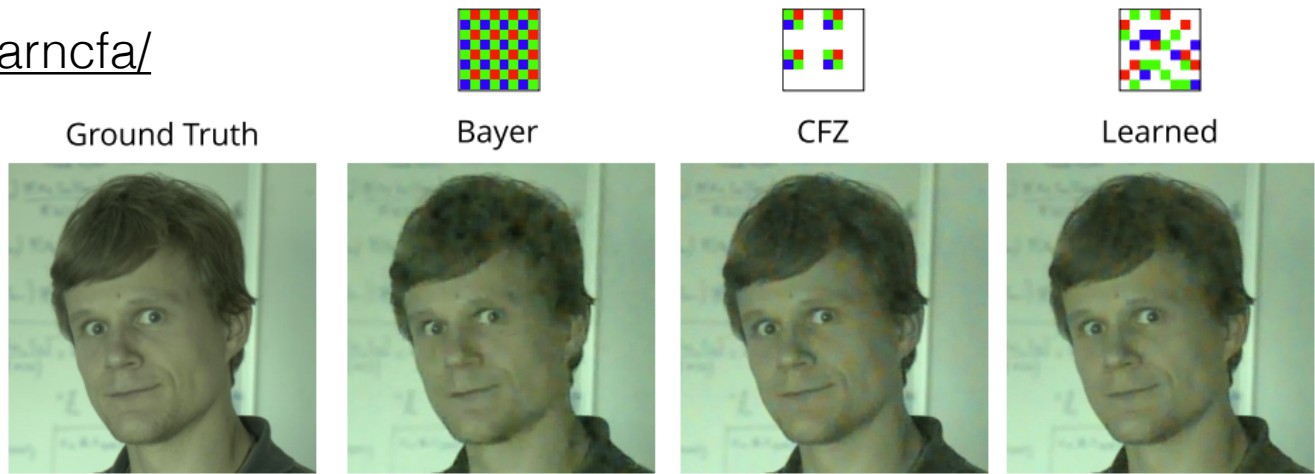


increasing noise level →





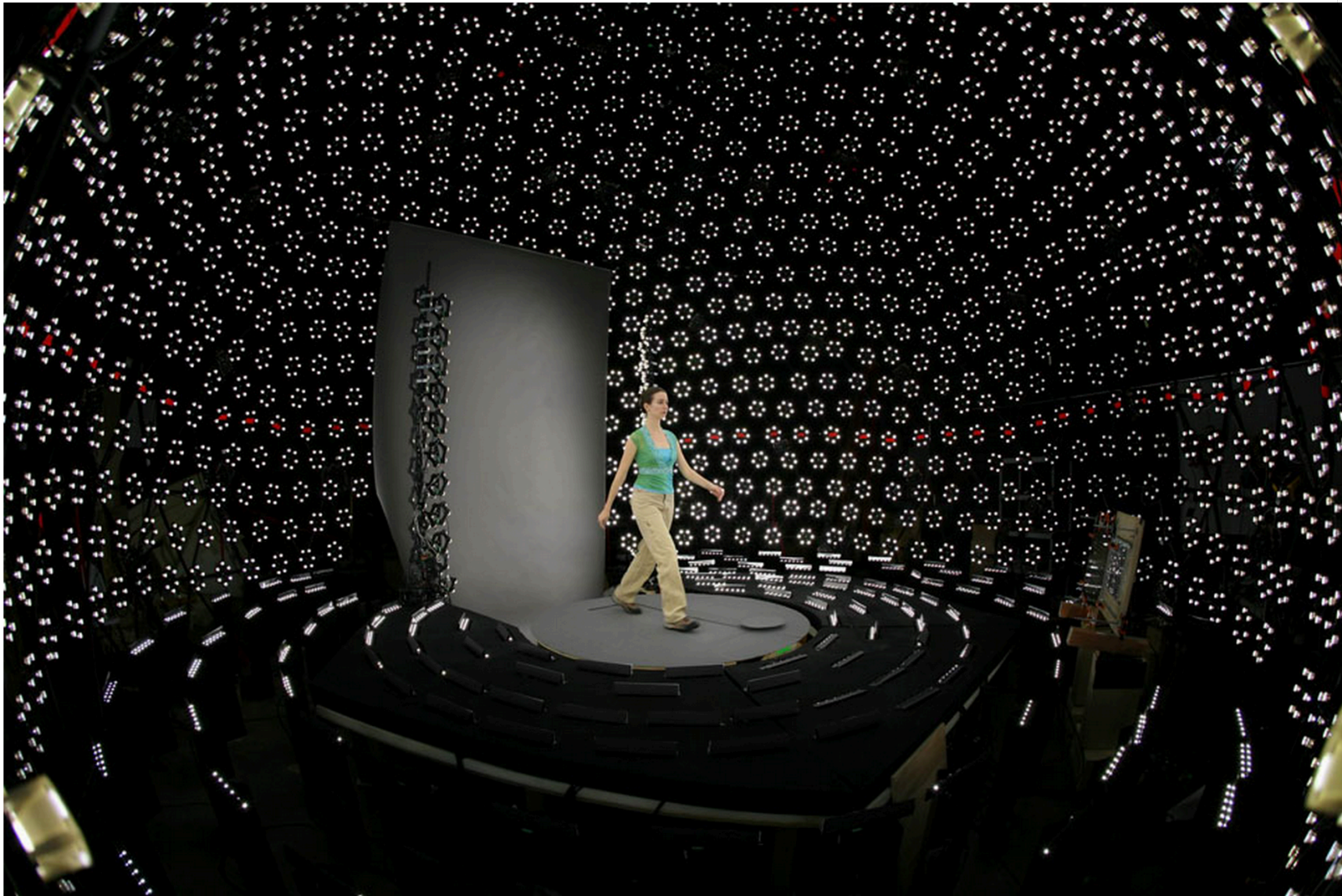
<http://ttic.uchicago.edu/~ayanc/learncfa/>





# Light Stage 6

- ◆ Sample over time, lighting, viewing direction, pose

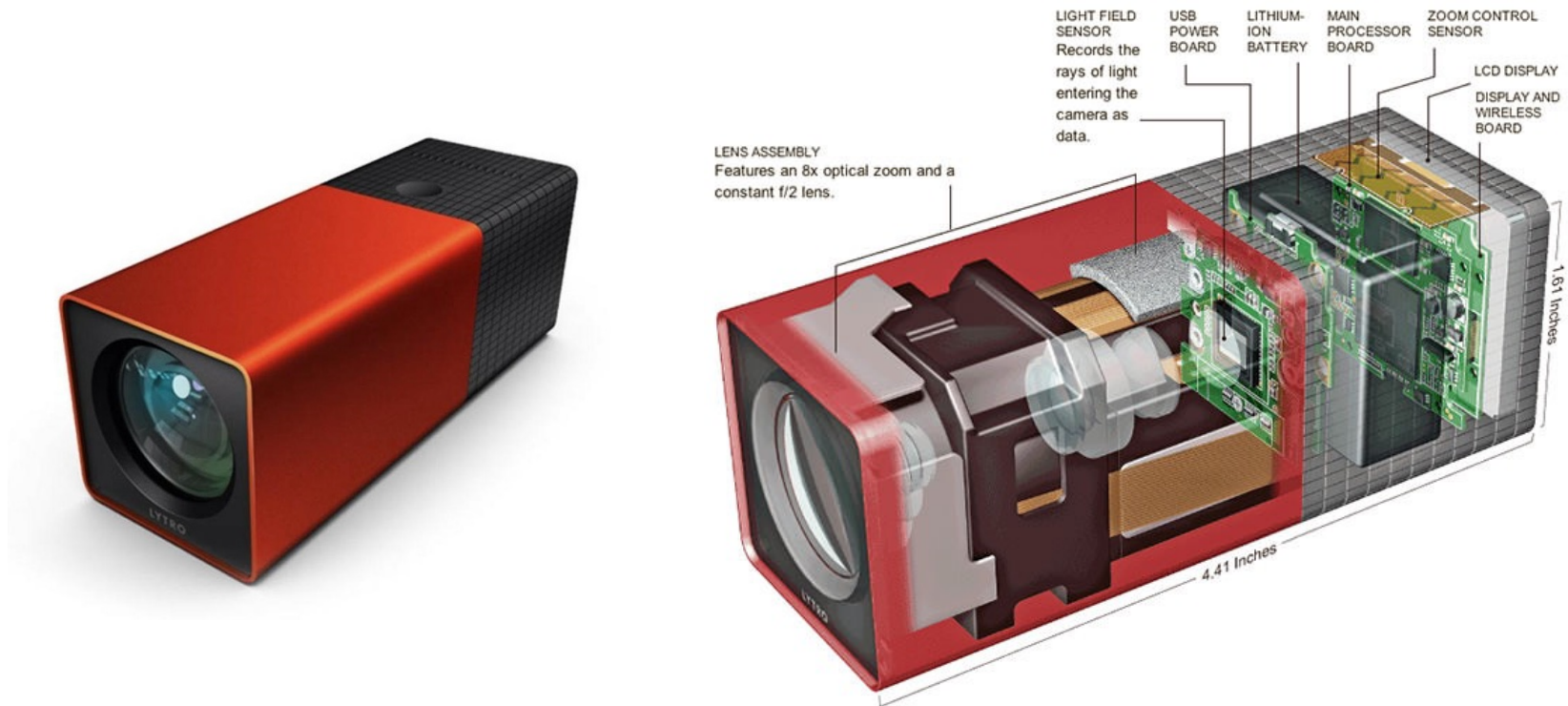


inside Light Stage 6



# Lytro camera

- ◆ Light field camera: capture intensity along each direction of the light
  - ▶ Traditional cameras integrate light coming from all directions
- ◆ A captured light field allows you re-render an image post-hoc
  - ▶ <https://pictures.lytro.com/lytro/collections/41/pictures/1088670>



# More readings and thoughts

- ◆ [History of optics](#), Wikipedia
- ◆ A. Torralba and W. Freeman, [Accidental Pinhole and Pinspeck Cameras](#), CVPR 2012
- ◆ DIY <http://www.pauldebevec.com/Pinhole>
- ◆ In MATLAB, compute the projection of a sphere using the perspective model and visualize the distortions
- ◆ Light stages over time <http://gl.ict.usc.edu/LightStages>
- ◆ Sergey Prokudin-Gorskii photographic collection at the Library of Congress <http://www.loc.gov/exhibits/empire/index.html>
- ◆ Richard Szeliski's book, Sections 2.2.3 - 2.3.2