



23-Analysis Overview

- **Readings:**
 - GJM03 Chapter 6
 - Adr82 Adrion, W.R., M.A. Branstad, and J.C. Cherniavsky, "Validation, Verification and Testing of Computer Software," ACM Computing Surveys, June 1982, pp.159-192
 - Hoa69 Hoare, C.A.R., "An Axiomatic Basis for Computer Programming," Communications of the ACM, October 1969.
 - Flo67 Floyd, R.W. "Assigning Meaning to Programs", in the Proceedings of Symposium on Applied Mathematics, 1967, pp. 19-32, (Appeared as volume 19 of Mathematical Aspects of Computer Science).
 - Han76 Hantler, S.L. and J.C King., "An Introduction to Proving the Correctness of Programs," ACM Computing Surveys, September 1976, pp. 278-300.
 - Cla85 Clarke L. A. and D. J. Richardson, "Applications of Symbolic Evaluation," Journal of Systems and Software, January 1985, 5 (1), pp.15-35.
 - Zhu97 Zhu, Hong, Patrick A. V. Hall, and John H. R. May, "Software Unit Test Coverage and Adequacy," ACM Computing Surveys, vol. 29, no.4, pp. 366-427, December, 1997.
 - Wey80 Weyuker, Elaine J. and Thomas Ostrand, "Theories of Program Testing and the Application of Revealing Subdomains," IEEE Transactions on Software Engineering, May 1980, SE-6(5), pp. 236-246
 - DeM79 DeMillo R.A. and R.J. Lipton and A.J. Perlis, "Social Processes and Proofs of Theorems and Programs, Communications of the ACM, May 1979, 22(5), pp. 271-280





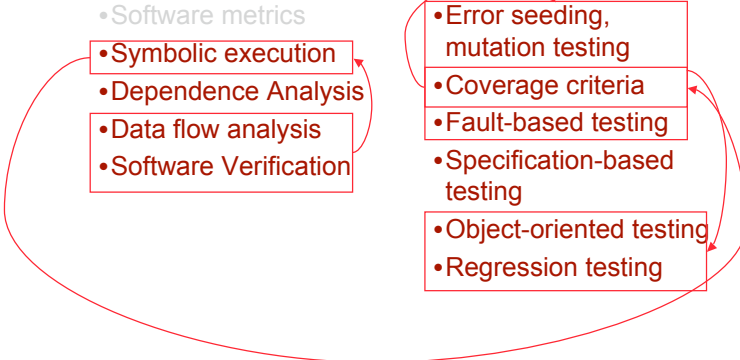


Approaches

- **Static Analysis**
 - Inspections
 - Software metrics

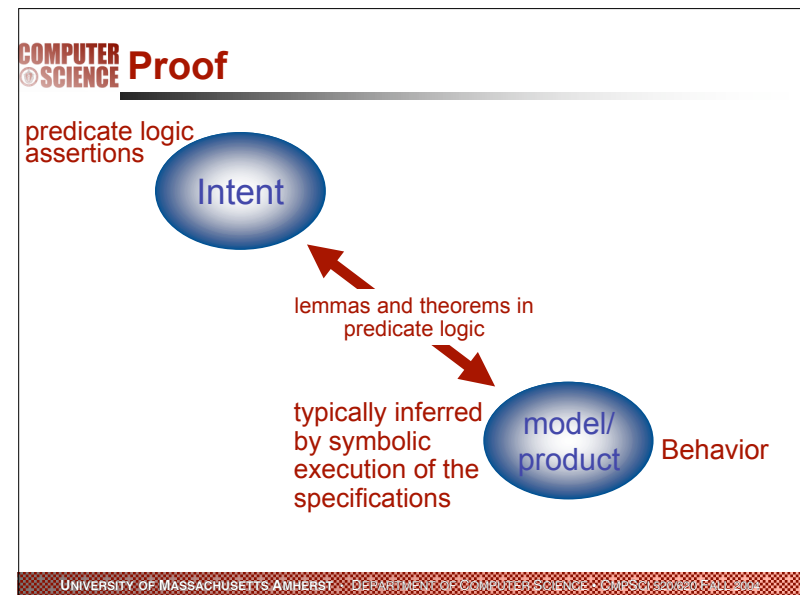
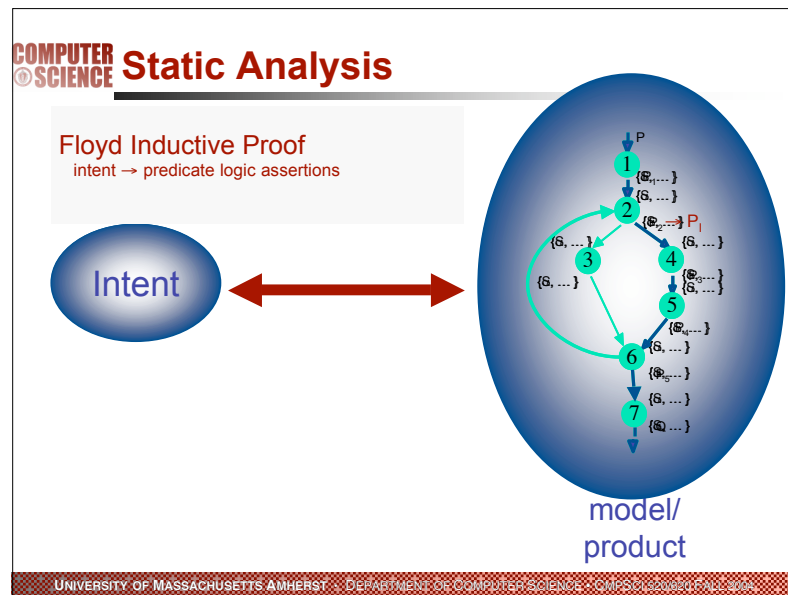
- Symbolic execution
- Dependence Analysis
- Data flow analysis
- Software Verification

- **Dynamic Analysis**
 - **Assertions**
 - Error seeding, mutation testing
 - Coverage criteria
 - Fault-based testing
 - Specification-based testing
 - Object-oriented testing
 - Regression testing



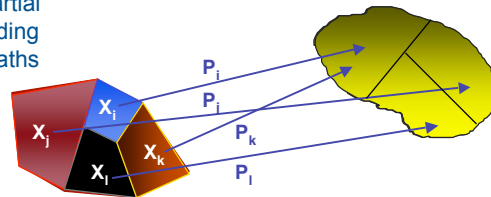






COMPUTER SCIENCE Symbolic Evaluation/Execution

- Creates a functional representation of a path of an executable component
- P is composed of partial functions corresponding to the executable paths
 $P = \{P_1, \dots, P_r\}$
 $P_i : X_i \rightarrow Y$
- For a path P_i
 - $D[P_i]$ is the domain for path P_i
 - $C[P_i]$ is the computation for path P_i



UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE • CMPSCI.520/FALL.2004

COMPUTER SCIENCE Execution tree (Hantler-King)

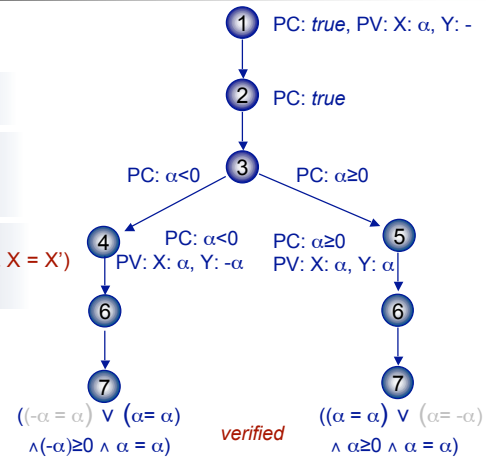
ABSOLUTE

assume (true)

```

1  procedure(X);
2  declare X,Y integer
3  if X<0
4    then Y ← -X;
5    else Y ← X;
6  return (Y);
7  end;
```

prove((Y = X' | Y = -X') & Y ≥ 0 & X = X')



UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE • CMPSCI.520/FALL.2004

COMPUTER SCIENCE **Loops -- unroll them?**

```

n
n+1  do_while predicate1
n+2    if predicate2
n+3      then code ;
n+4      else code ;
n+5    end;
n+6  output assertion ;
    
```

input assertion

output assertion

better: find a loop invariant

UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE • CMPSCI.520/620 FALL 2004

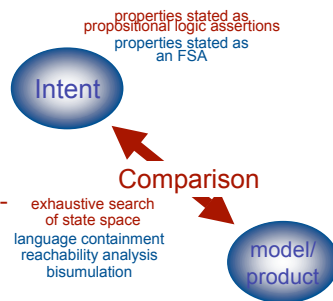
COMPUTER SCIENCE **Straightforward Observations**

- **Problems**
 - formal proofs are long, tedious and are often hard; assertions are hard to get right; invariants are difficult to get right (need to be invariant, but also need to support overall proof strategy)
- **Unsuccessful proof attempt $\Rightarrow$???**
 - incorrect software? assertions? placement of assertion? inept prover? although failed proofs often indicate which of the above is likely to be true (especially to an astute prover)
- **Deeper Issues**
 - undecidability of predicate calculus $\Rightarrow$ no way to be sure when you have a false theorem
 - there is no sure way to know when you should quit trying to prove a theorem (and change something)
 - proofs are generally much longer than the software being verified $\Rightarrow$ errors in the proof are more likely than errors in the software being verified

UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE • CMPSCI.520/620 FALL 2004

Model Checking: Overview

- properties usually expressed in
 - in a propositional logic (e.g., temporal logic)
 - as a FSA
- system represented as a (possibly “abstracted”) reachability graph
- reasoning engine
 - logic $\Rightarrow$ propagates valid sub-formulas through the graph
 - FSA $\Rightarrow$ compares FSAs via language inclusion; reachability; or bisimulation



Conservative Analysis

- If property is verified, property holds for all possible executions of the system
- If property is not verified:
 - an error found
 - OR
 - a spurious result
- System model abstracts information to be tractable
 - Conservative abstractions usually over-approximate behavior
 - If inconsistency relies upon over-approximations, then a spurious result
 - e.g. all counter example correspond to infeasible paths

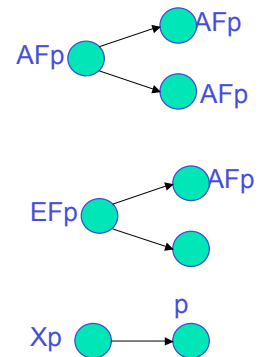
COMPUTER SCIENCE Temporal logic

- augments the standard operators of propositional logic with “tense” operators
- “possible worlds semantics” $\Rightarrow$ Kripke model
 - relativize the truth of a statement to temporal stages or states
 - a statement is not simply true, but true at a particular state
 - states are temporally ordered, with the type of temporal order determined by the choice of axioms.
- model of time
 - partially ordered time
 - linearly ordered time
 - linear temporal logic is typically extended by two additional operators, “until” and “since”
 - discrete time
 - branching (nondeterministic) time
 - foundation for one of the principal approaches to verifying concurrent systems = Computational Tree Logics.

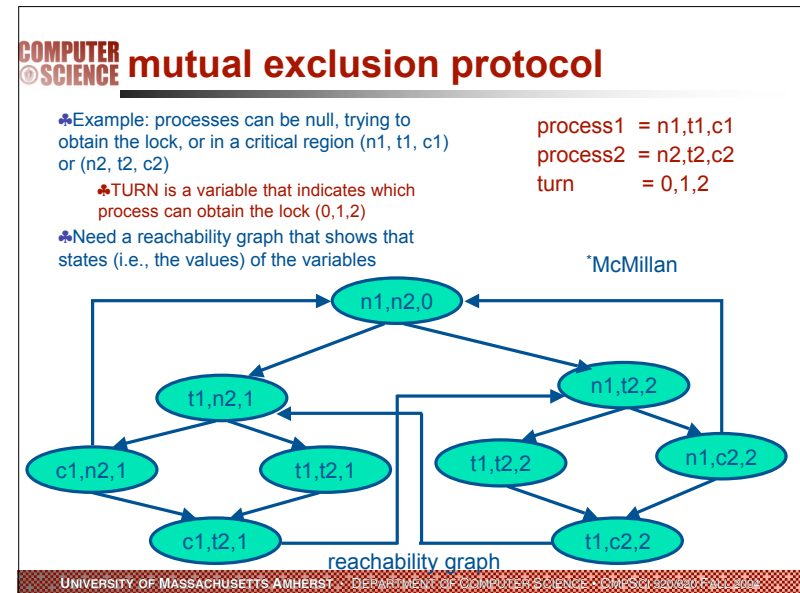
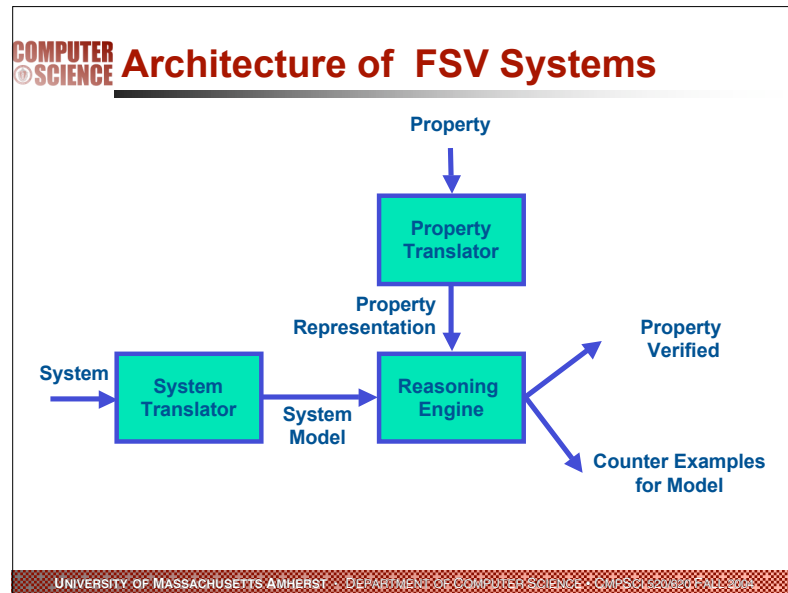
UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE CMPSCI520/620 FALL 2004

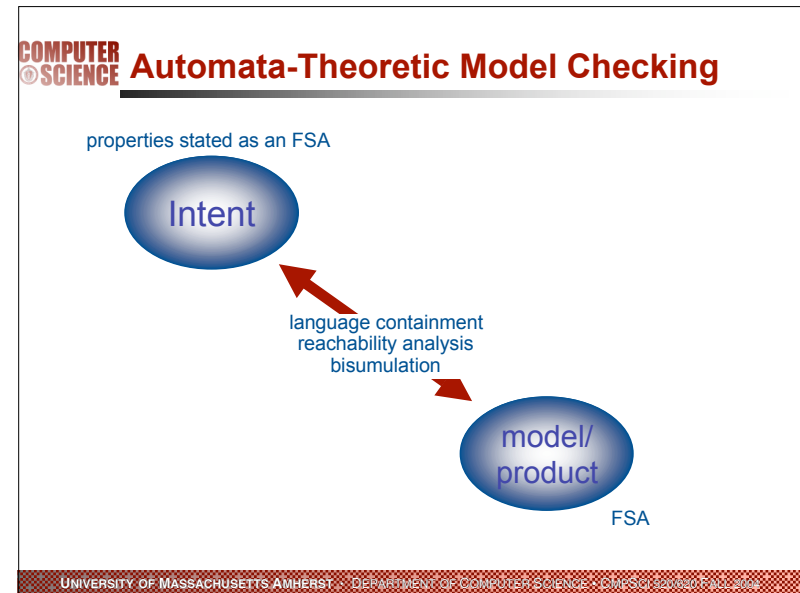
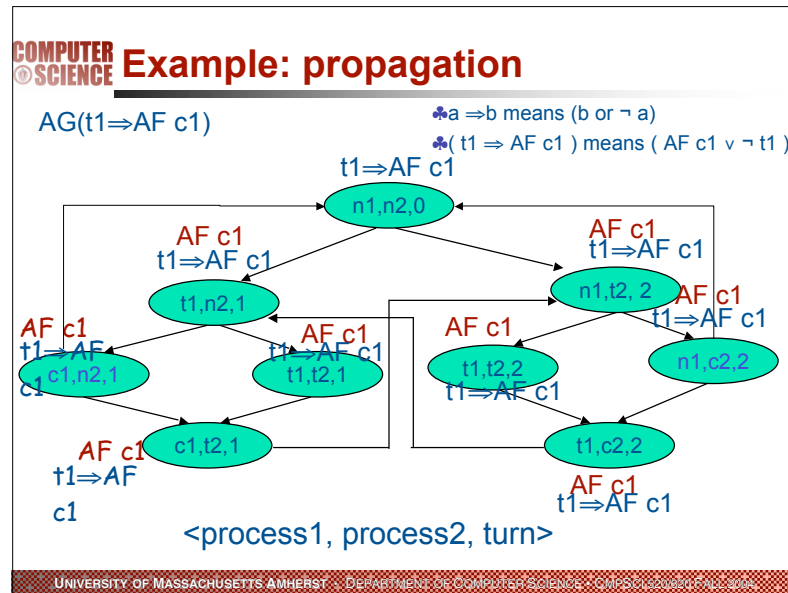
COMPUTER SCIENCE Computation Tree Logics

- specification language
 - a propositional temporal logic.
- verification procedure
 - exhaustive search of the state space of the concurrent system to determine truth of specification.
- formulas constructed from path quantifiers and temporal operators:
 - path quantifier:
 - A “for every path”
 - E “there exists a path”
 - temporal operator:
 - Xp “p holds next time”
 - Fp “p holds sometime in the future”
 - Gp “p holds globally in the future”
 - pUq “p holds until q holds”



UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE CMPSCI520/620 FALL 2004

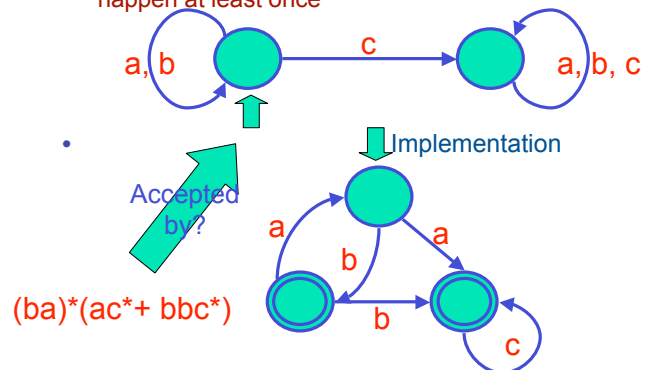




Example

- Specification:

- of the possible observable events (a, b, c), c must happen at least once



Some observations

- Model Checking

- worst case bound linear in size of the model
 - but the model is exponential
- not clear if model checking or symbolic model checking is superior
 - depends on the problem
- experimentally often very effective!
 - used selectively to verify hardware designs
 - trying to develop appropriate abstractions to make it applicable to software systems

Verification

- How are they different?
 - (Automated) mathematical reasoning
 - difficult, error prone
 - decidability vs. expressiveness
 - Propositional calculus is decidable
 - Predicate calculus is semi-decidable
 - Finite-state verification
 - Reason about a finite model of the system
 - Fast, yields counterexamples, manages partial specifications, applies to concurrency
 - State explosion!

Approaches

- Static Analysis
 - Inspections
 - Software metrics
 - Symbolic execution
 - Dependence Analysis
 - Data flow analysis
 - Software Verification
- Dynamic Analysis
 - Assertions
 - Error seeding, mutation testing
 - Coverage criteria
 - Fault-based testing
 - Specification-based testing
 - Object-oriented testing
 - Regression testing

Types of Testing--what is tested

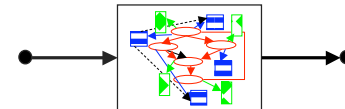
- Unit testing
 - exercise a single simple (procedure) component
- Integration testing
 - exercise a collection of inter-dependent components
 - focus on interfaces between components
- System testing
 - exercise a complete, stand-alone system
- Acceptance testing
 - customer's evaluation of a system
 - usually a form of system testing
- Regression testing
 - exercise a changed system
 - Focus on modifications or their impact

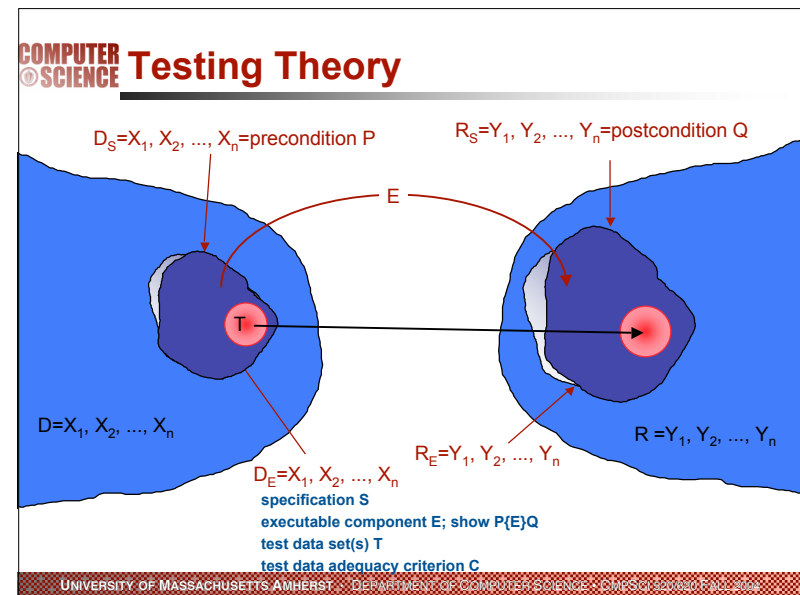
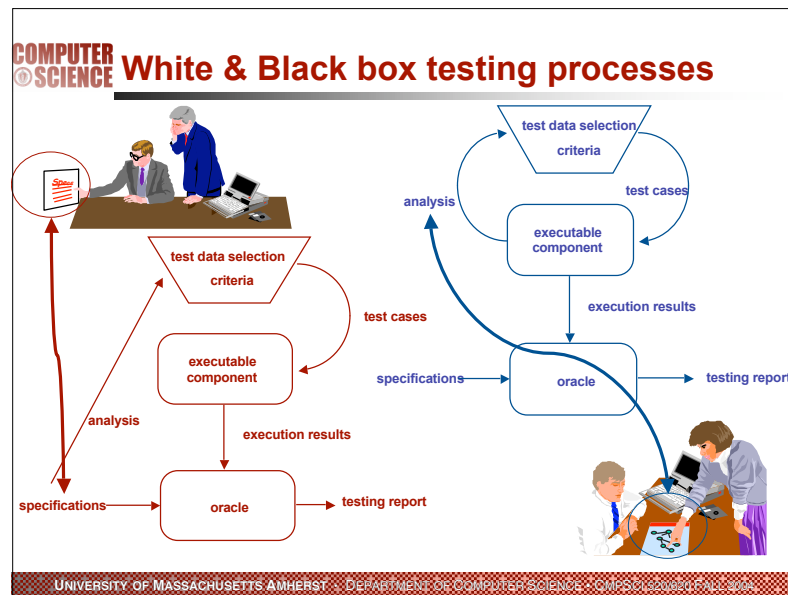
Testing approaches

- “black box”



- “white box” or “glass box”





Testing Theory

• Criterion C for Test Adequacy

$$C: S \times E \rightarrow 2^T$$

• specification-based	$C(s)$	"black box"
• interface-based	$C(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n)$	
• program-based	$C(e)$	
• combined	$C(s, e)$	"white box"

• Types

- structural
- fault-based
- error-based

• if specification S defines a function F, such that $P\{F\}Q$, then C is *reliable* if $T_1, T_2, \dots, T_m; C(T_i, E);$ and $D(E) \supseteq T_i$

- $\forall T_i (\forall t \in T_i, E(t) = F(t)) \vee \forall T_i (\exists t \in T_i, E(t) \neq F(t))$
- $\forall t \in T_i, E(t) = F(t) \Rightarrow \forall t \in T_i, OK(T_i) \Rightarrow E = F$

Ideal Test Criterion

- test criterion C is *ideal* if for any executable component E and every test set $T_i \subseteq D(E)$ such that $C(T_i, E)$, T_i is successful
 - of course we want $T_i \ll D(E)$
 - but in general, $T = D(P)$ is the only ideal test criterion
- In general, there is no ideal test criterion
 - "Testing shows the presence, not the absence of bugs" E. Dijkstra
- Dijkstra was arguing that verification was better than testing
- but, verification has similar problems
 - can't prove an arbitrary program is correct
 - can't solve the halting problem
 - can't determine if the specification is complete
- need to use these techniques so that they compliment one another



Black Box Testing

- Functional/Interface Test Data Selection
 - typical cases
 - boundary conditions/values
 - illegal conditions (if robust)
 - fault-revealing cases
 - based on intuition about what is likely to break the system
 - other special cases
- stress testing
 - large amounts of data
 - worse case operating conditions
- combinations of events
 - select those cases that appear to be more error-prone
- common representations for selecting sequences of events
 - decision tables
 - cause and effect graphs
 - usage scenarios

UNIVERSITY OF MASSACHUSETTS AMHERST · DEPARTMENT OF COMPUTER SCIENCE · CMPSCI.520/620 FALL 2004



“White Box” Test Data Selection

- structural
 - coverage based
- fault-based
 - e.g., mutation testing, RELAY
- error-based
 - domain and computation based
 - use representations created by symbolic execution

UNIVERSITY OF MASSACHUSETTS AMHERST · DEPARTMENT OF COMPUTER SCIENCE · CMPSCI.520/620 FALL 2004

CFG-Based Coverage

- Criteria
 - Statement Coverage
 - Path Coverage
 - Cyclomatic-number
 - Branch Coverage
 - Hidden Paths
 - Loop Guidelines
 - Boundary - Interior
- Selecting paths that satisfy the criteria
 - static selection
 - some of the associated paths may be infeasible
 - dynamic selection
 - monitors coverage and displays areas that have not been satisfactorily covered

“Simple” coverage measures

- Statement Coverage
 - requires that each statement in a program be executed at least once
 - a set P of paths in the CFG satisfies the statement coverage criterion iff $\forall n_i \in N, \exists p \in P$ such that n_i is on path p
- Path Coverage
 - Requires that every path in the program be executed at least once
 - P satisfies the path coverage criterion iff P contains all execution paths from the start node to the end node in the CFG
 - In most programs, path coverage is impossible
- Multiple Condition Coverage
 - T is adequate if for every condition C which consists of atomic predicates $(p_1, p_2, \dots, p_n)$ and all possible combinations $(b_1, b_2, \dots, b_n)$ of their values, there is at least one $t \in T$ such that the value of p_i is equal to b_i for all i

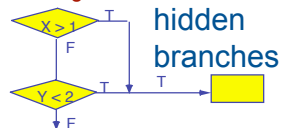
Branch & Loop Coverage

• Branch Coverage

- Requires that each branch in a program (each edge in a control flow graph) be executed at least once

- e.g., Each predicate must evaluate to each of its possible outcomes

- Branch coverage is stronger than statement coverage



• Loop Coverage

- Path 1, 2, 1, 2, 3 executes all branches (and all statements) but does not execute the loop well.

• Better

- fall through case
- minimum number of iterations
- minimum +1 number of iterations
- maximum number of iterations
- maximum -1 number of iterations

1, 2, 1, 2, 1, 2, 3
(1, 2)ⁿ⁻¹, 3
(1, 2)ⁿ, 3

Data Flow Path Selection

• Definitions

- $d_n(x)$ denotes that variable x is assigned a value at node n (defined)
- $u_m(y)$ denotes that variable y is used (referenced at node m)
 - a definition clear path p with respect to (wrt) x is a subpath where x is not defined at any of the nodes in p
 - a definition $d_m(x)$ reaches a use $u_n(x)$ iff there is a subpath $(m) \cdot p \cdot (n)$ such that p is definition clear wrt x

• Rapps and Weyuker

- definition-clear subpaths from definitions to uses

• Ntafos

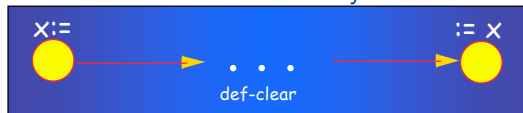
- chains of alternating definitions and uses linked by definition-clear subpaths

• Laski and Korel

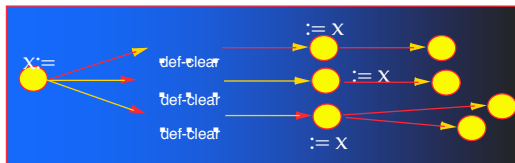
- combinations of definitions that reach uses at a node via a subpath

Rapps' and Weyuker's DF Criteria

- All-Defs - Some definition-clear subpath from each definition to some use reached by that definition

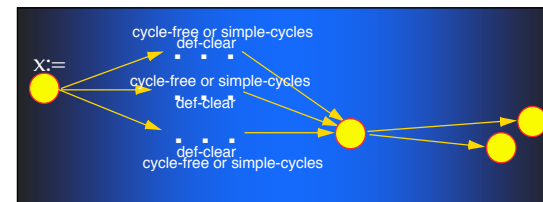


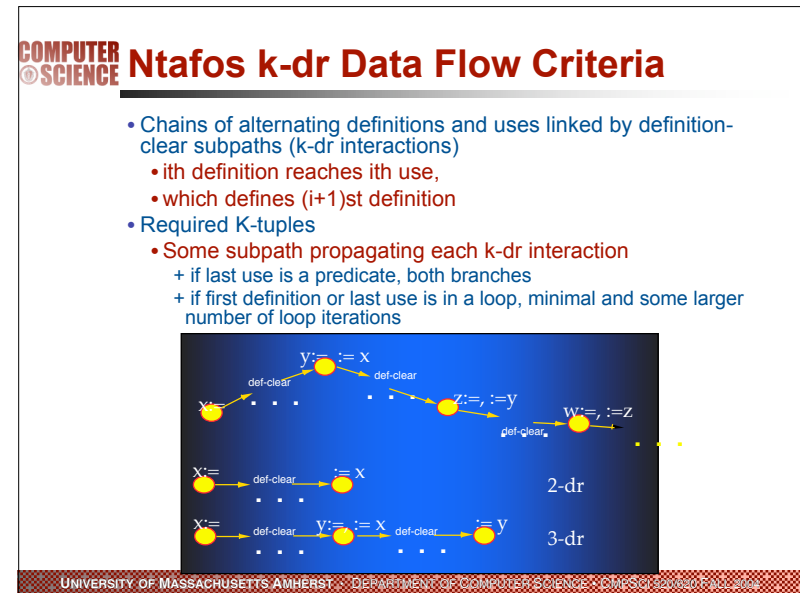
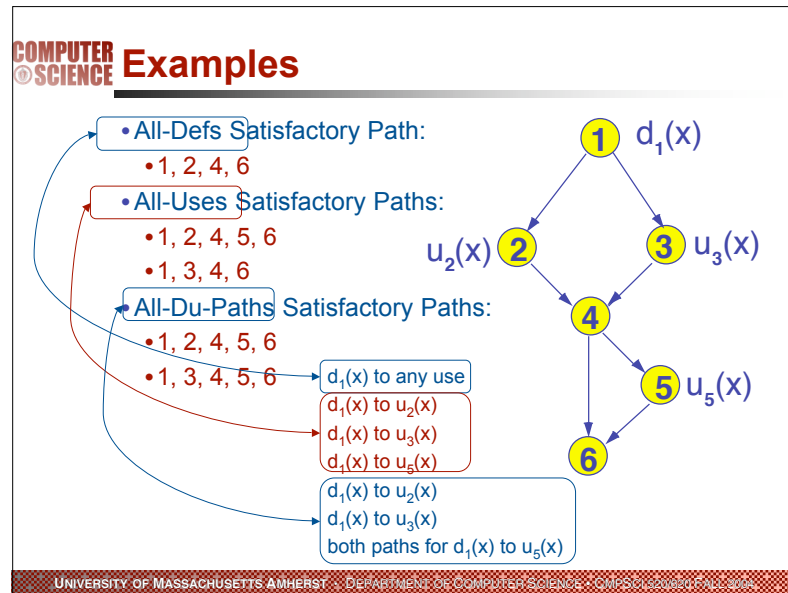
- All-Uses - Some definition-clear subpath from each definition to each use reached by that definition and each successor node of the use



Rapps' and Weyuker's DF Criteria

- All-C-Uses, Some-P-Uses C-use is a "computation use"
P-use is a "predicate use"
 - either All-C-Uses for $dm(x)$ or at least one P-Use
- All-P-Uses, Some-C-Uses
 - either All-P-Uses for $dm(x)$ or at least one C-Use
- All-Du-Paths



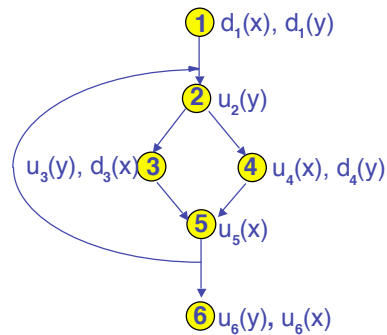


COMPUTER SCIENCE 3-DR interactions

$d_1(x), u_4(x), d_4(y), u_6(y)$
 $d_1(x), u_4(x), d_4(y), u_2(y)$
 $d_1(x), u_4(x), d_4(y), u_3(y)$
 $d_1(y), u_3(y), d_3(x), u_5(x)$
 $d_1(y), u_3(y), d_3(x), u_6(x)$
 $d_1(y), u_3(y), d_3(x), u_4(x)$
 $d_3(x), u_4(x), d_4(y), u_6(y)$
 $d_4(y), u_3(y), d_3(x), u_5(x)$
 $d_4(y), u_3(y), d_3(x), u_6(x)$

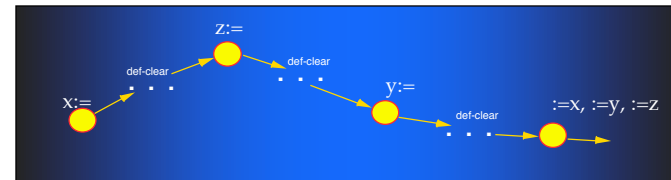
Paths

- 2-DR paths

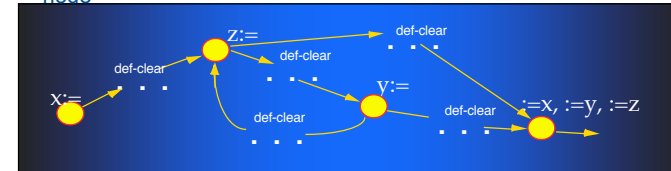


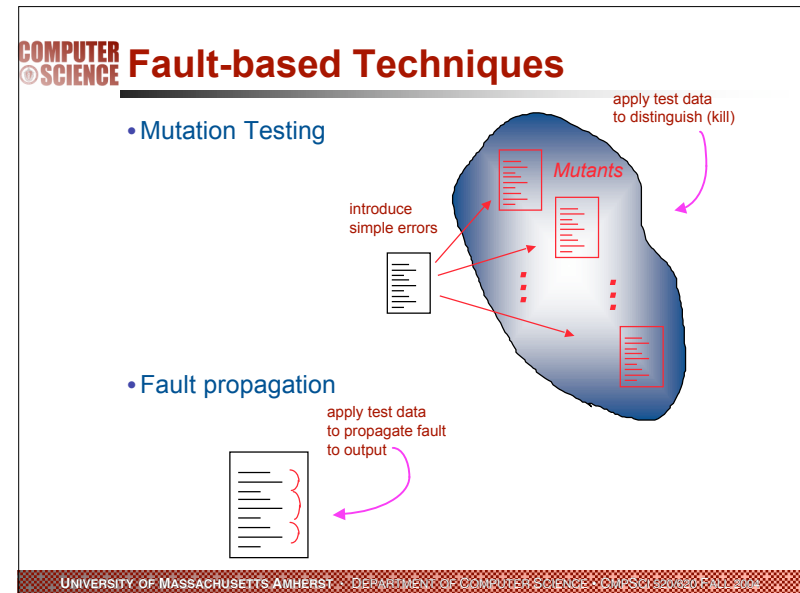
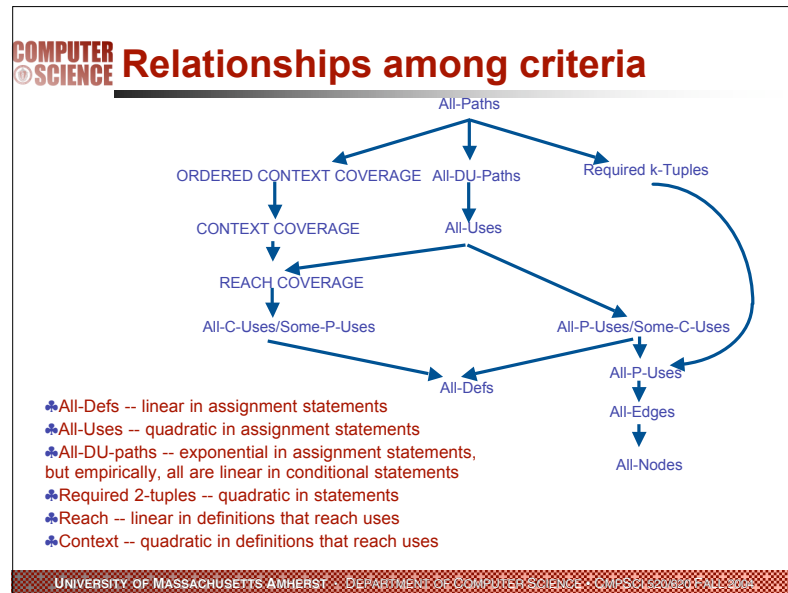
COMPUTER SCIENCE Laski's and Korel's Criteria

- Context Coverage - Some subpath along which each set of definitions reach uses at some node



- Ordered Context Coverage - Some subpath along which each ordering of each sequence of definitions reach uses at some node





Mutation Testing

- **Competent Programmer Hypothesis**
 - programmers write programs that are reasonably close to the desired program
 - e.g., sort program is not written as a hash table
- **Coupling Effect**
 - detecting simple atomic faults will lead to the detection of more complex faults
- **considers all simple (atomic) faults that could occur**
 - introduces single faults one at a time to create “mutants” of original program
 - interactively(?) apply test data to complete (or partial) set of mutants
 - “test adequacy” is measured by “mutants killed”

operand mutations:

$A := X + 1; \Rightarrow A := X + 2 \text{ or } A := X + Y$

binary operator replacement:

$A := X + 1; \Rightarrow A := X - 1 \text{ or } A := X * 1$

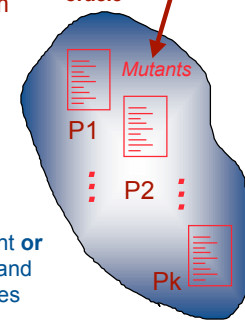
statement replacement:

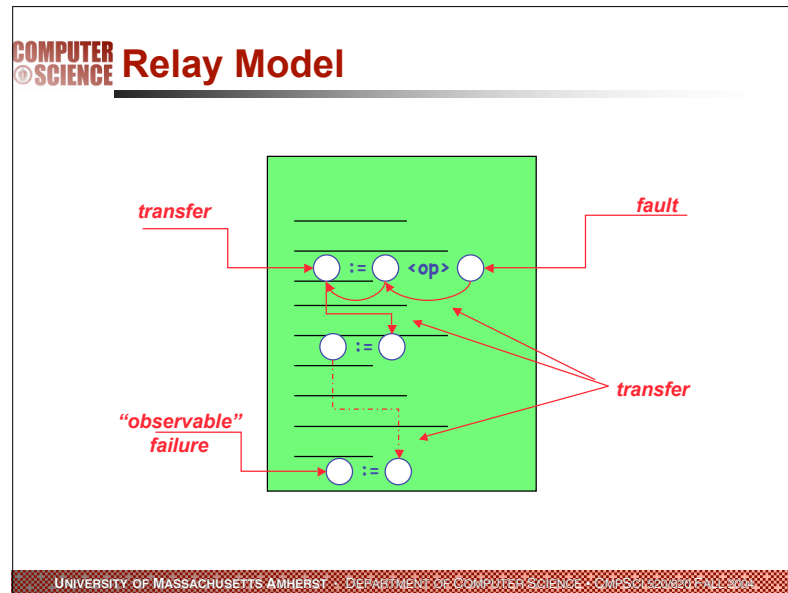
$A := X + 1; \Rightarrow \text{continue or } \Rightarrow \text{return}$

Mutation testing process

- **Execute program P on test set T**
 - save results R to serve as an oracle
 - P is considered the “correct” program
- **Each fault results in a new program**
 - Mutant programs = $P_1, \dots, P_k$
- **Execute each mutant P_i on T and compare results R_i to R**
 - If $R_i \neq R$ then mutant is killed
 - if $R_i = R$ then either
 - $P_i = P$, thus it is an **equivalent** mutant or the test cases do not reveal the error and **need to find a new test case** that does

apply test data to distinguish (kill) by comparing output with “oracle”





COMPUTER SCIENCE **Other Fault-Based techniques:**

- mutating test data
 - instead of mutating program, mutate input
- Bart Miller did an experiment where he demonstrated that arbitrary strings caused UNIX to consistently fail
 - wanted to understand why storms caused his connection to go down

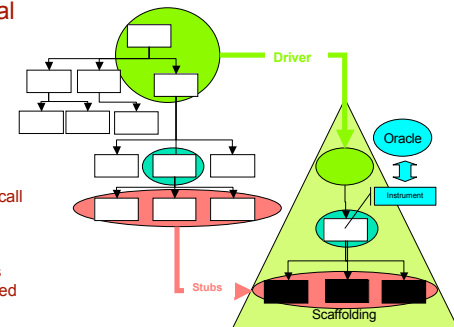
UNIVERSITY OF MASSACHUSETTS AMHERST · DEPARTMENT OF COMPUTER SCIENCE · CMPSCI.520/620 FALL 2004

Putting it all together

- unit testing
- integration & system testing
- regression testing

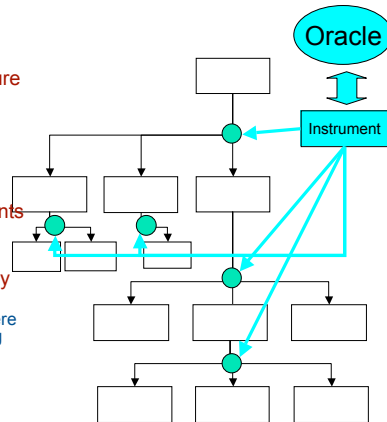
Unit testing

- test scaffolding
 - can be created for general or for specific tests
 - is composed of
 - one or more drivers
 - provide a prototype activation environment
 - drivers initialize non-local variables and parameters and call the unit
 - one or more stubs
 - provide a prototype of the units used by the program to be tested
 - one or more oracles
 - identify the tests that cause failures.



COMPUTER SCIENCE Unit vs. Integration vs. System Testing

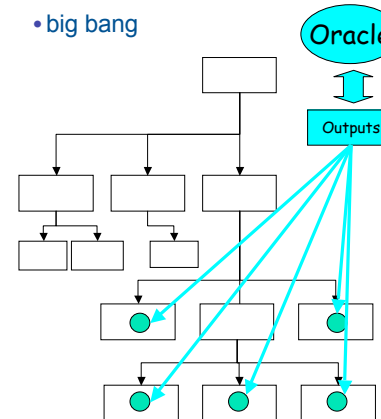
- **Integration testing**
 - focuses on communication and interface problems
 - tests derived from module interfaces and detailed architecture specifications
 - some scaffolding is required
- **System testing**
 - focuses on the behavior of the system as a whole
 - tests are derived from requirements specifications
 - code is seen as a black box
 - support of scaffoldings not usually needed
 - exception is embedded code, where some simulation of the embedding environment may be required



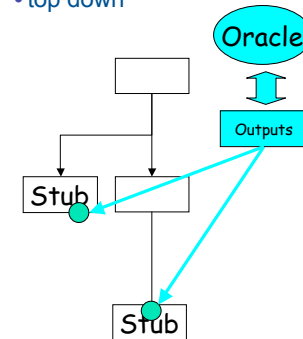
UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE CMPSCI520/620 FALL 2004

COMPUTER SCIENCE Integration testing strategies

- **big bang**



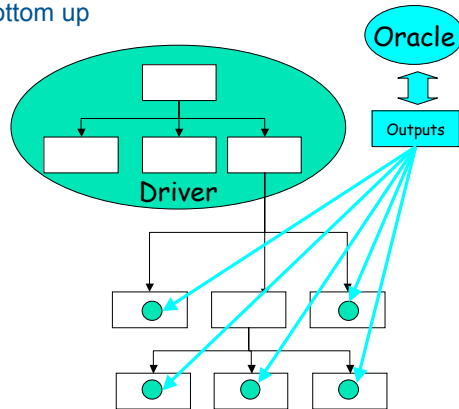
- **top down**



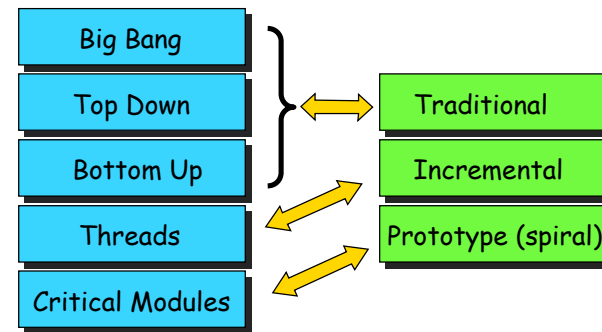
UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE CMPSCI520/620 FALL 2004

Integration testing strategies

- bottom up



Relation to design





O-O Programs are Different

- High Degree of Reuse
 - Does this mean more, or less testing?
- Unit Testing vs. Class Testing
 - What is the right "unit" in OO testing?
- Review of Analysis & Design
 - Classes appear early, so defects can be recognized early as well



Testing OOA and OOD Models

- Correctness (of each model element)
 - Syntactic (notation, conventions)
 - review by modeling experts
 - Semantic (conforms to real problem)
 - review by domain experts
- Consistency (of each class)
 - Revisit Class Diagram
 - Trace delegated responsibilities
 - Examine / adjust cohesion of responsibilities
- Evaluating the Design
 - Compare behavioral model to class model
 - Compare behavioral & class models to the use cases
 - Inspect the detailed design for each class (algorithms & data structures)



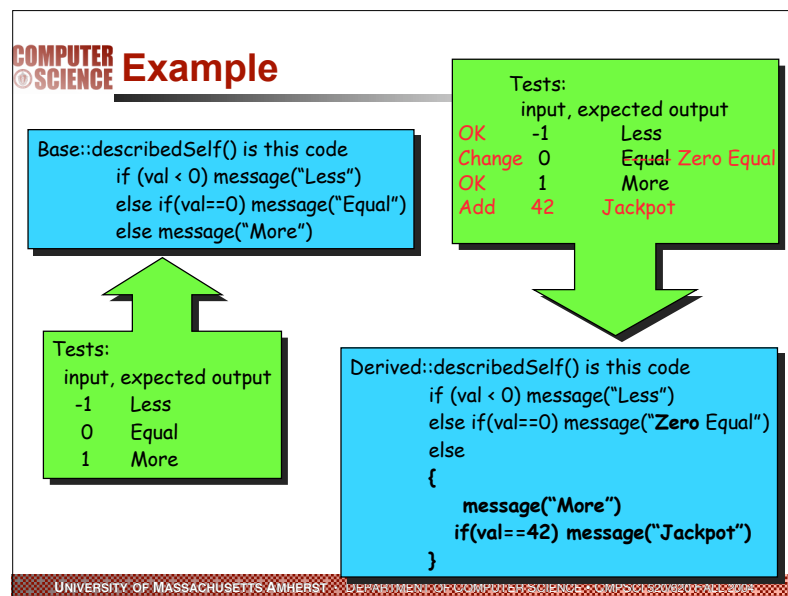
Unit Testing

- What is a "Unit"?
 - Traditional: a "single operation"
 - O-O: encapsulated data & operations
- Smallest testable unit = class
many operations
- Inheritance
 - testing "in isolation" is impossible
 - operations must be tested every place they are used



Issues in O-O testing

- Need to re-examine all testing techniques and processes
 - Primary Issues:
 - implications of encapsulation
 - implications of inheritance
 - implications of genericity
 - implications of polymorphism
 - Changes concerns
 - State of instance variables
 - Sequences of methods calls
 - Must test a class and its specializations



COMPUTER SCIENCE White-box vs. Black-box Testing

- The distance between object-oriented specification and implementation is typically small
 - gap (and therefore usefulness) of the white-box/black-box distinction is decreasing
- But object-oriented specification describes functional behavior, while the implementation describes how that is achieved
- These techniques can be adapted to method testing, but are not sufficient for class testing
- Conventional flow-graph approaches
 - may be inconsistent the object-oriented paradigm
 - method-level control faults are not likely

UNIVERSITY OF MASSACHUSETTS AMHERST DEPARTMENT OF COMPUTER SCIENCE CMPSCI520/620 FALL 2004



Black-box O-O Testing

- Conventional black-box methods are useful for object-oriented systems
 - error-guessing strategies
 - verification of ADTs can be adapted to object-oriented systems
- Other approaches
 - utilize specifications integrated with the implementation as assertions
 - specification integrated with the implementation as dynamic assertions
 - C++ assertions or Eiffel pre/post-conditions offer similar self-checking
 - Utilize method (event) sequence information
 - usually don't have history of method invocations so can't do this with assertions

UNIVERSITY OF MASSACHUSETTS AMHERST · DEPARTMENT OF COMPUTER SCIENCE · CMPSCI520/620 FALL 2004



Encapsulation

- not a source of errors but may be an obstacle to testing
- how to get at the concrete state of an object?
- use the abstraction
 - state is inspected via access methods
 - equivalence scenarios
 - comparing sequences of events
 - state is implicitly inspected by comparing related behavior
 - examine sequences of events
 - need to be able to define what are equivalent sequences and need to determine equal states
- use or provide hidden functions to examine the state
 - useful for debugging throughout the life of the system
 - but modified code, may alter the behavior
 - especially true for languages that do not support strong typing
- proof-of-correctness techniques
 - a proved method could be excused from testing to bootstrap testing of other methods
 - state reporting methods tend to be small and simple, they should be relatively easy to prove

UNIVERSITY OF MASSACHUSETTS AMHERST · DEPARTMENT OF COMPUTER SCIENCE · CMPSCI520/620 FALL 2004

Implications of Inheritance

- rule rather than the exception?
- inherited features usually require re-testing
 - because a new context of usage results when features are inherited
 - multiple inheritance increases the number of contexts to test
- specialization relationships
 - implementation specialization should correspond to problem domain specialization
 - reusability of superclass test cases depends on this

Which fns must be tested

Base class contains:
inherited(int x)
redefined() - returns a number in range 1 to 10 inclusive

Derived class contains:
redefined() - returns a number in range 0 to 20 inclusive
//inherited() is inherited

- derived::redefined has to be tested afresh
- does derived::inherited() have to be retested?

inherited contains the code:
if (x<0)
x = x/redefined()
return x

have to test
when x<0, could
divide by 0

- derived::inherited() may not have to be completely tested
 - if code in inherited() doesn't depend on redefined(), doesn't call it nor call any code that indirectly calls it



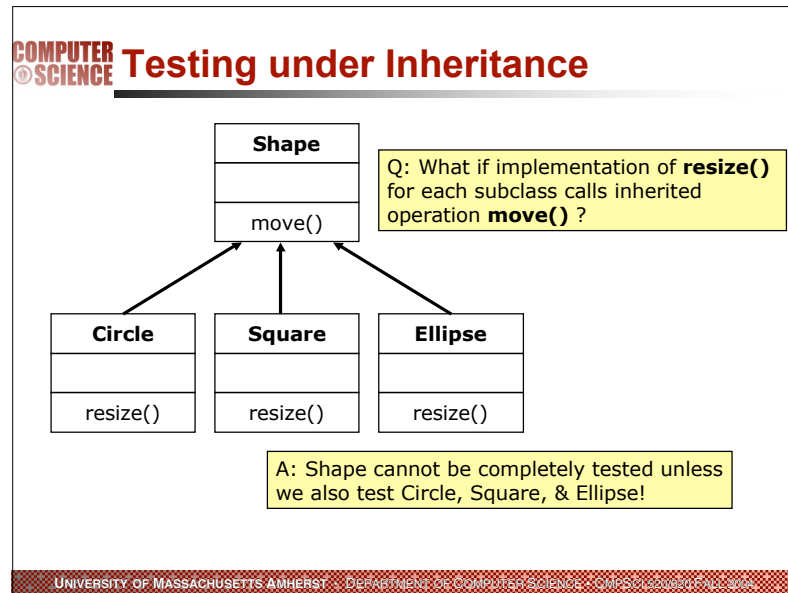
Inheritance Testing

- flattening inheritance
 - each subclass is tested as if all inherited features were newly defined
 - tests used in the super-classes can be reused
 - many tests are redundant
- incremental testing
 - reduce tests only to new/modified features
 - determining what needs to be tested requires automated support



Polymorphism

- in procedural programming, procedure calls are statically bound
- each possible binding of a polymorphic component requires a separate set of test cases
 - many server classes may need to be integrated before a client class can be tested
- may be hard to determine all such bindings
- complicates integration planning and testing



COMPUTER SCIENCE **Integration Testing**

- O-O Integration: Not Hierarchical
 - Coupling is not via subroutine
 - “Top-down” and “Bottom-up” have little meaning
- Integrating one operation at a time is difficult
 - Indirect interactions among operations

UNIVERSITY OF MASSACHUSETTS AMHERST · DEPARTMENT OF COMPUTER SCIENCE · CMPSCI.520/620 FALL 2004



O-O Integration Testing

- **Thread-Based Testing**
 - Integrate set of classes required to respond to one input or event
 - Integrate one thread at a time
 - Example: Event-Dispatching Thread vs. Event Handlers in Java
 - Implement & test all GUI events first
 - Add event handlers one at a time
- **Use-Based Testing**
 - Implement & test independent classes first
 - Then implement dependent classes (layer by layer, or cluster-based)
 - Simple driver classes or methods sometimes required to test lower layers



Test Case Design

- Focus: "Designing sequences of operations to exercise the states of a class instance"
- **Challenges**
 - Observability - Do we have methods that allow us to inspect the inner state of an object?
 - Inheritance - Can test cases for a superclass be used to test a subclass?
- **Test Case Checklist**
 - Identify unique tests & associate with a particular class
 - Describe purpose of the test
 - Develop list of testing steps:
 - Specified states to be tested
 - Operations (methods) to be tested
 - Exceptions that might occur
 - External conditions & changes thereto
 - Supplemental information (if needed)